

Bearing Capacity Of Soil

Definitions:

Bearing Capacity:

أقصى ضغط يمكن أن يضغط به المنشأ على التربة بدون حدوث انهيار للتربة بالقص أو حدوث هبوط زائد.

Ultimate bearing capacity (q_{ult}):

أقل ضغط كلى عند قاعدة الأساس تنهار عنده التربة بالقص.

Net ultimate bearing capacity (q_{un}):

أقل ضغط صافي يسبب انهيار للتربة بالقص.

$$q_{un} = q_{ult} - \gamma * D_F$$

Net safe bearing capacity (q_{ns}):

It is the ultimate bearing capacity over a factor of safety (F).

$$q_{ns} = \frac{q_{un}}{F.O.S}$$

لو لم يعطي $F.O.S = 3$

Safe bearing capacity (q_s):

أقصى إجهاد (ضغط) يمكن أن تتحمله التربة بأمان من حدوث انهيار للتربة بالقص.

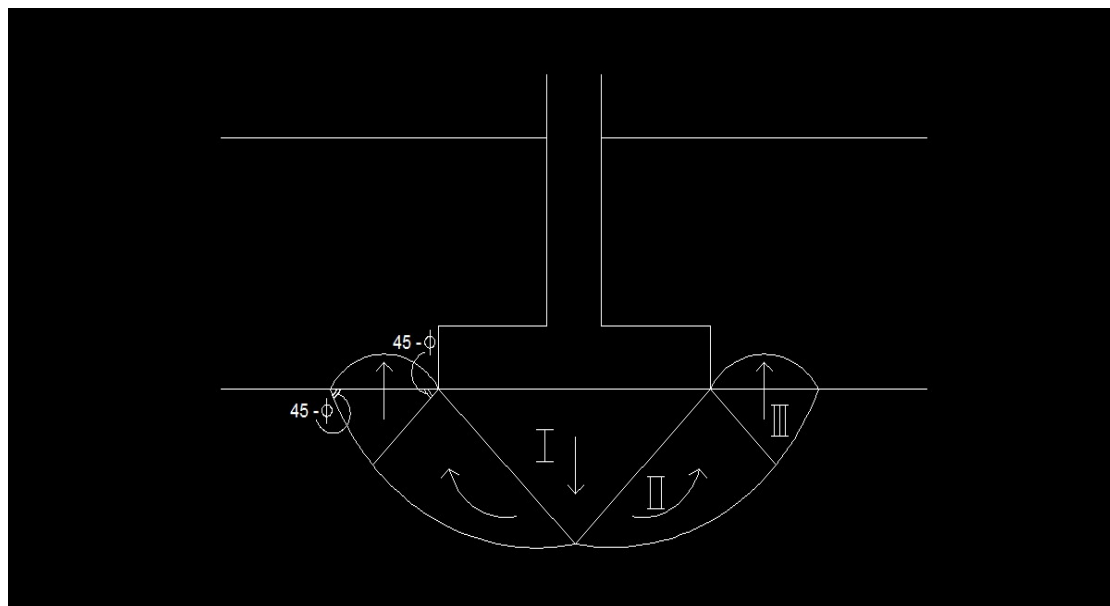
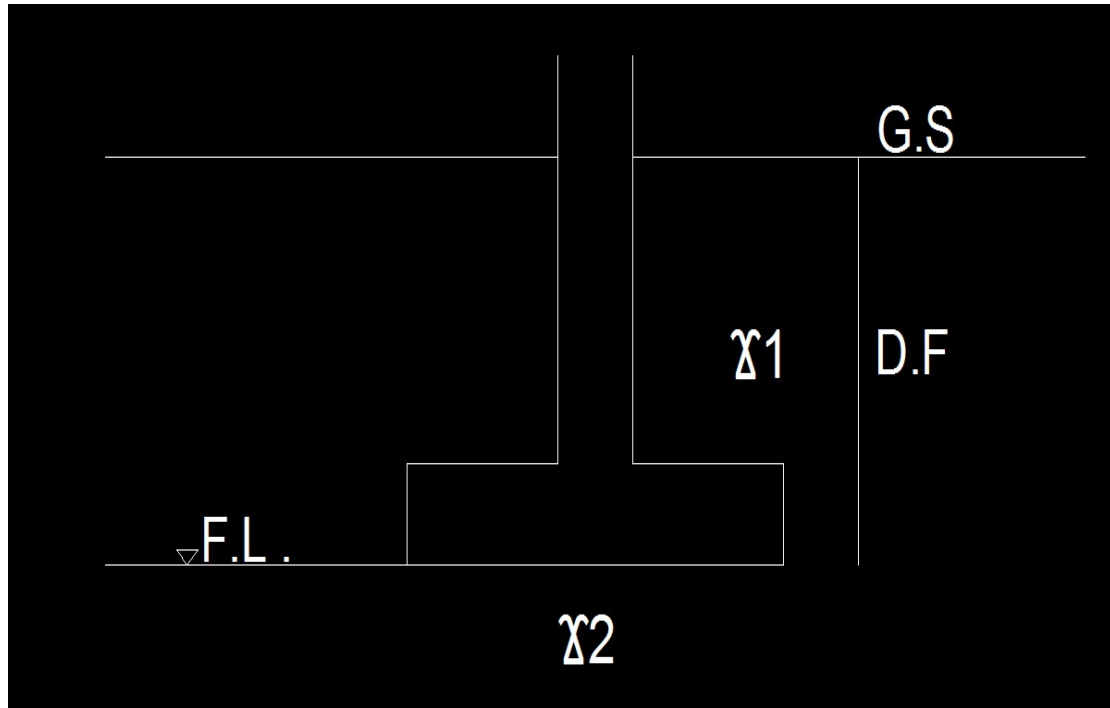
$$q_s = q_{ns} + \gamma * D_F$$

Allowable bearing capacity (q_{all}):

أقصى إجهاد (ضغط) آمن للتربة من حدوث انهيار بالقص أو هبوط زائد.

$$P_{all} = q_s * B * L$$

Terzaghi bearing capacity equation:



$$q_{ult} = k_1 c N_c + k_2 \gamma_1 D_F N_q + k_3 \gamma_2 B N_\gamma$$

حيث أن:

k_1, k_2, k_3 shape factor from table

shape	k_1	k_2	k_3
Strip Footing قاعدة شرطية	1	1	0.5
Rectangular Footing قاعدة مستطيلة	$1+0.3\frac{B}{L}$	1	$1-0.6\frac{B}{L}$
Square Footing قاعدة مربعة	1.3	1	0.4
Circular Footing قاعدة دائرية	1.3	1	0.3

C	Cohesion	التماسك بين الحبيبات
B	Foundation Width	عرض الأساس (البعد الأصغر)
L	Foundation Length	طول الأساس (البعد الأكبر)
γ_1	Soil intensity above F.L	كثافة التربة اعلي منسوب التأسيس
γ_2	Soil intensity under F.L	كثافة التربة أسفل منسوب التأسيس
D_F	Foundation Depth	عمق التأسيس
F.L	Foundation Level	منسوب التأسيس
N_c	B/C Factors	من الجدول ندخل بقيمة γ نوجد قيمة N_c
N_q	B/C Factors	من الجدول ندخل بقيمة γ نوجد قيمة N_q
N_γ	B/C Factors	من الجدول ندخل بقيمة γ نوجد قيمة N_γ

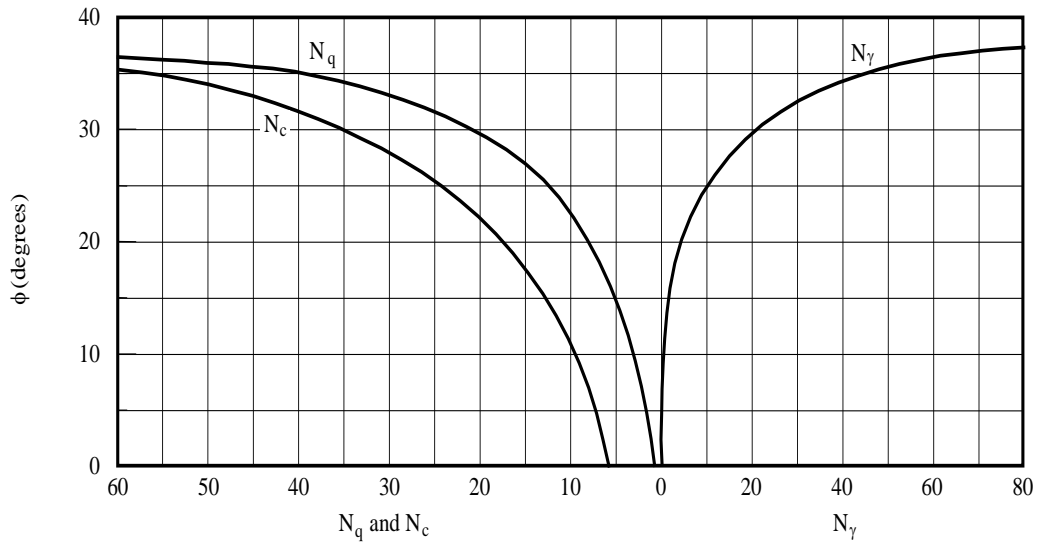
يوجد 3 طرق لإيجاد قيمة N_c , N_q , N_γ

الطريقة الأولى: من الجدول ندخل بقيمة ν نوجد قيمة N_q ,

N_c , N_γ

Angle of Internal Friction (ν)	N_c	N_q	N_γ
0	5	1	-
5	6.5	1.5	-
10	8.5	2.5	0.5
15	11	4	1
20	15	6.5	2
22.5	17.5	8	3
25	20.5	10.5	4.5
27.5	25	14	7
30	30	18	10
32.5	37	25	15
35	46	33	23
37.5	58	46	34
40	75	64	53
42.5	99	92	83

الطريقة الثانية:



الطريقة الثالثة: من المعادلات

$$N_q = e^{\pi \tan \phi} * \tan^2 (45 + \phi/2)$$

$$N_c = (N_q - 1) \cot \phi$$

$$N_\chi = (N_q - 1) \tan \phi$$

$$q_{ult} = k_1 c N_c + k_2 \lambda_1 D_F N_q + k_3 \lambda_2 B N_\gamma$$

Cohesion term (c) $\rightarrow k_1 c N_c$

Foundation Depth term $\rightarrow k_2 \lambda_1 D_F N_q$

Dimension and Foundation Soil term (ϕ) $\rightarrow k_3 \lambda_2 B N_\gamma$

For cohesive soil (clay) : (c - soil)

$$c = \square, \phi = 0$$

في هذه الحالة الجزء الثالث = صفر

$$q_{ult} = k_1 c N_c + k_2 \lambda_1 D_F N_q + k_3 \lambda_2 B N_\gamma$$

$$q_{ult} = k_1 c N_c + k_2 \lambda_1 D_F N_q + 0$$

For cohesion less soil (sand) : (ϕ - soil)

$$c = 0, \phi = \square$$

في هذه الحالة الجزء الأول = صفر

$$q_{ult} = k_1 c N_c + k_2 \lambda_1 D_F N_q + k_3 \lambda_2 B N_\gamma$$

$$q_{ult} = 0 + k_2 \lambda_1 D_F N_q + k_3 \lambda_2 B N_\gamma$$

لو c لم يعطي يتم حسابه بالمعادلة

$$C = \frac{qu}{2}$$

Effect of Ground water table on B/c :

لأخذ تأثير المياه الجوفية في الاعتبار يضاف معاملين w_q , w_χ إلى معادلة B/C لتقليل B/C

$$q_{ult} = k_1 c N_c + k_2 \chi_1 D_F N_q w_q + k_3 \chi_2 B N_\chi w_\chi$$

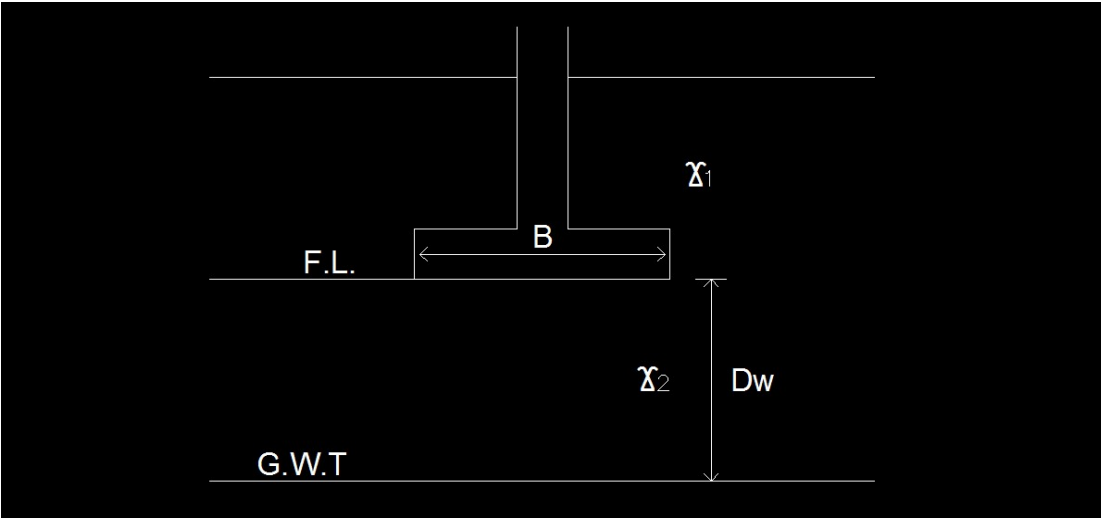
ملاحظة :

$$w_q , w_\chi \leq 1$$

هناك 4 حالات لوجود G.W.T في تربة التأسيس:

Case 1 :

1- في حالة وجود المياه علي عمق كبير من منسوب التأسيس.



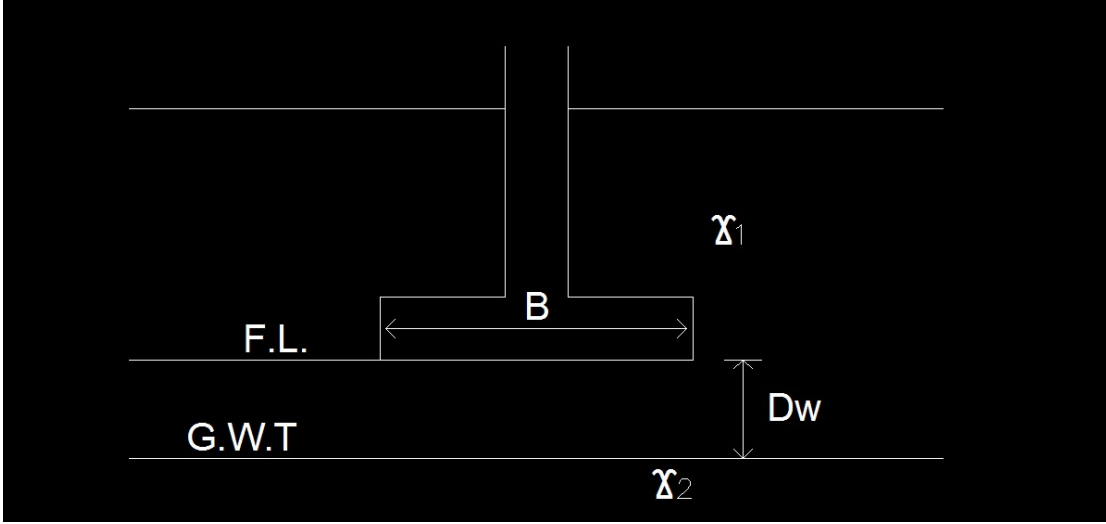
$$D_w \geq B$$

∴ المياه الجوفية لا تؤثر علي B/C

$$\therefore w_q = w_\chi = 1$$

Case 2 :

2- في حالة وجود المياه علي عمق صغير من منسوب التأسيس.



$$D_w < B$$

المياه الجوفية تؤثر علي الجزء الثالث من المعادلة ولا تؤثر علي الجزء الثاني من المعادلة.

$$\therefore w_q = 1$$

$$w_\chi = 0.5 + \frac{D_w}{B} * 0.5 \neq 1$$

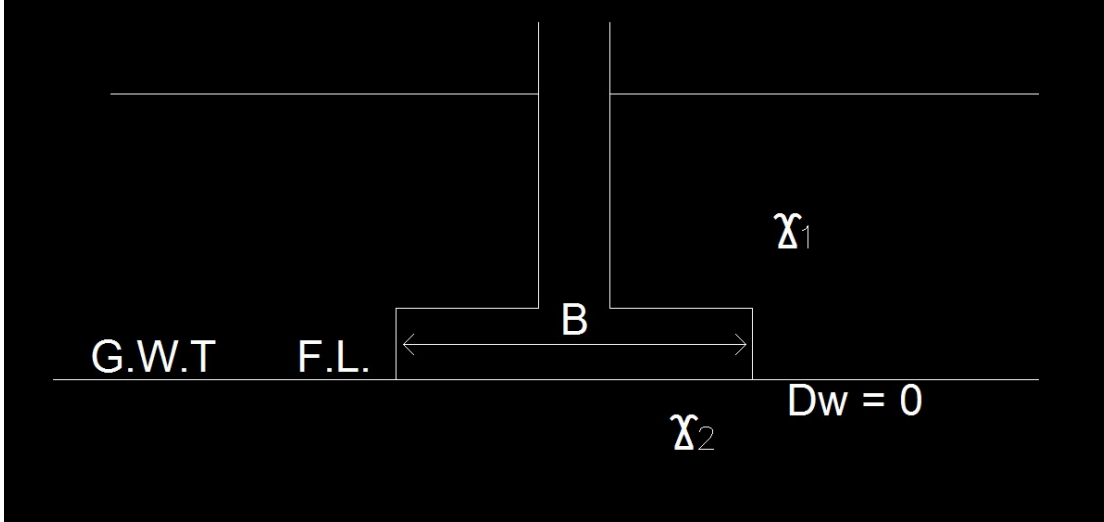
حيث أن :

D_w → عمق المياه من أسفل القاعدة

B → عرض الأساس

Case 3 :

3- في حالة وجود المياه عند منسوب التأسيس.



$$D_w = 0$$

$$\therefore w_q = 1$$

$$w_\chi = 0.5 + \frac{D_w}{B} * 0.5 = 0.5 + \frac{0}{B} * 0.5 = 0.5$$

Take χ_2 submerged

$$q_{ult} = k_1 c N_c + k_2 \chi_1 D_F N_q w_q + k_3 \chi_{2sub} B N_\chi w_\chi$$

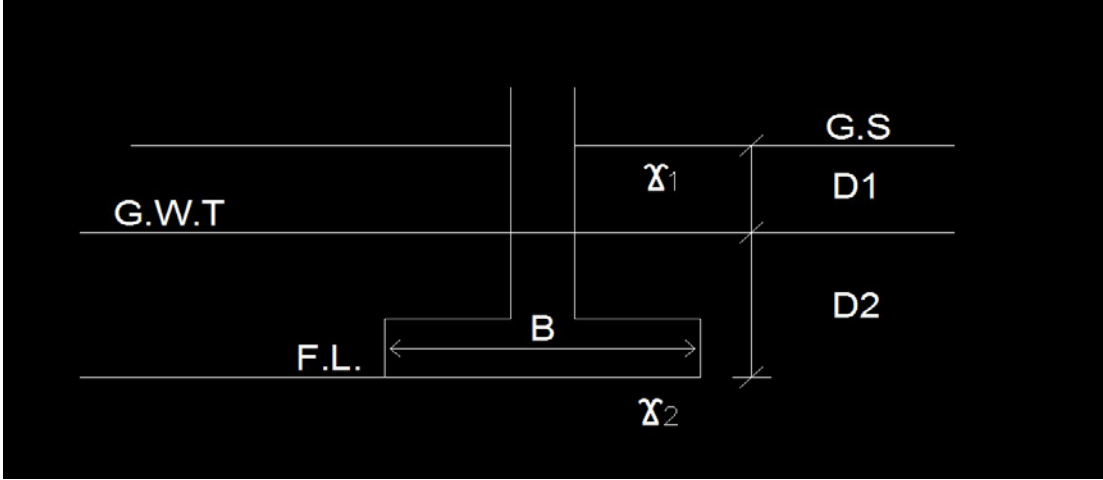
$$\chi_{sub} = \chi_{sat} - \chi_w$$

حيث أن:

$$\chi_w = 1$$

Case 4 :

4- في حالة وجود المياه بين منسوب التأسيس و سطح الأرض.



المياه الجوفية تؤثر علي الجزء الثاني والثالث من المعادلة.

$$\therefore w_{\chi} = 1$$

$$W_q = 0.5 + \frac{D1}{D2} * 0.5$$

Take χ_2 submerged

$$q_{ult} = k_1 c N_c + (\chi_{1\text{bulk or saturated}} * D_1 + \chi_{1\text{sub}} * D_2)$$

$$N_q w_q + k_3 \chi_{2\text{sub}} B N_{\chi} w_{\chi}$$

حيث أن:

D1 → المسافة من سطح الأرض حتى G.W.T

D2 → المسافة بين منسوب التأسيس و G.W.T

Example: 1

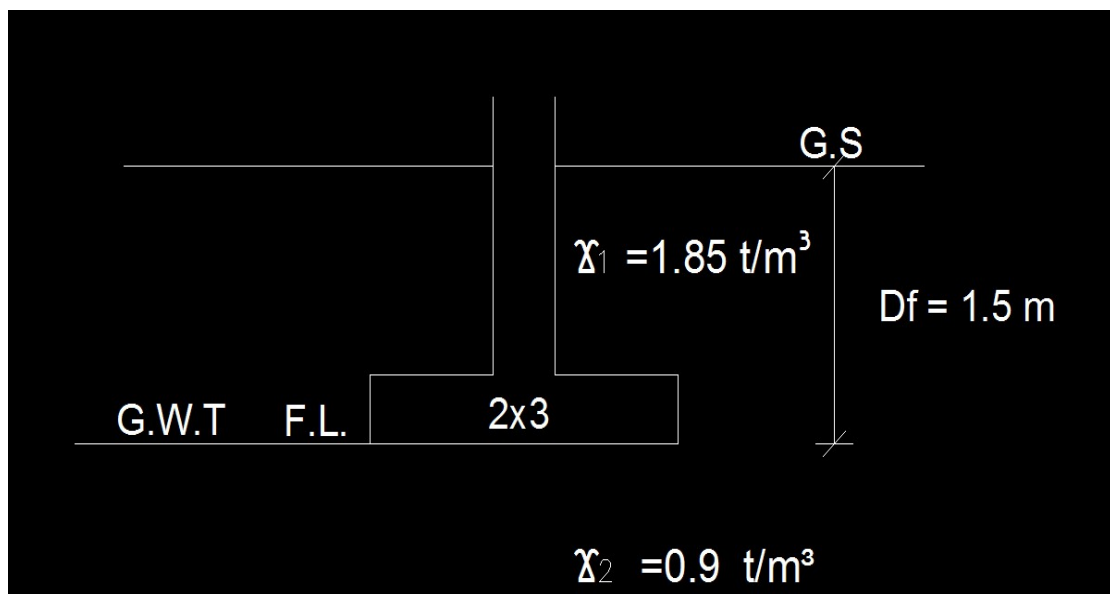
Determine the allowable load on a rectangular footing (2x3) m at depth 1.5 m below the ground surface if a fill $\gamma = 1.85 \text{ t/m}^3$ used above F.L. and the soil under footing has $\gamma_{\text{sat}} = 1.9 \text{ t/m}^3$, $c = 3 \text{ t/m}^2$, $\nu = 22^\circ$, G.W.T was find at foundation level.

Solution

rectangular footing $\rightarrow B = 2 \text{ m}$, $L = 3 \text{ m}$

$$\gamma_1 = 1.85 \text{ t/m}^3, \gamma_{\text{sub}} = \gamma_{\text{sat}} - \gamma_w = 1.9 - 1 = 0.9 \text{ t/m}^3$$

$c = 3$, $\nu = 22^\circ$, $D_f = 1.5 \text{ m}$, G.W.T was find at foundation level



For $\nu = 22^\circ$

$$N_q = e^{\pi \tan \phi} * \tan^2 (45 + \phi/2)$$

$$N_q = e^{\pi \tan 22} * \tan^2 (45 + 22/2) = 3.56 * 2.2 \\ = 7.82$$

$$N_c = (N_q - 1) \cot \phi$$

$$N_c = (7.82 - 1) \cot 22 = 6.82 * 2.4 = 16.88$$

$$N_\gamma = (N_q - 1) \tan \phi$$

$$N_\gamma = (7.82 - 1) \tan 22 = 6.82 * 0.4 = 2.76$$

For rectangular footing

$$k_1 = 1 + 0.3 \frac{B}{L} = 1 + 0.3 \frac{2}{3} = 1.2$$

$$k_2 = 1$$

$$k_3 = 1 - 0.6 \frac{B}{L} = 1 - 0.6 \frac{2}{3} = 0.6$$

∴ G.W.T was found at foundation level

∴ Case 3

$$w_q = 1$$

$$w_\gamma = 0.5 + \frac{D_w}{B} * 0.5 = 0.5 + \frac{0}{2} * 0.5 = 0.5$$

Take χ_2 submerged

$$q_{ult} = k_1 c N_c + k_2 \lambda_1 D_F N_q w_q + k_3 \lambda_{2sub} B N_\lambda w_\lambda$$

$$q_{ult} = (1.2 * 3 * 16.88) + (1 * 1.85 * 1.5 * 7.82 * 1) + (0.6 * 0.9 * 2 * 2.76 * 0.5)$$

$$= 60.77 + 21.7 + 1.49 = 83.96 \text{ t/m}^2$$

$$q_{un} = q_{ult} - \lambda_1 * D_F = 83.96 - (1.85 * 1.5) = 81.19 \text{ t/m}^2$$

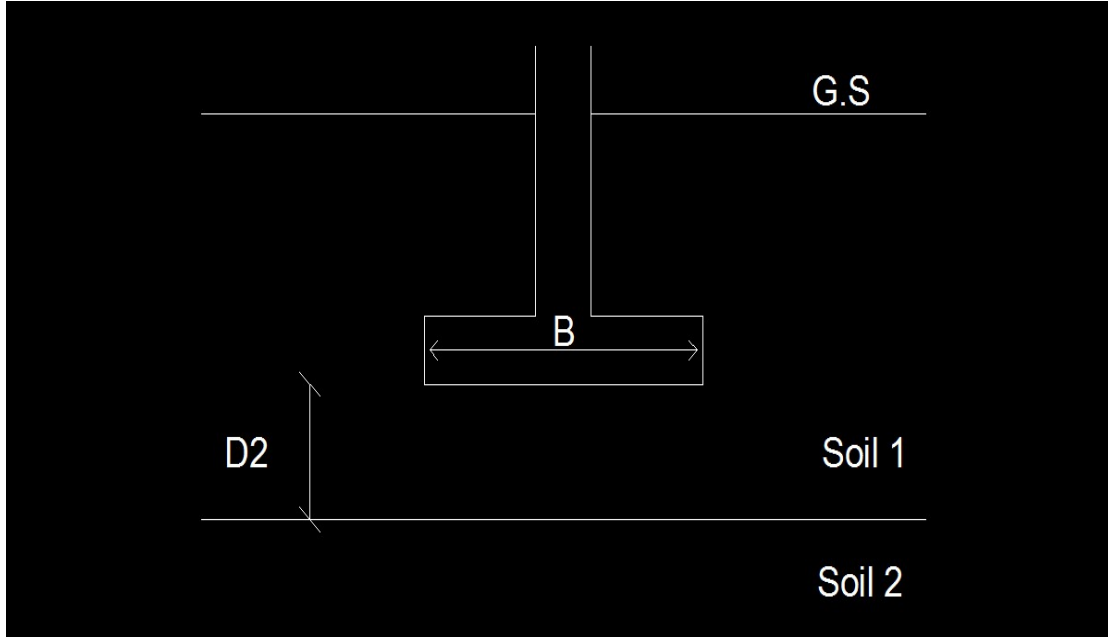
$$q_{ns} = \frac{q_{un}}{F.O.S} = \frac{81.19}{3} = 27.06 \text{ t/m}^2$$

$$q_s = q_{ns} + \lambda_1 * D_F = 27.06 + (1.85 * 1.5) = 29.84 \text{ t/m}^2$$

$$P_{all} = q_s * B * L = 29.84 * 2 * 3 = 179 \text{ ton}$$

In case of stratified soil

في حالة وجود طبقات مختلفة من التربة:



If $D_2 > 2B$

في حالة وجود الطبقة الثانية علي عمق أكبر من مرتين عرض الأساس يهمل تأثير الطبقة الثانية ونأخذ B/C للطبقة الأولى.

If $D_2 < 2B$

في حالة وجود الطبقة الثانية علي عمق أقل من مرتين عرض الأساس نوجد B/C للطبقتين الأولى والثانية ونأخذ B/C الأقل.

How to choose Foundation type:

Type of foundation:

Isolated footing

Raft footing

Deep foundation (piles)

For sand soil:

$$c = 0, \phi = \checkmark$$

$$P_{col} = \text{load of floor} / \text{No. of floors}$$

load of floor → حمل الدور الواحد

No. of floors → عدد الأدوار

$$\text{Area of footing} = \frac{p}{q_{all}}$$

If Area of footing < 70% for loaded Area

Use Isolated footing

حيث أن:

$$\text{loaded Area} = L * B$$

loaded Area → المساحة المحملة

If Area of footing \geq 70% for loaded Area

Use Raft footing

If Area of footing > 100% for loaded Area

Use Deep foundation

OR

Area of Building = $\sum p_{col}$

Area of foundation = $\frac{\sum p_{col}}{q_{all}}$

If Area of foundation < 70% for Building Area

Use Isolated footing

If Area of foundation \geq 70% for Building Area

Use Raft footing

If Area of foundation >100% for Building Area

Use Deep foundation

For clay soil:

$$c = \checkmark, \phi = 0$$

Calculate the Settlement:

$$S = C_c / 1+e * H * \text{Log} \frac{\sigma_0 + \Delta\sigma}{\sigma_0}$$

OR

$$S = m_v * H * \Delta\sigma$$

حيث أن:

$e \rightarrow$ void ratio of compressible layer (clay layer).

$H \rightarrow$ Height of compressible layer (clay layer).

$\sigma_0 \rightarrow$ effective overburden stress at Middle of clay layer.

$$\sigma_0 = \sum \gamma h$$

$$\Delta\sigma = \frac{qs * L * B}{(L+Z)(B+Z)}$$

$L, B \rightarrow$ Loaded area

$Z = H / 2 +$ height to F.L

$$C_c = 0.009(L.L\% - 10)$$

$m_v \rightarrow$ coeff of volume change

If the Settlement $0 \rightarrow 3$ Use Isolated footing

If the Settlement $3 \rightarrow 10$ Use Raft footing

ملاحظة:

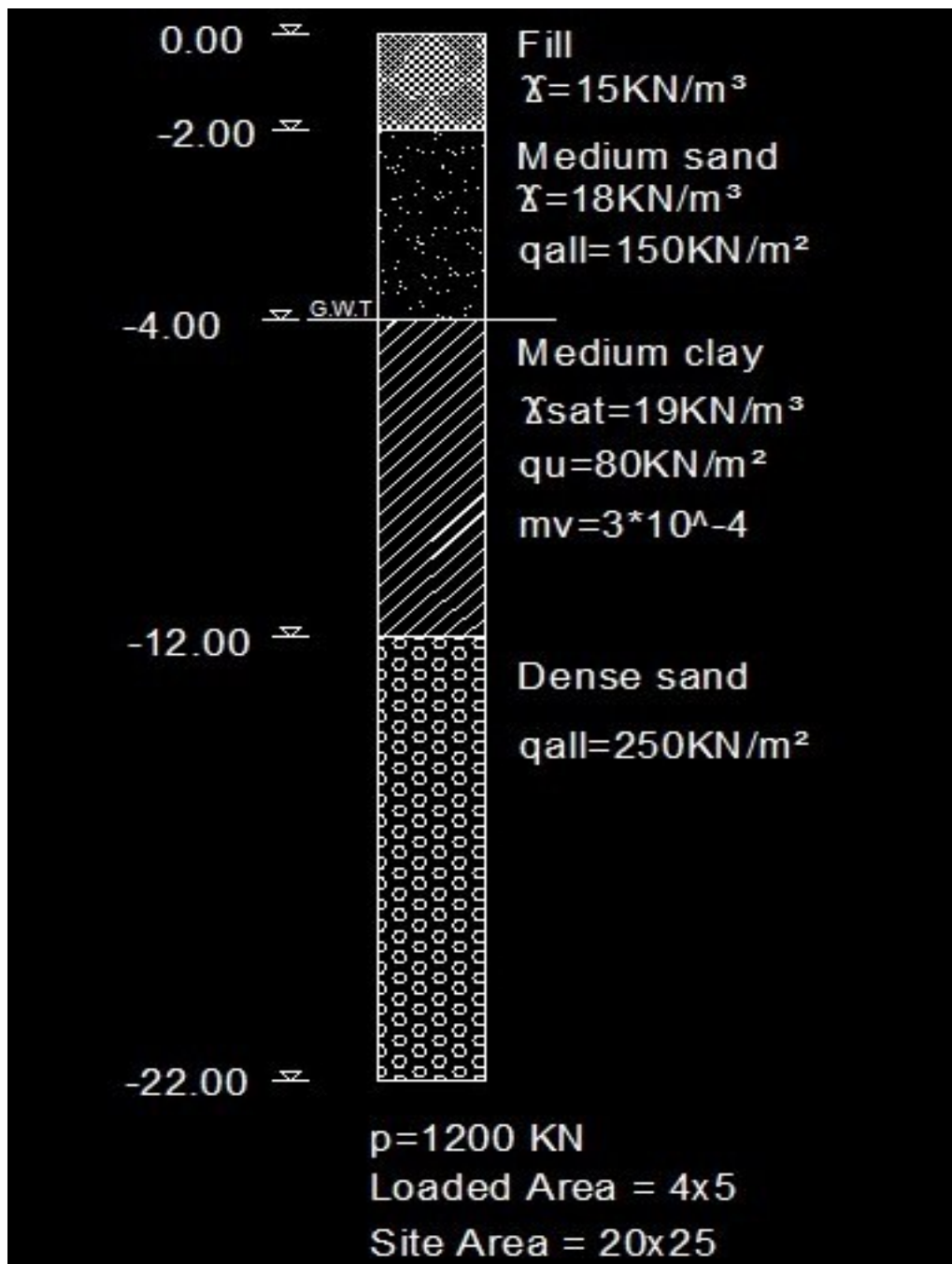
في حالة عدم الحصول علي الهبوط المسموح به نعوض في
المعادلة بالهبوط المسموح به و أوجد q_s

$$S = C_c / 1+e * H * \text{Log} \frac{\sigma_0 + \Delta\sigma}{\sigma_0}$$

$$\Delta\sigma = \frac{q_s * L * B}{(L + Z)(B + Z)}$$

Example: 2

Calculate the net safe B/C for the shown soil formation for a rectangular footing (4x5) m and choose Foundation type foundation level at -2.00 , $\nu = 0$.



Solution

rectangular footing $\rightarrow B = 4 \text{ m}$, $L = 5 \text{ m}$

For $\nu = 0$

$$N_q = 5 , N_c = 1 , N_\gamma = 0$$

For rectangular footing

$$k_1 = 1 + 0.3 \frac{B}{L} = 1 + 0.3 \frac{4}{5} = 1.24$$

$$k_2 = 1$$

$$k_3 = 1 - 0.6 \frac{B}{L} = 1 - 0.6 \frac{4}{5} = 0.52$$

$$w_q = 1 , w_\gamma = 0.5$$

$$D < 2B$$

$$2 < 2 * 4$$

$$2 < 8$$

\therefore Calculate q_{all} for Medium clay

$$C = \frac{qu}{2} = \frac{80}{2} = 40 \text{ KN/m}^2$$

$$q_{ult} = k_1 c N_c + k_2 (\gamma_1 D_F + \gamma_2 D_F) N_q w_q$$

$$\begin{aligned} q_{ult} &= (1.24 * 40 * 5) + (1 * (15 * 2) + (18 * 2) * 1 * 1) \\ &= 248 + 66 = 314 \text{ KN/m}^2 \end{aligned}$$

$$q_{un} = q_{ult} - (\gamma_1 D_F + \gamma_2 D_F)$$

$$= 314 - ((15 * 2) + (18 * 2)) = 248 \text{ KN/m}^2$$

$$q_{ns} = \frac{q_{un}}{\text{F.O.S}} = \frac{248}{3} = 82.67 \text{ KN/m}^2$$

$$q_{all 2} = q_s = q_{ns} + (\gamma_1 D_F + \gamma_2 D_F)$$

$$= 82.67 + ((15 * 2) + (18 * 2)) = 148.67 \text{ KN/m}^2$$

$$q_{all 2} < q_{all 1}$$

$$148.67 < 150$$

$$\therefore \text{take } q_{all} = q_{all 2} = 148.67 \text{ KN/m}^2 = 149 \text{ KN/m}^2$$

$$\text{Area of footing} = \frac{p}{q_{all}} = \frac{1200}{149} = 8 \text{ m}^2$$

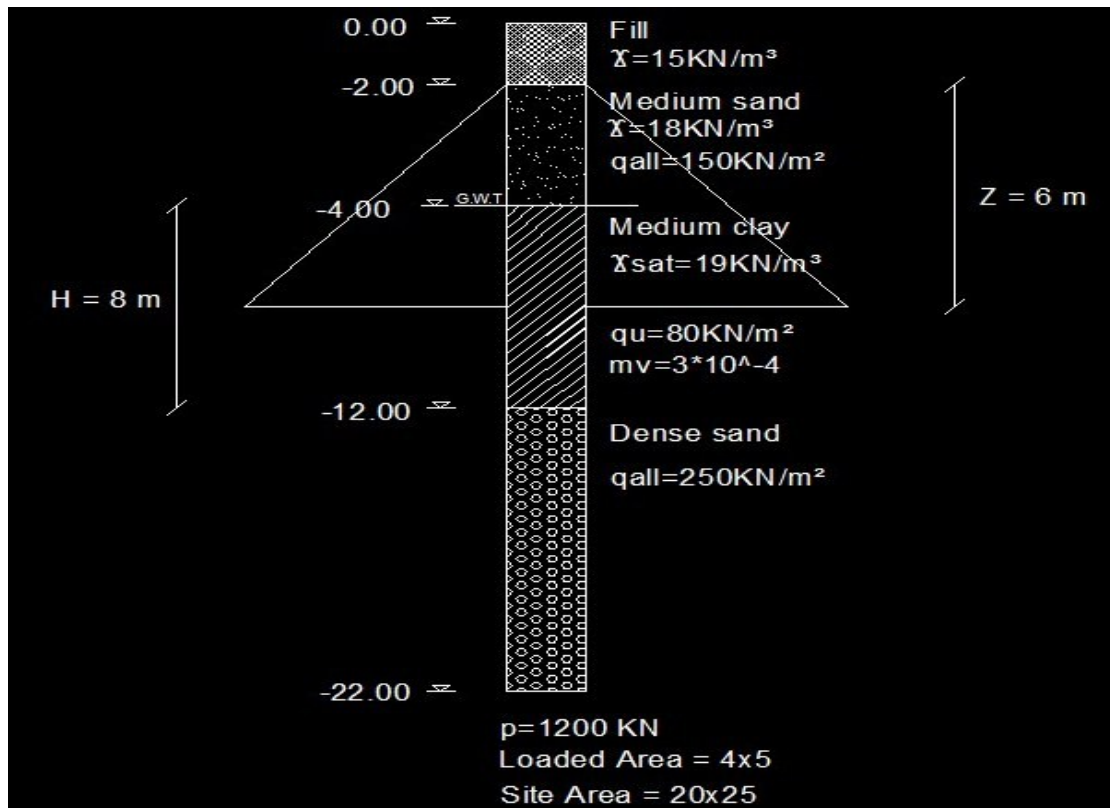
If Area of footing < 70% for loaded Area

$$8 < 70/100 * 4 * 5$$

$$8 \text{ m}^2 < 14 \text{ m}^2$$

\therefore Use Isolated footing

Check Settlement for clay layer



$$S = m_v * H * \Delta\sigma$$

$$\Delta\sigma = \frac{q_s * L * B}{(L + Z)(B + Z)}$$

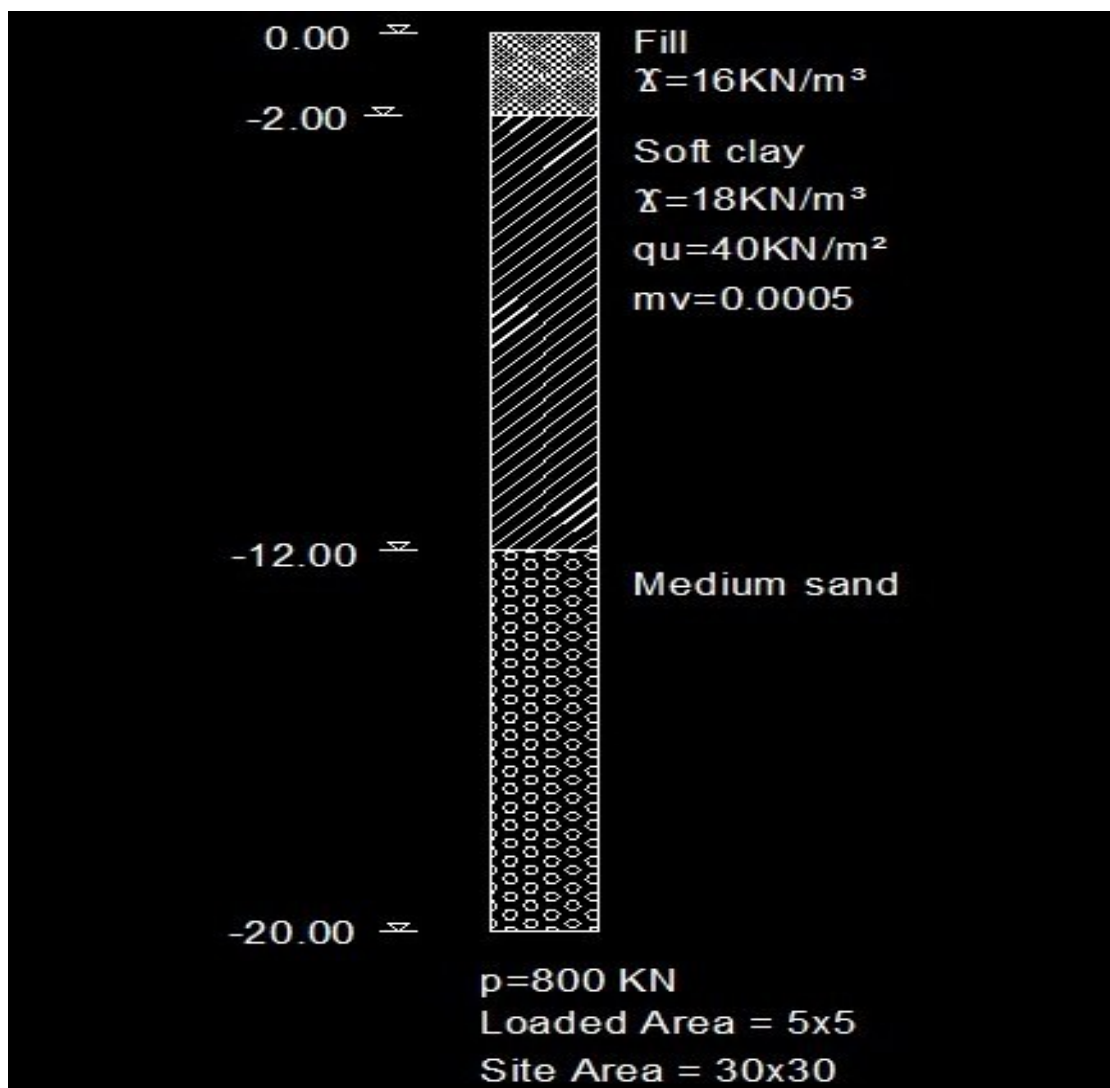
$$\Delta\sigma = \frac{149 * 5 * 4}{(5 + 6) * (4 + 6)} = 27.1 \text{ KN/m}^2$$

$$S = 3 * 10^{-4} * 27.1 * 8 = 0.065 \text{ m} = 6.5 \text{ cm}$$

the Settlement is = 6.5 Use Raft footing

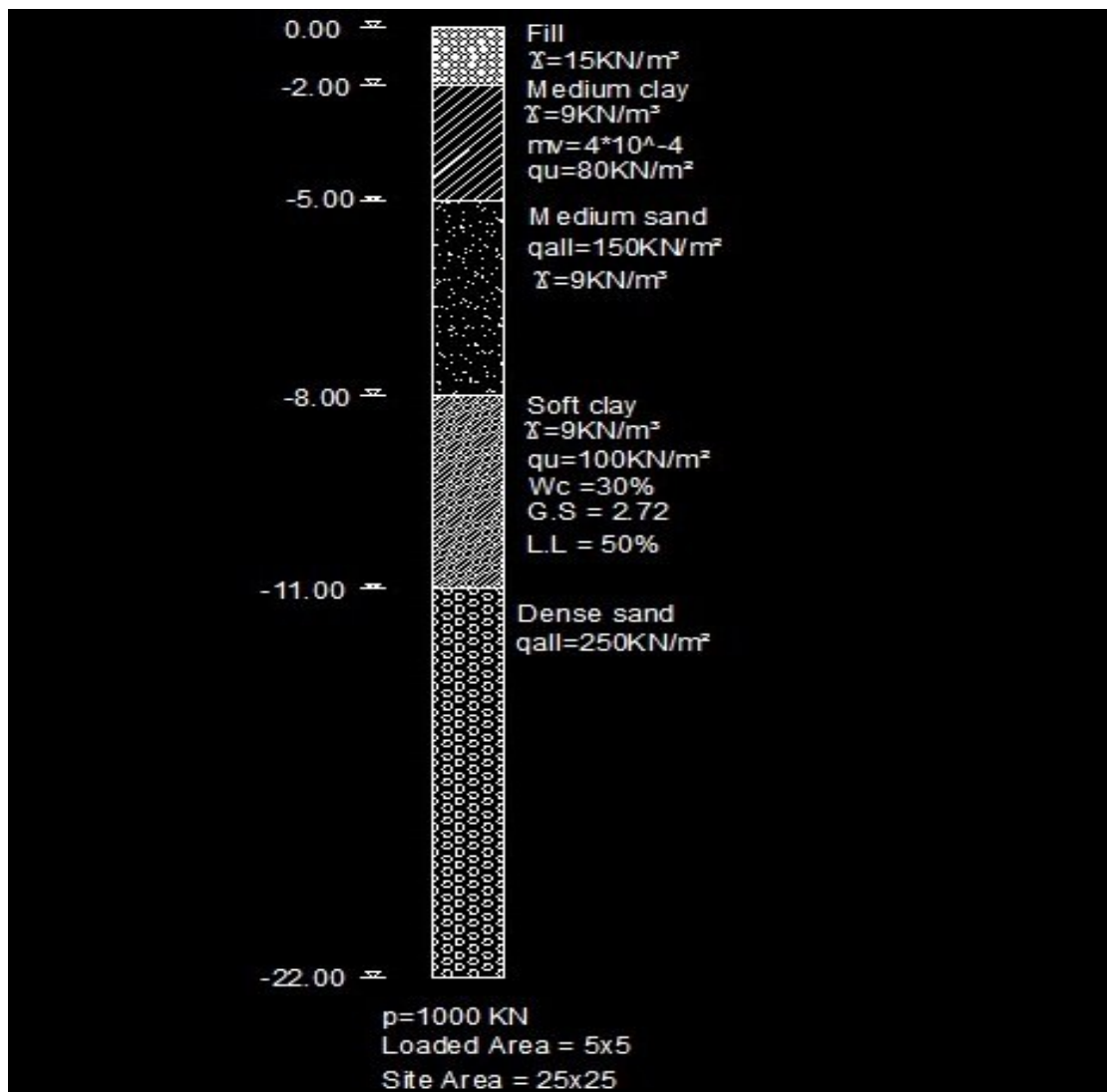
Example: 3

Calculate the net safe B/C for the shown soil formation for a rectangular footing (5x5) m and choose Foundation type , foundation level at -2.00 and G.W.T was find at Ground surface , $\nu = 0$.



Example: 4

Calculate the net safe B/C for the shown soil formation for a rectangular footing (5x5) m and choose Foundation type , foundation level at -2.00 and G.W.T was find at Ground surface , $\nu = 0$.



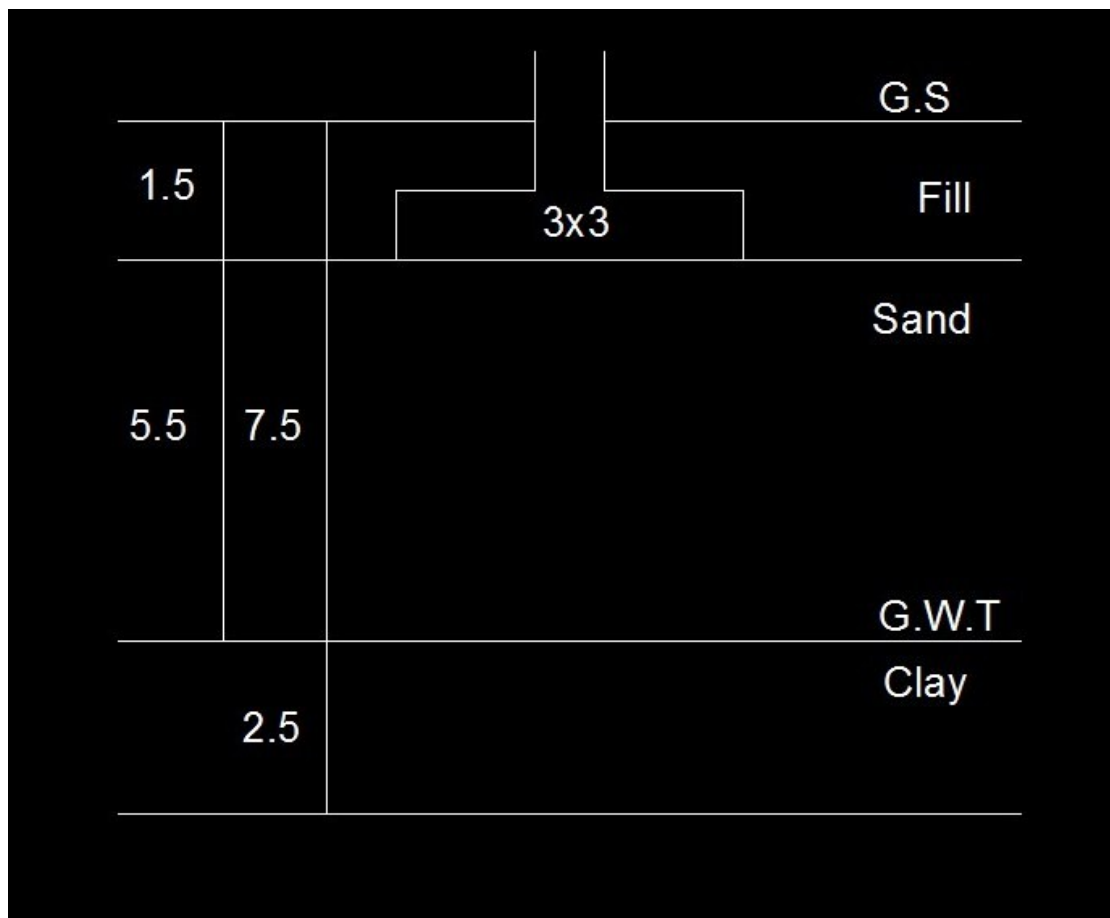
Example: 5

Fill : $\gamma = 1.45 \text{ t / m}^3$

Sand : $\gamma = 1.81 \text{ t / m}^3$, $v = 30\%$, F.O.S = 3

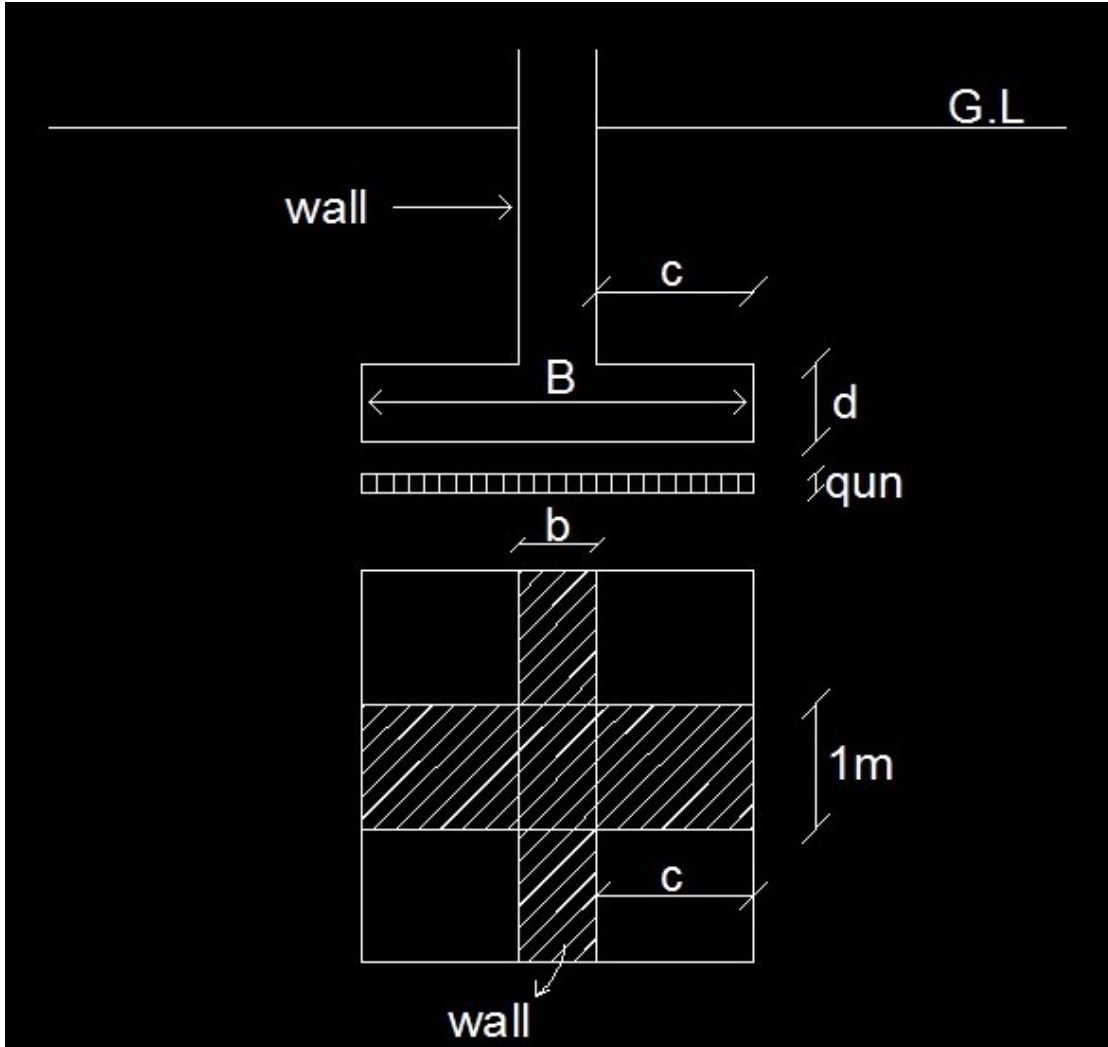
Clay : $\gamma_{\text{sat}} = 2.1 \text{ t / m}^3$, $m_v = 0.038 \text{ cm}^2 / \text{kg}$

The allowable Settlement = 2.5 cm



Strip Footing:

القاعدة الشريطية:



الأبعاد ب working load

السمك و الحديد ب Ultimate load

للتحويل من ال working to Ultimate * 1.5

Procedure of Design:

Plain Concrete:

الخرسانة العادية:

If $t_{p.c} > 20$ cm	If $t_{p.c} \leq 20$ cm
Consider p.c in design	Neglect فرشہ نظافة فقط in design
$P_t = P_w * 1.1$	$P_t = P_w * 1.1$
$A_{p.c} = P_t / q_{all=1} * B_{p.c}$	$A_{R.c} = P_t / q_{all=1} * B_{R.c}$
$B_{R.c} = B_{p.c} - 2t_{p.c}$ to the nearest 5cm	$B_{R.c} =$ to the nearest 5cm

$t_{p.c}$ is assumed 10 → 40 cm

فرشہ نظافة و لا تؤخذ في حسابات التصميم

$t_{p.c} = 10 \rightarrow 20$ cm

تعتبر قاعدة عادية و تؤخذ في حسابات التصميم

$t_{p.c} = 20 \rightarrow 40$ cm

Minimum dimensions of R.C. Footing:

$$B_{R.c.} = 80 \text{ cm}$$

$$t_{R.c.} = 40 \text{ cm}$$

$$d_{R.c.} = 33 \text{ cm}$$

If $t_{p.c}$ not given take $t_{p.c} = 20$ cm

$$q_{ult} = 1.5 * p_w / B_{R.c} * 1$$

$$M_{ult} = q_{ult} * c^2 / 2$$

$$C = B_{R.c} - b_w / 2$$

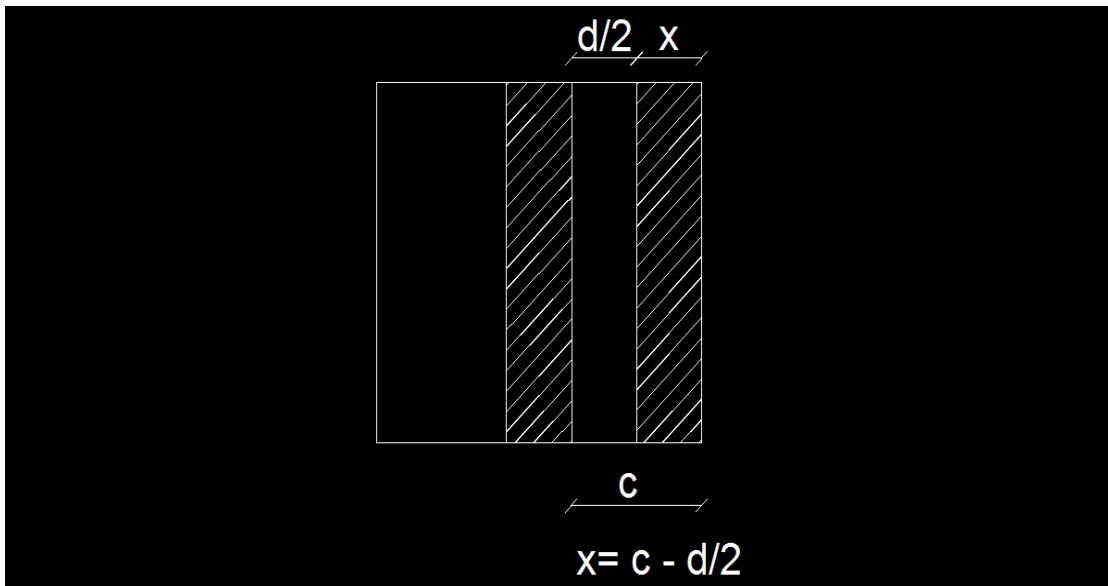
$$d = c_1 \sqrt{\frac{M_{ult}}{F_{cu} * B}} \cong \text{to the nearest 5cm}$$

If F_{cu} not given take $F_{cu} = 250$ kg / cm²

$$C_1 = 5 , B = 100 \text{ cm}$$

p.c	Plain concrete	الخرسانة العادية
R.c	Reinforced concrete	الخرسانة المسلحة
P_w	wall load	حمل الحائط
$t_{p.c}$	Thickness of Plain concrete	سمك الخرسانة العادية
$A_{p.c}$	Area of Plain concrete	مساحة الخرسانة العادية
$A_{R.c}$	Area of Reinforced concrete	مساحة الخرسانة المسلحة
$B_{p.c}$	Plain concrete thickness	عرض الخرسانة العادية
$B_{R.c}$	Reinforced concrete thickness	عرض الخرسانة المسلحة
b_w	Wall thickness	عرض الحائط
q_{sh}	Actual shear stress	اجهادات ال shear
q_{cu}	Allowable shear stress	مقاومة الخرسانة لل shear
La	Available length	طول السيخ
ν	Diameter of bars	قطر السيخ

Check shear:



القطاع الحرج علي مسافة $d/2$ من وش الحائط.

Critical section

$$Q_{sh} = q_{ult} (c - d/2)$$

$$q_{sh} = Q_{sh} / B * d$$

$$q_{cu} = 0.4 \sqrt{f_{cu}}$$

if $q_{sh} < q_{cu}$ ok safe

if $q_{sh} > q_{cu}$ not safe increase depth

$$d = Q_{sh} / q_{cu} * b$$

$t = d + \text{cover} \cong$ to the nearest 5cm

cover = (5 to 10 cm)

Reinforcement of the footing:

Min 5 y 12 / m

Max 10 y ?? / m

$$A_s = M_{ult} / J * d * f_y \text{ -----(1)}$$

$$A_{s \text{ min}} = 5 \text{ y } 12 / \text{ m } \text{ -----(2)}$$

$$A_{s \text{ min}} = (0.15 / 100) * B * d \text{ -----(3)}$$

نأخذ القيمة الأكبر في القيم 1,2,3

If $A_s \geq A_{s \text{ min}} \rightarrow \text{ok}$

If $A_s < A_{s \text{ min}} \rightarrow \text{take } A_s = A_{s \text{ min}}$

Check Bond:

$$L_d = \alpha * \beta * \mu * (f_y / \chi_s) * (v / 4 q_{ub})$$

حيث أن:

$\alpha = 1 \rightarrow \text{plan bars}$ سيخ أملس

$\alpha = 0.75 \rightarrow \text{H.G.S}$ سيخ مشرشر

$\beta = 1$

$\mu = 1$

$\chi_s = 1.15$

$$F_y = 3600 \text{ kg / cm}^2$$

$$q_{ub} = 0.87 \sqrt{\frac{F_{cu}}{\chi_c}}$$

$$\chi_c = 1.5$$

$$L_d \leq L_a$$

Example: 1

Given : $f_{cu} = 200 \text{ kg/cm}^2$, $P_w = 180 \text{ kN / m}^2$,

$b_w = 0.5 \text{ m}$, $f_y = 3600 \text{ kg/cm}^2$, $t_{p,c} = 20 \text{ cm}$, B/C ($q_{all} = 100 \text{ kN / m}^2$)

Req : Design of strip footing that carry the given line load.

Solution

$$100 \text{ kN / m}^2 = 10 \text{ t / m}^2 = 1 \text{ kg / cm}^2$$

$$\therefore t_{p,c} \leq 20 \text{ cm}$$

\therefore Neglect in design

$$\begin{aligned} A_{R.c} &= 1.1 * P_w / q_{all} = 1.1 * 180 / 100 = 1.98 \text{ m}^2 \\ &= 1 * B_{R.c} = 1 * 1.98 = 1.98 \cong 2 \text{ m}^2 \end{aligned}$$

End of working load

$$q_{ult} = 1.5 * p_w / B_{R.c} * 1 = (1.5 * 18) / (2 * 1) = 13.5 \text{ t / m}^2$$

$$C = B_{R.c} - b_w / 2 = (2 - 0.5) / 2 = 0.75 \text{ m}$$

$$M_{ult} = q_{ult} * c^2 / 2 = (13.5 * (0.75)^2) / 2 = 3.8 \text{ t.m}$$

$$d = c_1 \sqrt{\frac{M_{ult}}{F_{cu} * B}} = 5 \sqrt{\frac{3.8 * 10^5}{200 * 100}} = 21.8 \text{ cm} \cong 25 \text{ cm}$$

$$t = d + \text{cover} = 25 + 10 = 35 \text{ cm}$$

Check shear:

$$Q_{sh} = q_{ult} (c - d/2) = 13.5 * (0.75 - (0.25/2)) = 8.4 \text{ ton}$$

$$q_{sh} = Q_{sh} / B * d = \frac{8.4 * 10^3}{100 * 25} = 3.3 \text{ kg / cm}^2$$

$$q_{cu} = 0.4 \sqrt{f_{cu}} = 0.4 \sqrt{200} = 5.66 \text{ kg / cm}^2$$

$q_{sh} < q_{cu}$ ok safe

$3.3 < 5.66$ safe

Reinforcement:

$$A_{s1} = M_{ult} / J * d * f_y = \frac{3.8 * 10^5}{0.826 * 25 * 3600} = 5.11 \text{ cm}^2 / \text{m}'$$

$$A_{s \text{ min}2} = 5 \text{ y } 12 / \text{m} = 5.65 \text{ cm}^2 / \text{m}'$$

$$A_{s \text{ min}3} = \frac{0.15}{100} * B * d = \frac{0.15}{100} * 100 * 25 = 3.75 \text{ cm}^2 / \text{m}'$$

take $A_s = 5.65 \text{ cm}^2 / \text{m}'$

use 5 y 12 /m

Check Bond:

$$L_d = \alpha * \beta * \mu * (f_y / \gamma_s) * (v / 4 q_{ub})$$

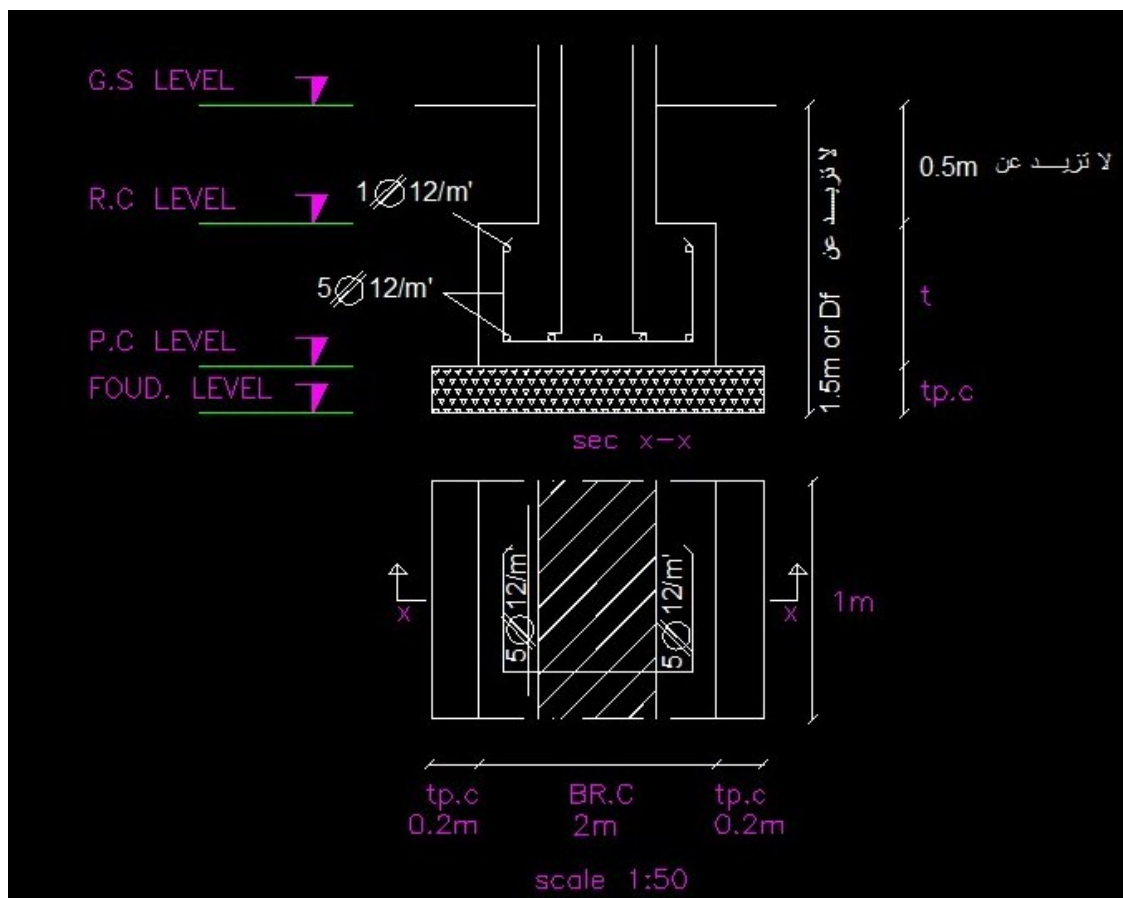
$$q_{ub} = 0.87 \sqrt{\frac{F_{cu}}{\gamma_c}} = 0.87 \sqrt{\frac{200}{1.5}} = 10 \text{ kg/cm}^2$$

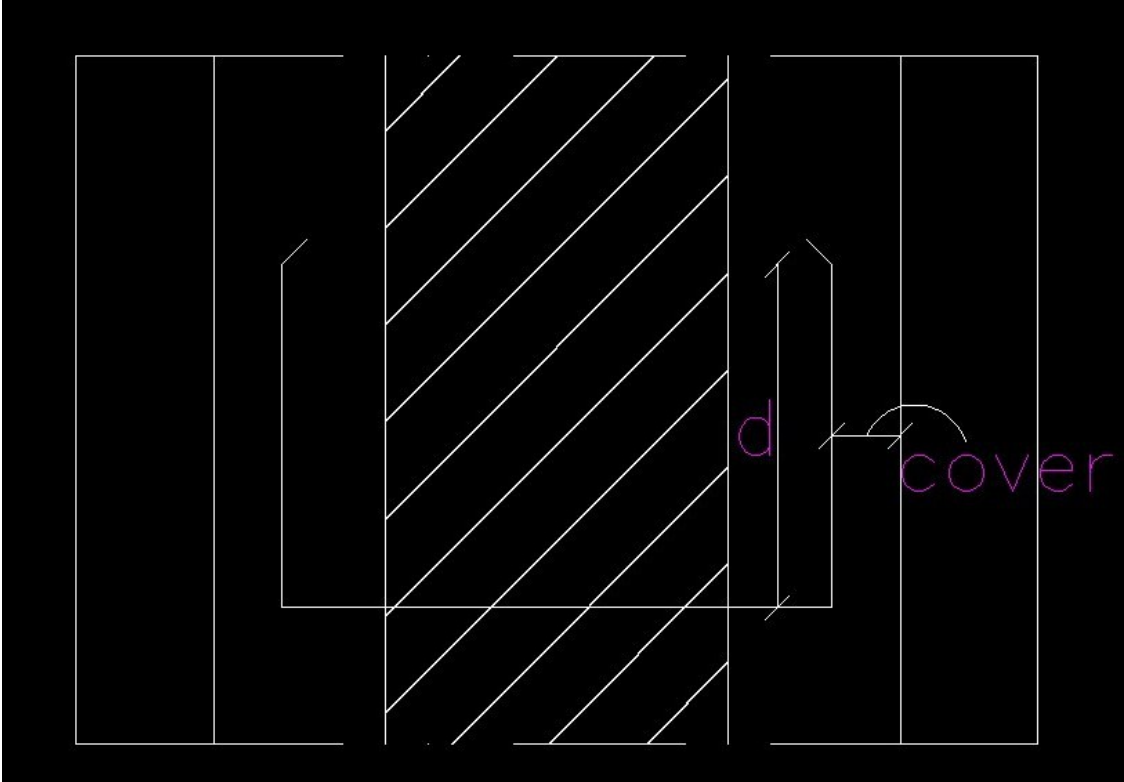
$$L_d = 0.75 * 1 * 1 * (3600 / 1.15) * (1.2 / (4 * 10))$$

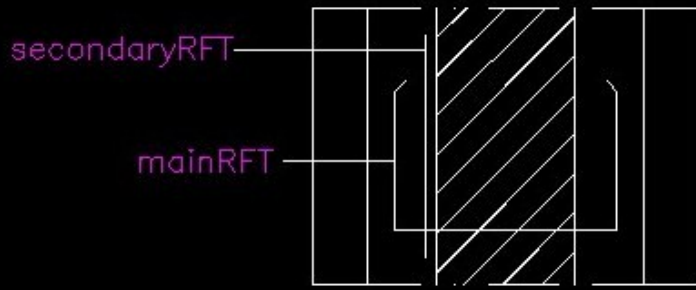
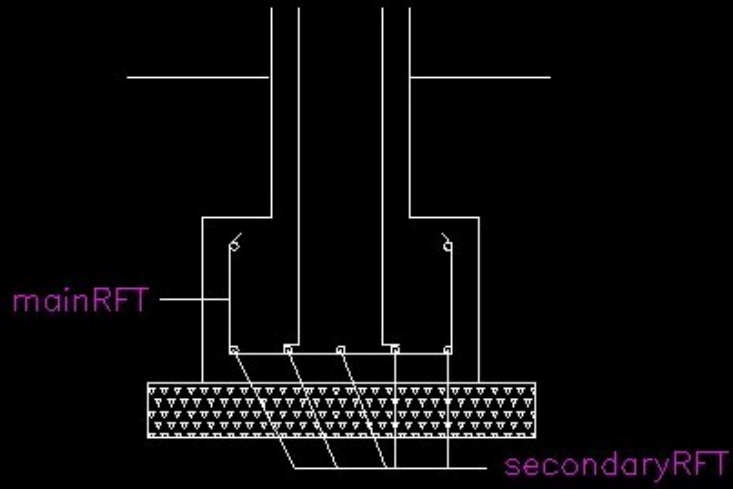
$$= 70.4 \text{ cm} \rightarrow 0.704 \text{ m}$$

$$L_d \leq L_a$$

$$0.704 \leq 2 \text{ ok}$$







Isolated footing:

Squared Isolated footing .

تستخدم في حالة:

- 1- عمود مربع.
- 2- عمود دائري.
- 3- يمكن مع الأعمدة المستطيلة لكنة غير مفضل.

Hunched Squared Isolated footing .

Rectangular Isolated footing .

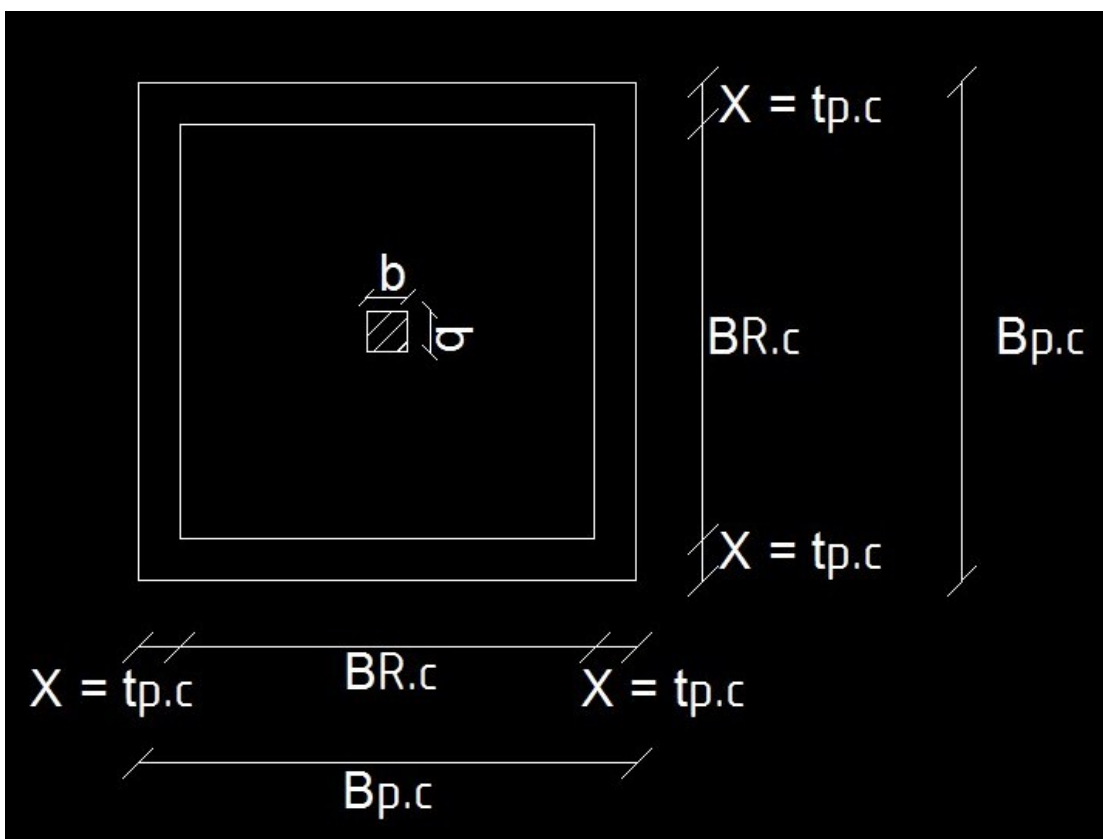
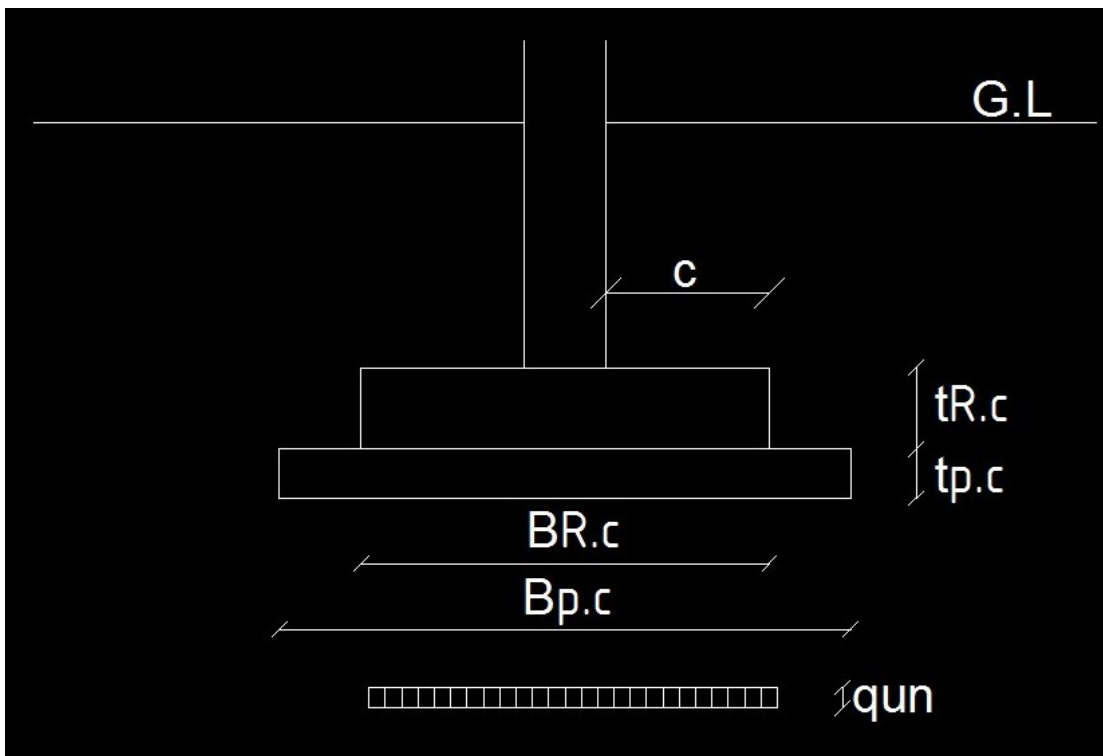
تستخدم في حالة:

- 1- الأعمدة المستطيلة.
- 2- يمكن مع الأعمدة المربعة لكنة غير مفضل.

Circular Isolated footing .

تستخدم فقط مع الأعمدة الدائرية.

Design Isolated Squared footing:



Procedure of Design:

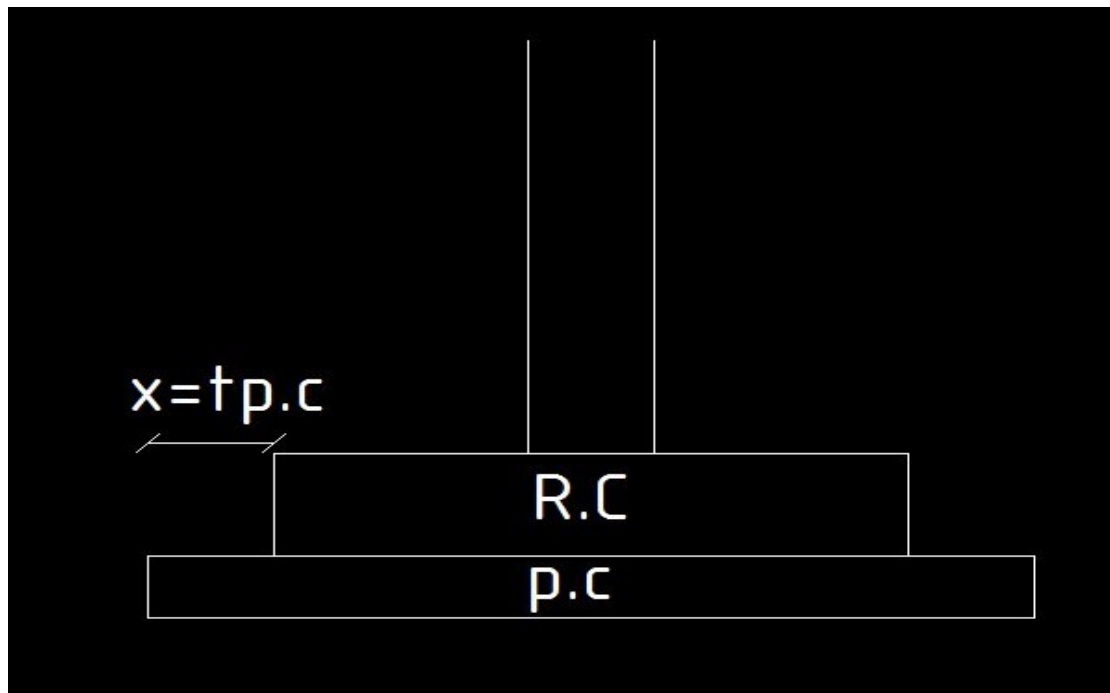
Plain concrete:

If $t_{p.c} > 20$ cm	If $t_{p.c} \leq 20$ cm
Consider p.c in design	Neglect فرشہ نظافة فقط in design
$P_t = P_w * 1.1$	$P_t = P_w * 1.1$
$A_{p.c} = P_t / q_{all} = B_{p.c}^2$	$A_{R.c} = P_t / q_{all} = B_{R.c}^2$
$B_{p.c} = \sqrt{A_{p.c}}$	$B_{R.c} = \sqrt{A_{R.c}}$
$B_{R.c} = B_{p.c} - 2t_{p.c}$ \cong to the nearest 5cm	$B_{p.c} = B_{R.c} + 2t_{p.c}$ \cong to the nearest 5cm

في حالة العمود المربع:

Check stresses on plain concrete:

عند أخذ القاعدة العادية في الحسابات:



$$q_{ult} = 1.5 * p_w / B_{p.c}^2$$

$$M_{ult} = (q_{ult} * (X^2)) / 2$$

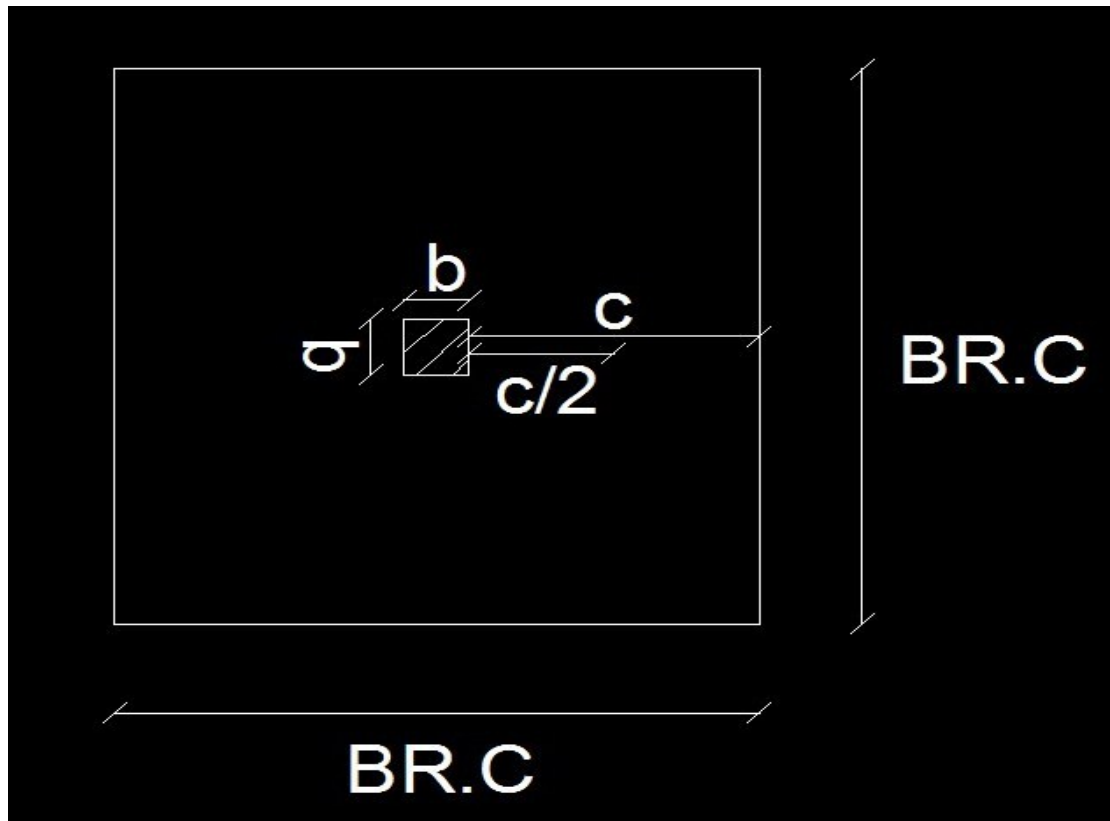
$$F_t = 6 * M_{ult} / 100 * (t_{p.c})^2$$

$$F_{tcu} = (0.75 * (f_{cu})^{2/3}) / 1.5$$

If $F_t < F_{tcu}$ ok safe

If $F_t > F_{tcu}$ not safe (X) نقل بروز الخرسانة العادية

$$q_{ult} = 1.5 * p_w / B_{R.c}^2$$



$$M_{ult} = q_{ult} * (B_{R.c} * c) * (c / 2)$$

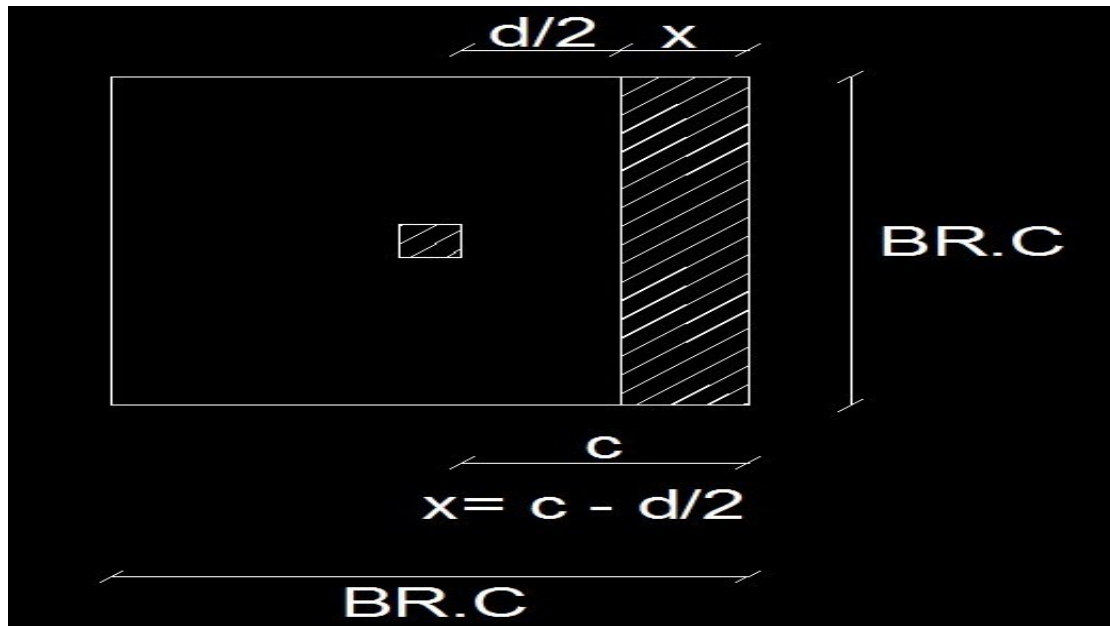
$$C = (B_{R.c} - b / 2)$$

$$d = c_1 \sqrt{\frac{M_{ult}}{F_{cu} * BR.c}} \cong \text{to the nearest 5cm}$$

$$t = d + \text{cover} \cong \text{to the nearest 5cm}$$

$$\text{cover} = (5 \text{ to } 10 \text{ cm})$$

Check shear:



القطاع الحرج علي مسافة $d/2$ من وش العمود.

Critical section

$$Q_{sh} = q_{ult} (B_{R.c} * (c - d/2))$$

$$q_{sh} = Q_{sh} / (B_{R.c} * d)$$

$$q_{cu} = 0.4 \sqrt{f_{cu}}$$

if $q_{sh} < q_{cu}$ ok safe

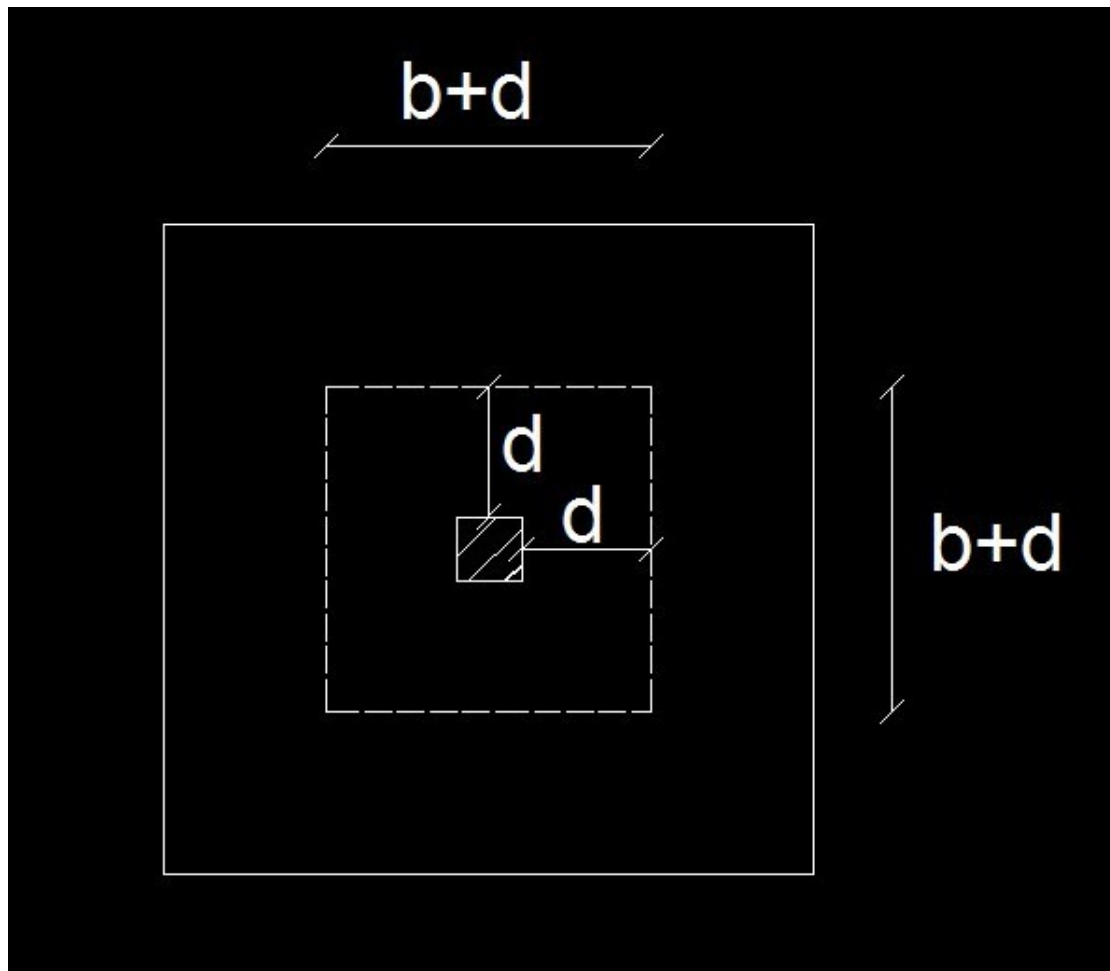
if $q_{sh} > q_{cu}$ not safe increase depth

$$d = Q_{sh} / (q_{cu} * B_{R.c})$$

$$t = d + \text{cover}$$

$$\text{cover} = (5 \text{ to } 10 \text{ cm})$$

Check punching:



$$Q_p = p_u - q_{ult} (b+d)^2$$

$$q_p = Q_p / (4(b+d)d)$$

$$q_{pcu} = \sqrt{\frac{f_{cu}}{\lambda c}}$$

If $q_{pcu} > q_p$ ok safe

If $q_{pcu} < q_p$ un safe \rightarrow increase depth

Reinforcement of the footing:

Min 5 y 12 / m

Max 10 y ?? / m

$$A_s = M_{ult} / J * d * f_y / B_{R.C} \text{ -----(1)}$$

$$A_{s \min} = 5 \text{ y } 12 / \text{m} \text{ -----(2)}$$

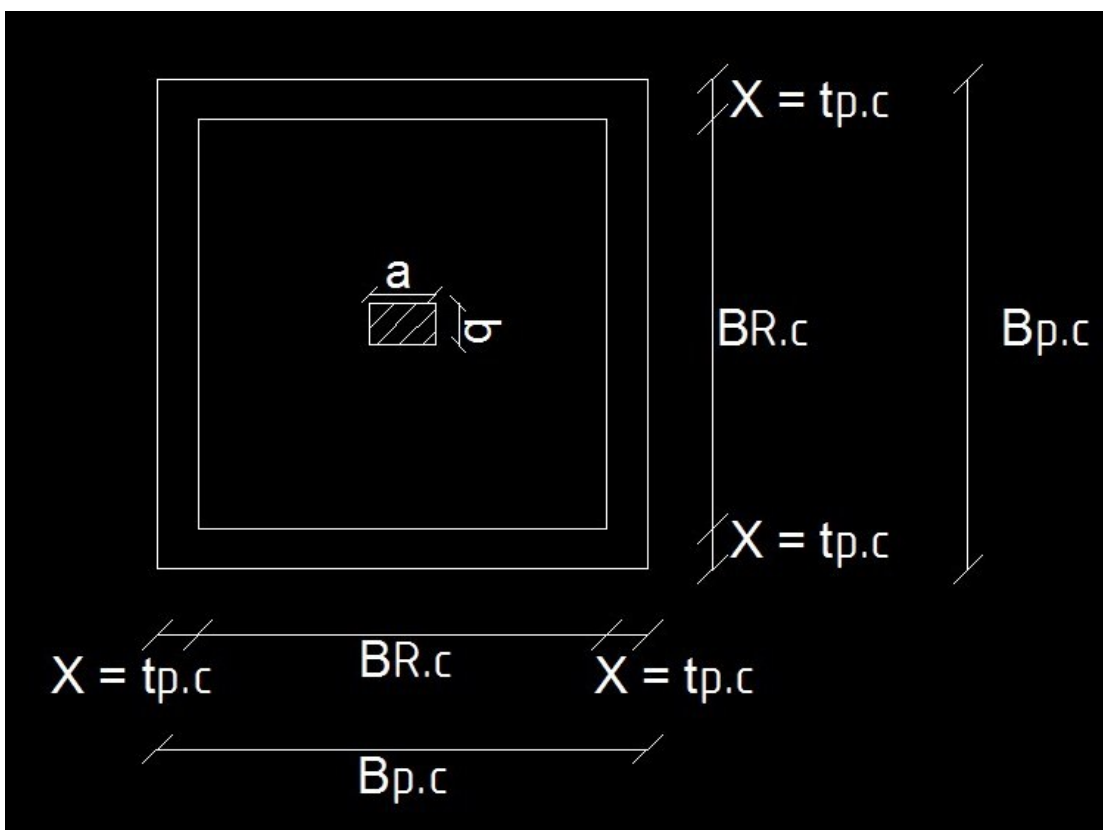
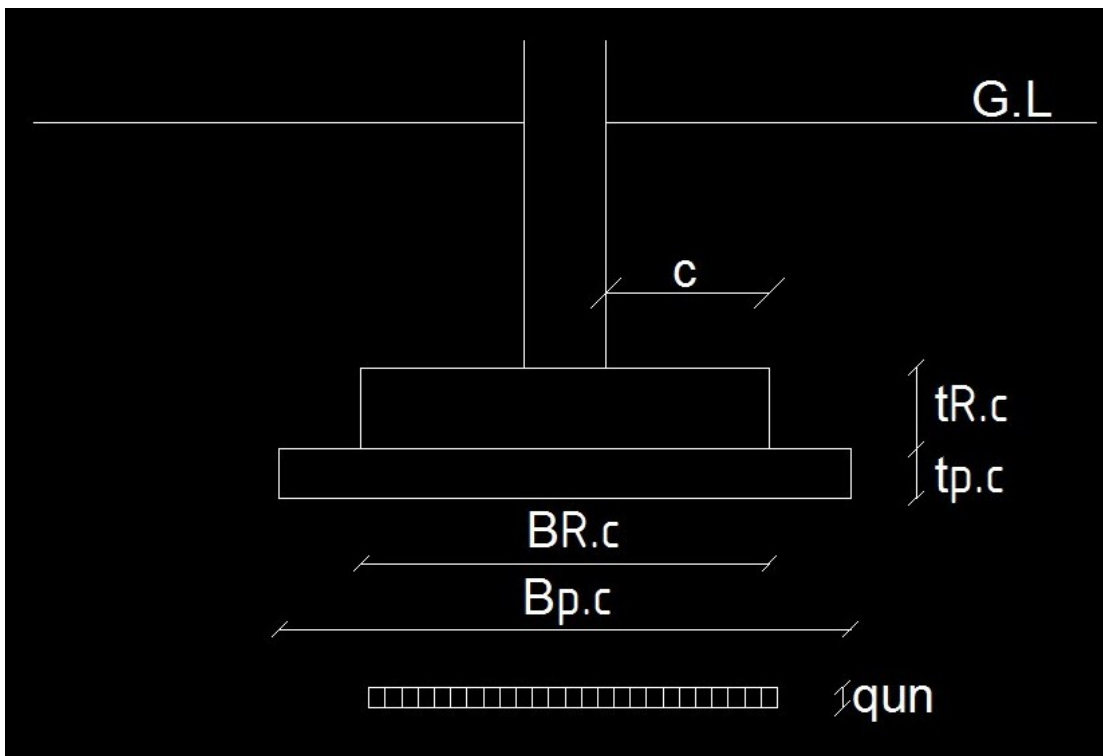
$$A_{s \min} = (0.15 / 100) * B * d \text{ -----(3)}$$

نأخذ القيمة الأكبر في القيم 1,2,3

If $A_s \geq A_{s \min} \rightarrow \text{ok}$

If $A_s < A_{s \min} \rightarrow \text{take } A_s = A_{s \min}$

Design Isolated Squared footing:



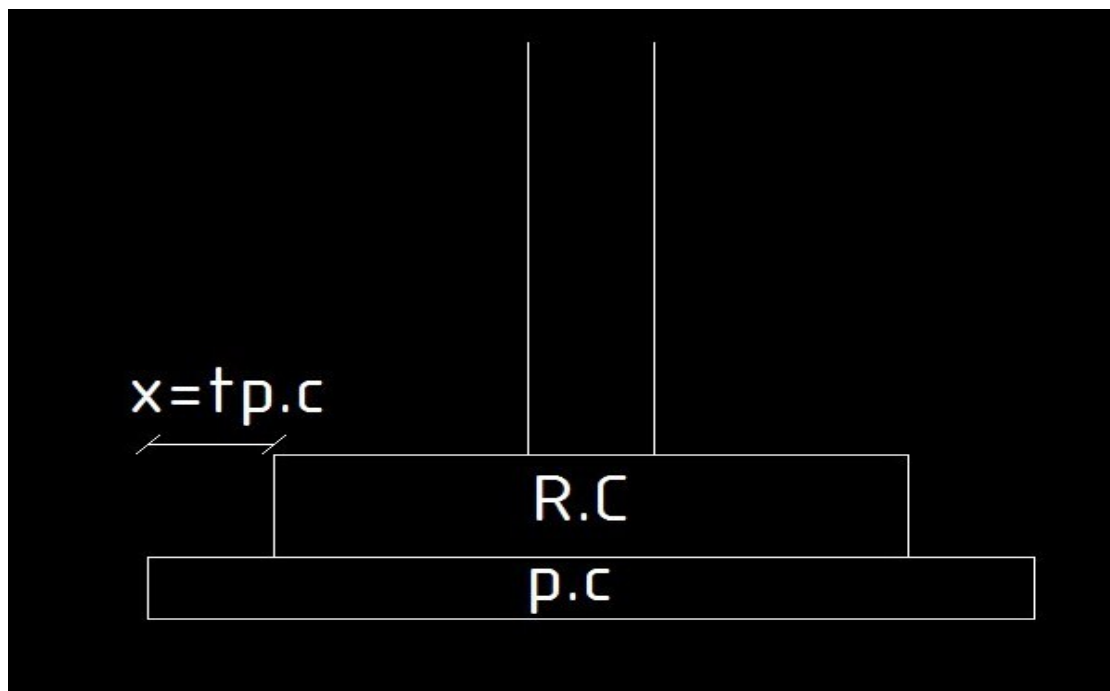
Procedure of Design:

If $t_{p.c} > 20$ cm	If $t_{p.c} \leq 20$ cm
Consider p.c in design	Neglect فرشہ نظافة فقط in design
$P_t = P_w * 1.1$	$P_t = P_w * 1.1$
$A_{p.c} = P_t / q_{all} = B_{p.c}^2$	$A_{R.c} = P_t / q_{all} = B_{R.c}^2$
$B_{p.c} = \sqrt{A_{p.c}}$	$B_{R.c} = \sqrt{A_{R.c}}$
$B_{R.c} = B_{p.c} - 2t_{p.c}$ to the nearest 5cm	$B_{p.c} = B_{R.c} + 2t_{p.c}$ to the nearest 5cm

في حالة العمود المستطيل:

Check stresses on plain concrete:

عند أخذ القاعدة العادية في الحسابات:



$$q_{ult} = 1.5 * p_w / B_{p.c}^2$$

$$M_{ult} = (q_{ult} * (X^2)) / 2$$

$$F_t = 6 * M_{ult} / 100 * (t_{p.c})^2$$

$$F_{tcu} = (0.75 * (f_{cu})^{2/3}) / 1.5$$

If $F_t < F_{tcu}$ ok safe

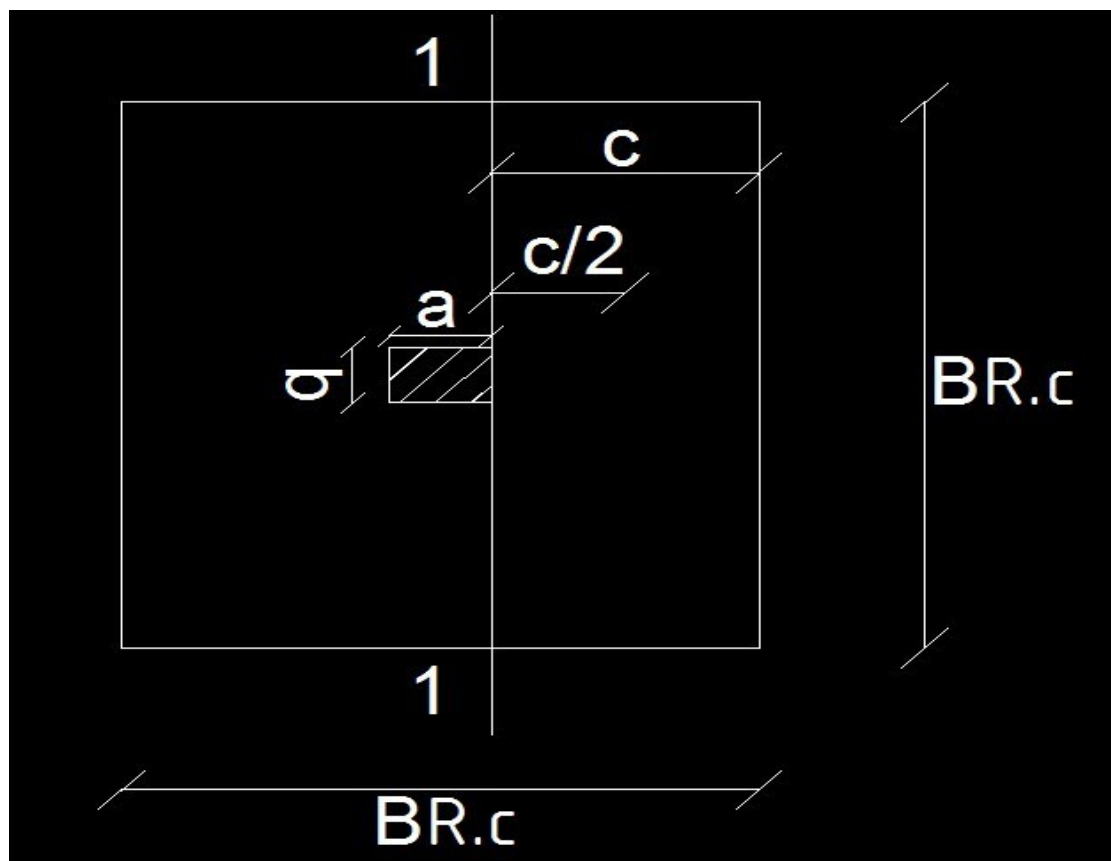
If $F_t > F_{tcu}$ not safe (X) نقل بروز الخرسانة العادية

$$q_{ult} = 1.5 * p_w / B_{R.c}^2$$

نأخذ القطاعات الحرجة للعزوم علي وش العمود من الجهتين

Critical section of bending at R.C Footing .

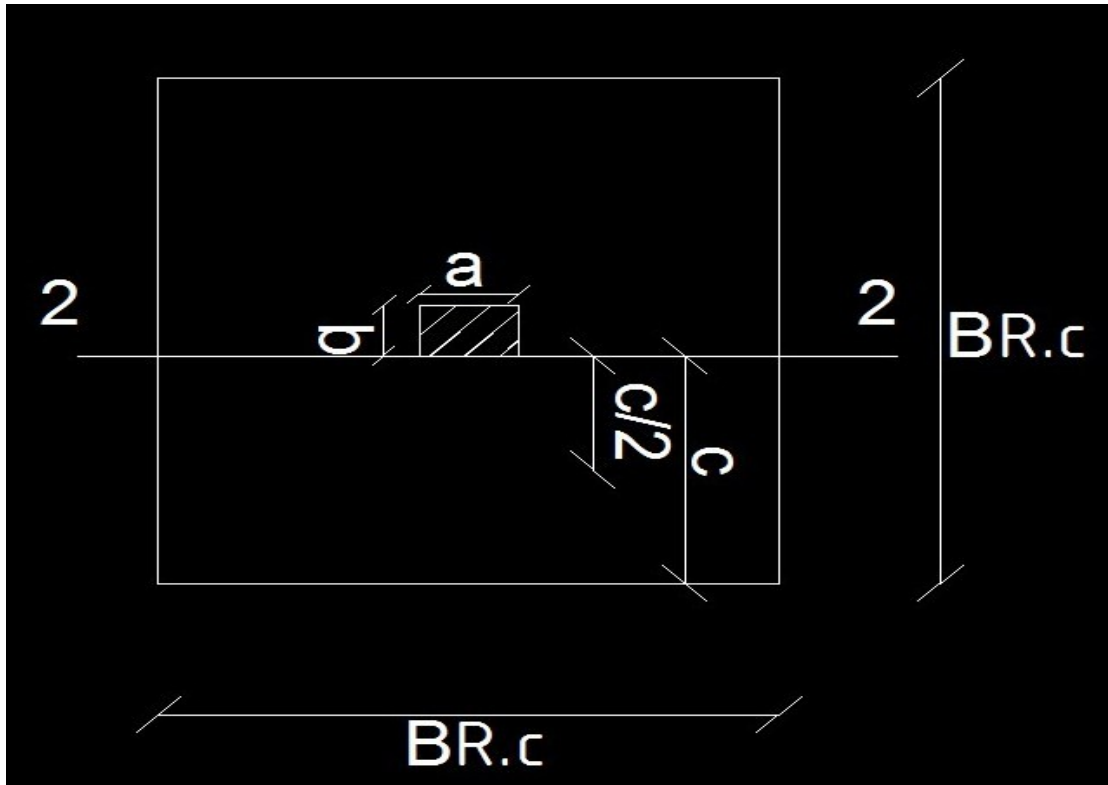
Direction 1:



$$C_1 = (B_{R.c} - a / 2)$$

$$M_{ult 1} = q_{ult} * (B_{R.c} * c_1) * (c_1 / 2)$$

Direction 2:



$$C_2 = (B_{R.c} - b / 2)$$

$$M_{ult 2} = q_{ult} * (B_{R.c} * c_2) * (c_2 / 2)$$

يتم التصميم علي العزم الكبر من $M_{ult 1}$, $M_{ult 2}$

$$d = c_1 \sqrt{\frac{M_{ult}}{F_{cu} * B_{R.c}}} \cong \text{to the nearest 5cm}$$

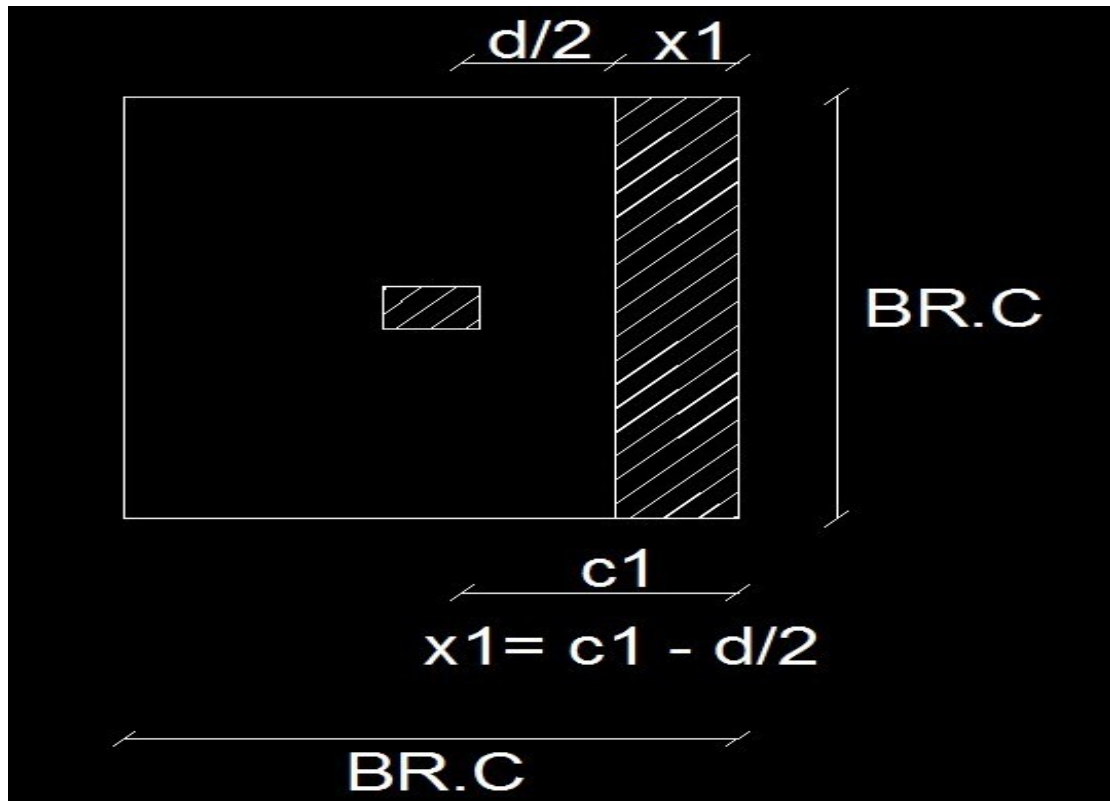
$$t = d + \text{cover} \cong \text{to the nearest 5cm}$$

$$\text{cover} = (5 \text{ to } 10 \text{ cm})$$

Check shear:

القطاع الحرج علي مسافة $d/2$ من وش العمود.

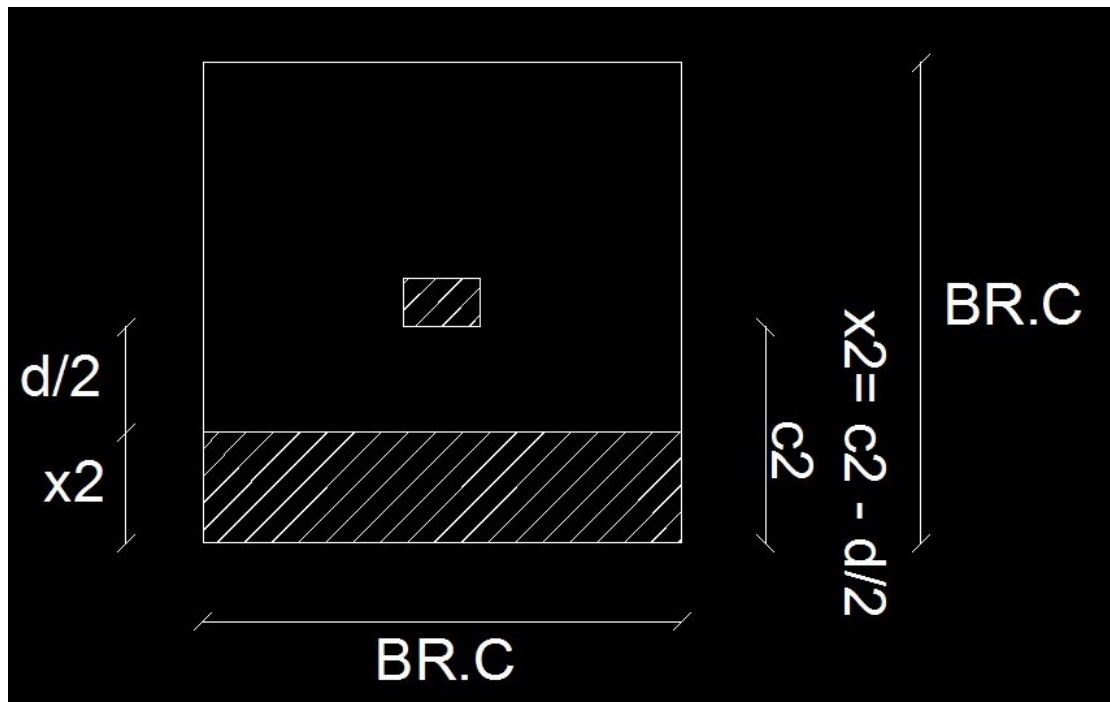
Critical section



$$Q_{sh1} = q_{ult} (B_{R.C} * (c_1 - d/2))$$

$$q_{sh1} = Q_{sh1} / (B_{R.C} * d)$$

$$q_{cu} = 0.4 \sqrt{f_{cu}}$$



$$Q_{sh2} = q_{ult} (B_{R.C} * (c_2 - d/2))$$

$$q_{sh2} = Q_{sh2} / (B_{R.C} * d)$$

$$q_{cu} = 0.4 \sqrt{f_{cu}}$$

Take the bigger of Q_{sh1} , Q_{sh2} and q_{sh1} , q_{sh2}

if $q_{sh} < q_{cu}$ ok safe

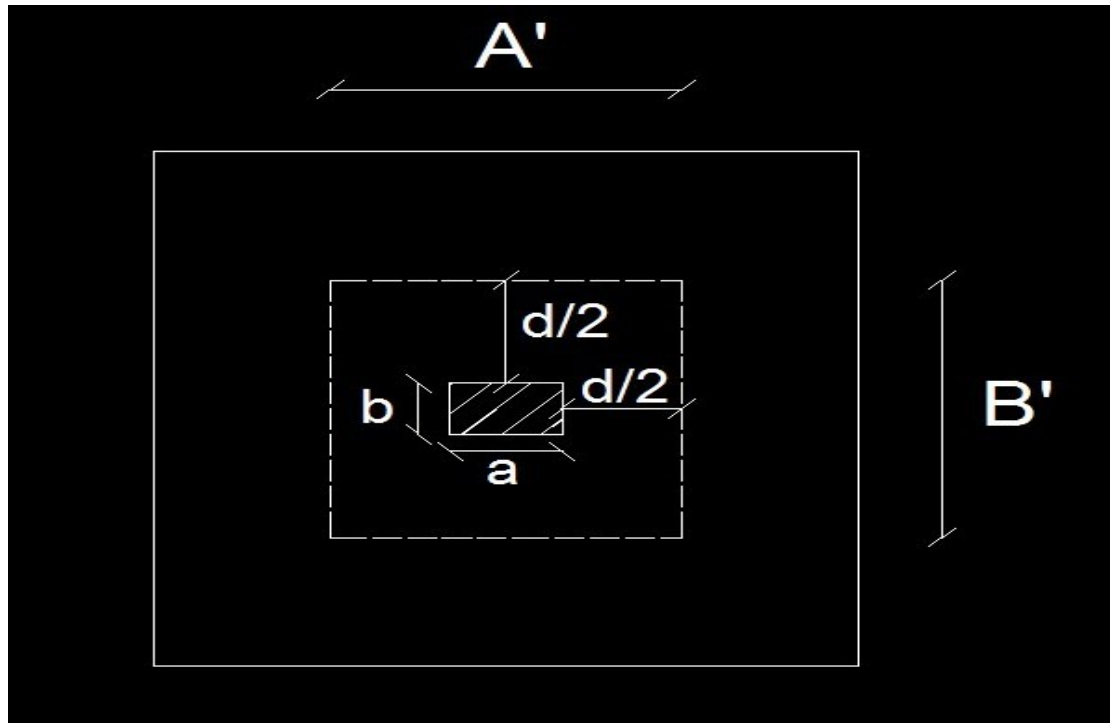
if $q_{sh} > q_{cu}$ not safe increase depth

$$d = Q_{sh} / (q_{cu} * B_{R.C})$$

$$t = d + \text{cover}$$

$$\text{cover} = (5 \text{ to } 10 \text{ cm})$$

Check punching:



$$Q_p = p_u - q_{ult} (A' + B')$$

$$A' = a + d, B' = b + d$$

$a \rightarrow$ طول العمود , $b \rightarrow$ عرض العمود

$$q_p = Q_p / (2(A' + B')d)$$

$$q_{pcu} = \left(0.5 + \frac{b}{a}\right) \sqrt{\frac{f_{cu}}{\gamma_c}}$$

If $q_{pcu} > q_p$ ok safe

If $q_{pcu} < q_p$ un safe \rightarrow increase depth

Reinforcement of the footing:

Min 5 y 12 / m

Max 10 y ?? / m

$$A_s = M_{ult} / J * d * f_y / B_{R.C} \text{ -----(1)}$$

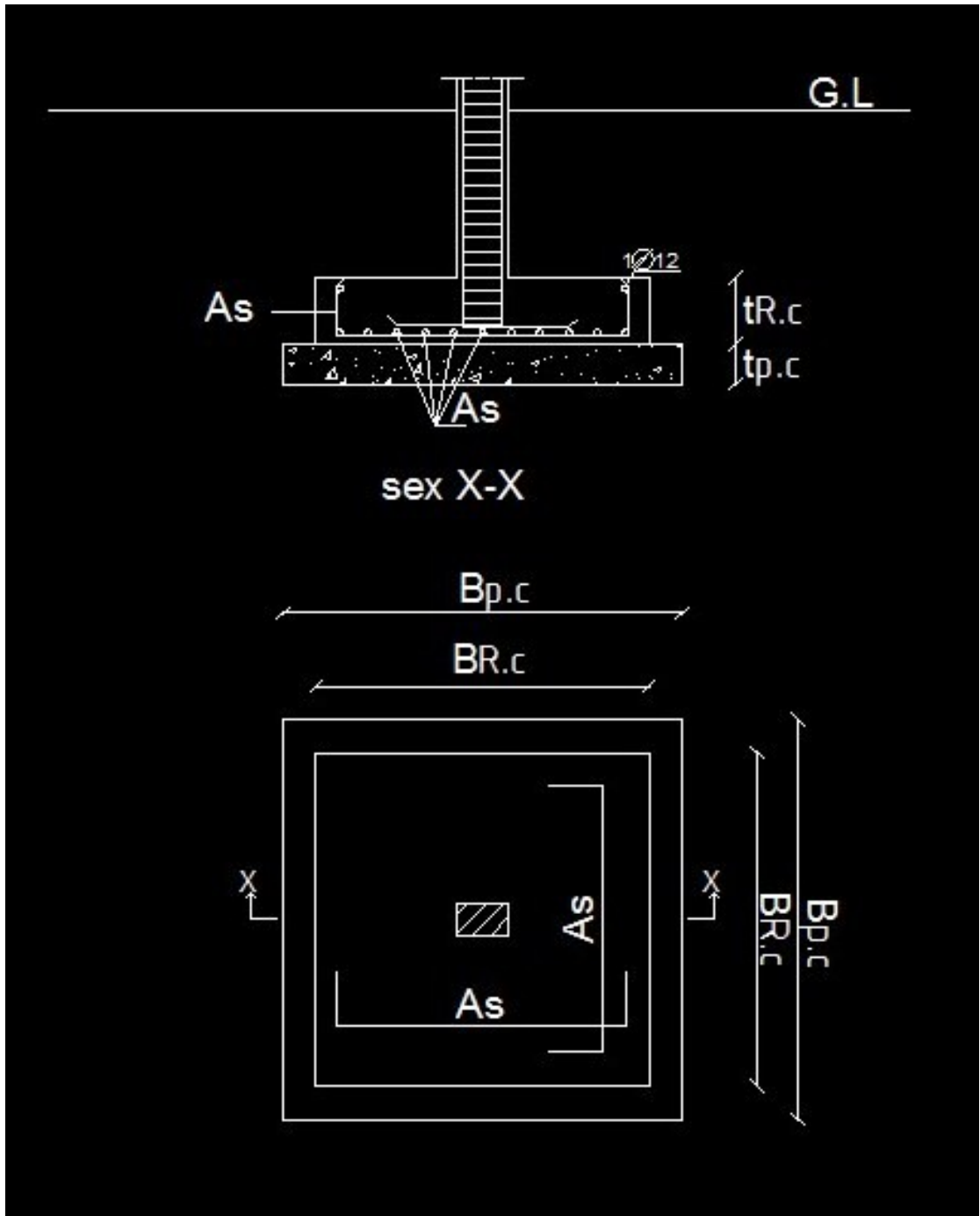
$$A_{s \min} = 5 \text{ y } 12 / \text{m} \text{ -----(2)}$$

$$A_{s \min} = (0.15 / 100) * B * d \text{ -----(3)}$$

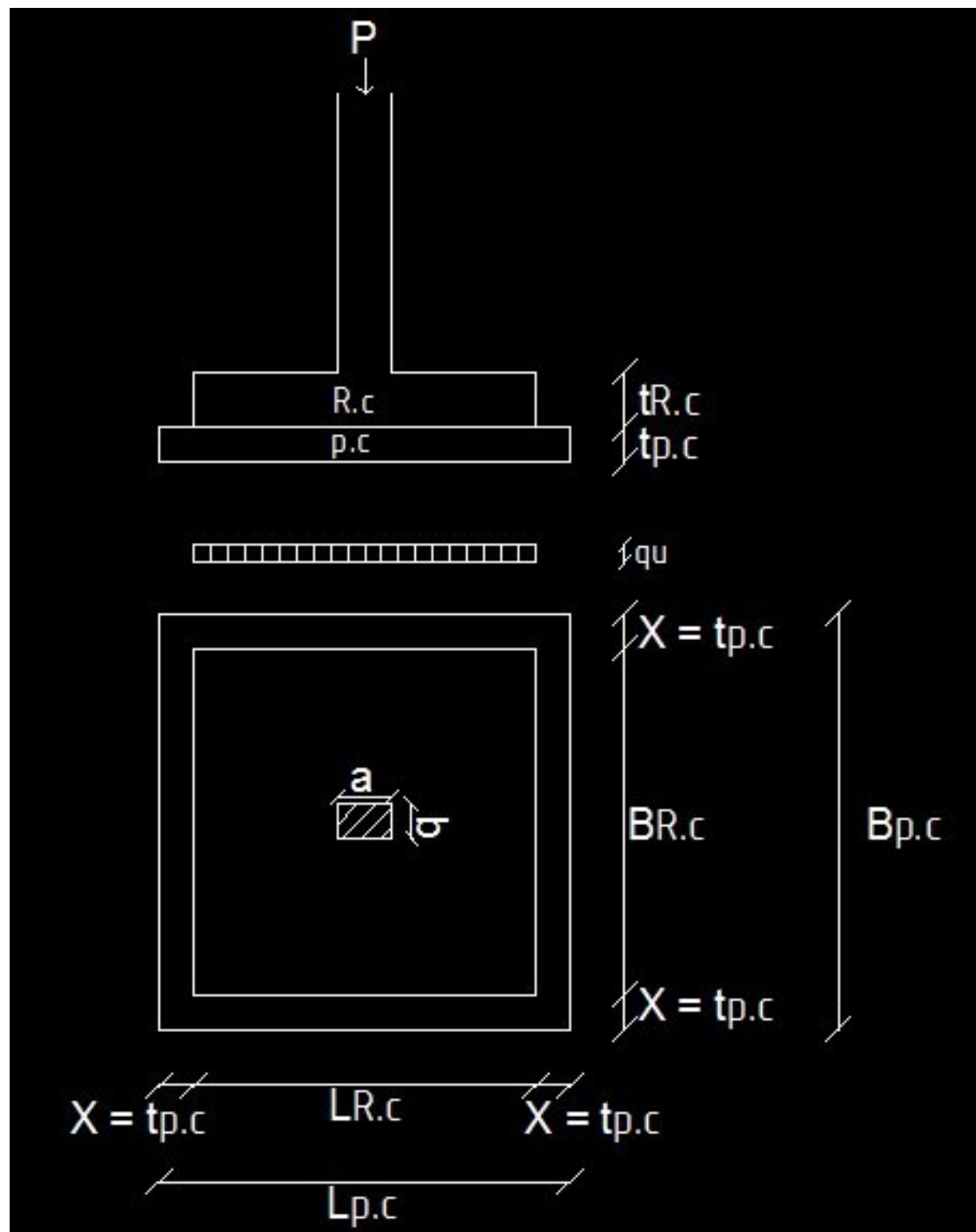
نأخذ القيمة الأكبر في القيم 1,2,3

If $A_s \geq A_{s \min} \rightarrow \text{ok}$

If $A_s < A_{s \min} \rightarrow \text{take } A_s = A_{s \min}$



Design of Isolated Rectangular footing:



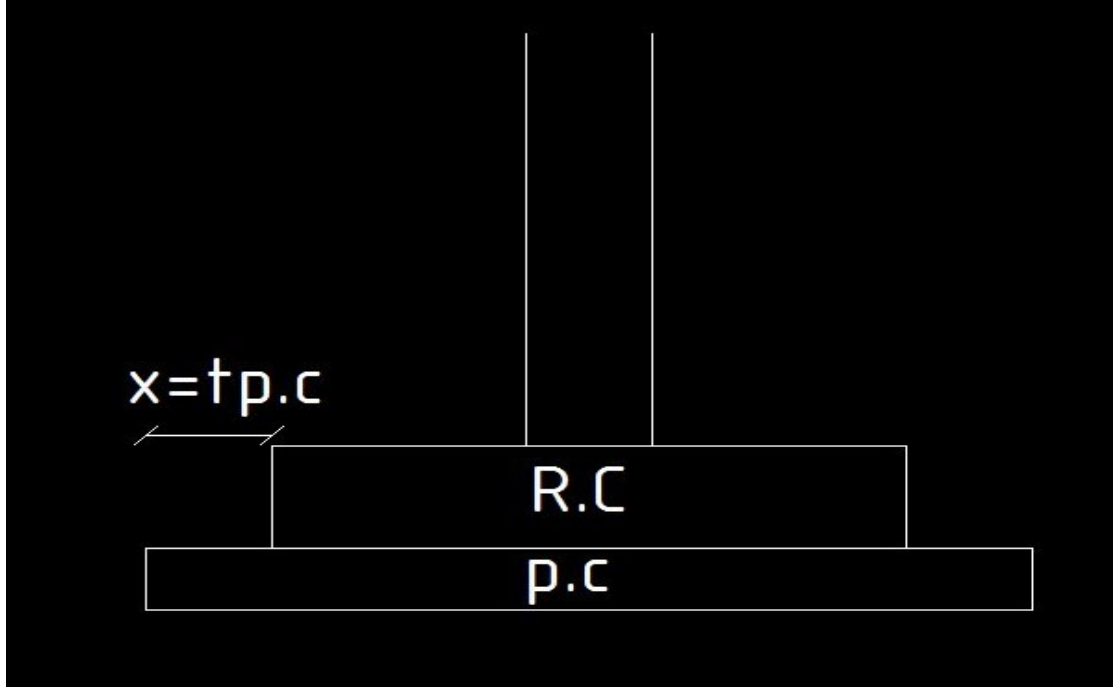
Procedure of Design:

Plain concrete:

If $t_{p.c} > 20$ cm	If $t_{p.c} \leq 20$ cm
Consider p.c in design	Neglect فرشہ نظافة فقط in design
$P_t = P_w * 1.1$	$P_t = P_w * 1.1$
$A_{p.c} = P_t / q_{all} = B_{p.c} \times L_{p.c}$	$A_{R.c} = P_t / q_{all} = B_{R.c} \times L_{R.c}$
$B_{p.c} = \sqrt{A_{p.c}}$	$B_{R.c} = \sqrt{A_{R.c}}$
نأخذ الفرق بين أبعاد القاعدة = الفرق بين أبعاد العمود $L_{p.c} + B_{p.c} = a - b$	نأخذ الفرق بين أبعاد القاعدة = الفرق بين أبعاد العمود $L_{R.c} + B_{R.c} = a - b$
$B_{R.c} = B_{p.c} - 2t_{p.c}$ $L_{R.c} = L_{p.c} - 2t_{p.c}$ \cong to the nearest 5cm	$B_{p.c} = B_{R.c} + 2t_{p.c}$ \cong to the nearest 5cm

Check stresses on plain concrete:

عند أخذ القاعدة العادية في الحسابات:



$$q_{ult} = 1.5 * p_w / (B_{p.c} * L_{p.c})$$

$$M_{ult} = (q_{ult} * (X^2)) / 2$$

$$F_t = 6 * M_{ult} / 100 * (t_{p.c})^2$$

$$F_{tcu} = (0.75 * (f_{cu})^{2/3}) / 1.5$$

If $F_t < F_{tcu}$ ok safe

If $F_t > F_{tcu}$ not safe (X) نقل بروز الخرسانة العادية

$$q_{ult} = 1.5 * p_w / (B_{p.c} * L_{p.c})$$

القطاعات الحرجة للعزوم:

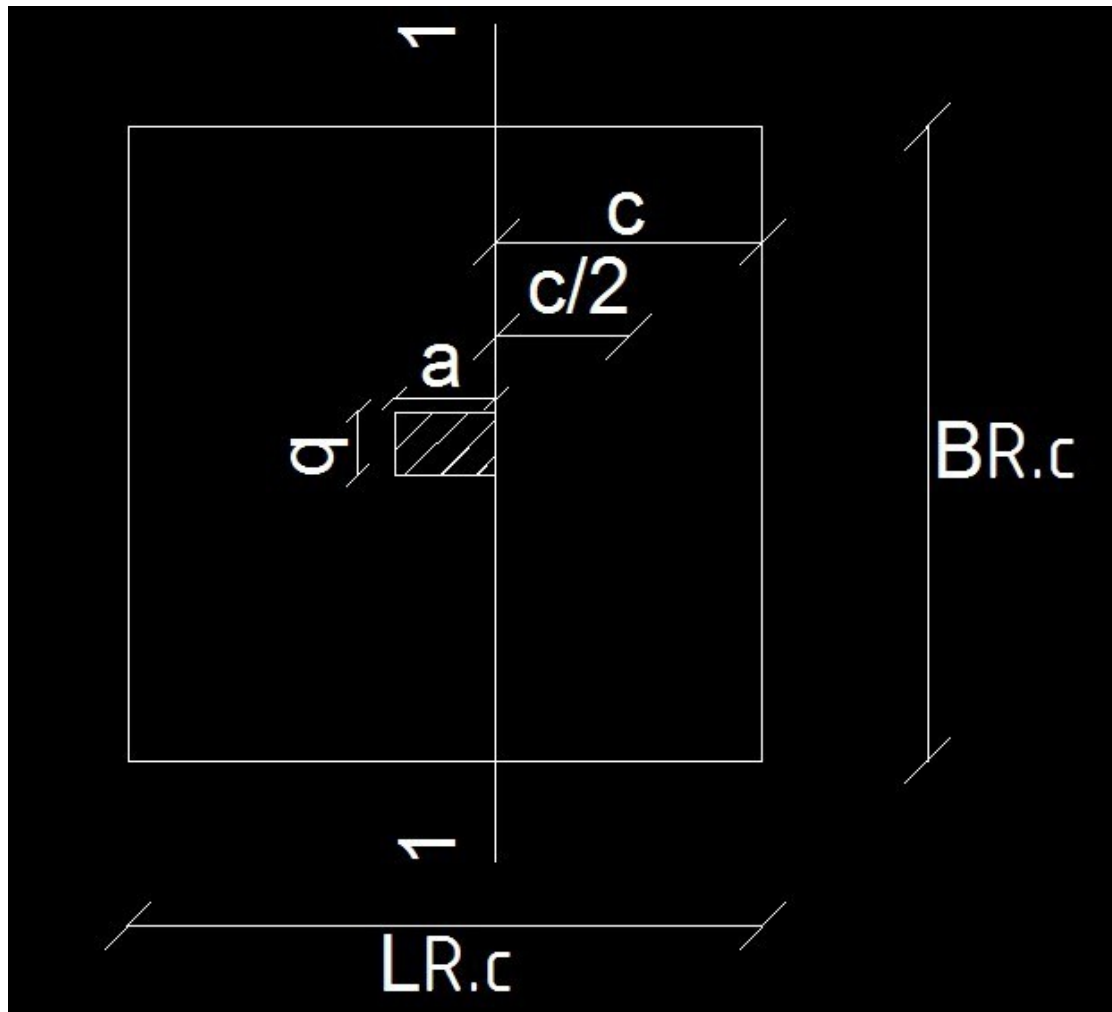
هناك طريقتين لحساب M_{ult}

الطريقة الأولى:

نأخذ القطاعات الحرجة للعزوم علي وش العمود من الجهتين

Critical section of bending at R.C Footing .

Direction 1:



$$C_1 = (L_{R.c} - a / 2)$$

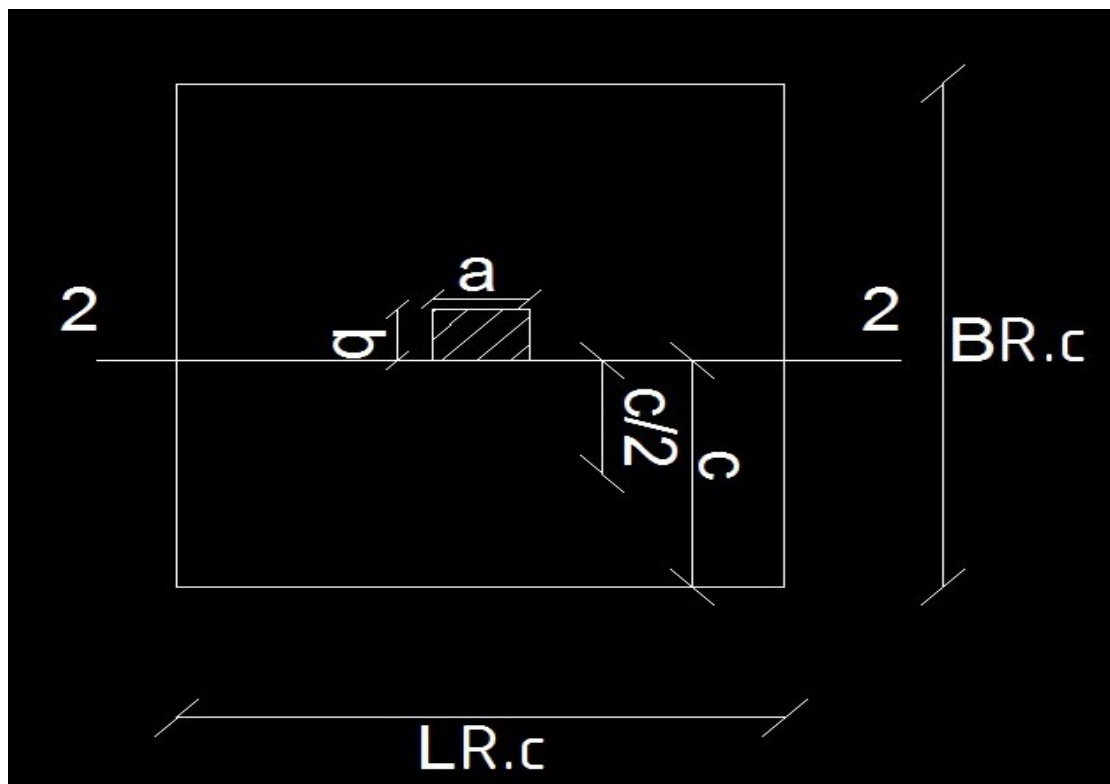
$$M_{ult 1} = q_{ult} * (B_{R.c} * c_1) * (c_1 / 2)$$

$$d_1 = c_1 \sqrt{\frac{M_{ult 1}}{F_{cu} * B_{R.c}}} \cong \text{to the nearest 5cm}$$

$$t_{1R.c} = d_1 + \text{cover} \cong \text{to the nearest 5cm}$$

cover = (5 to 10 cm)

Direction 2:



$$C_2 = (B_{R.c} - b / 2)$$

$$M_{ult 2} = q_{ult} * (L_{R.c} * c_2) * (c_2 / 2)$$

$$d_2 = c_1 \sqrt{\frac{\text{Mult}2}{F_{cu} * L_{R.C}}} \cong \text{to the nearest 5cm}$$

$$t_{2R.C} = d_2 + \text{cover} \cong \text{to the nearest 5cm}$$

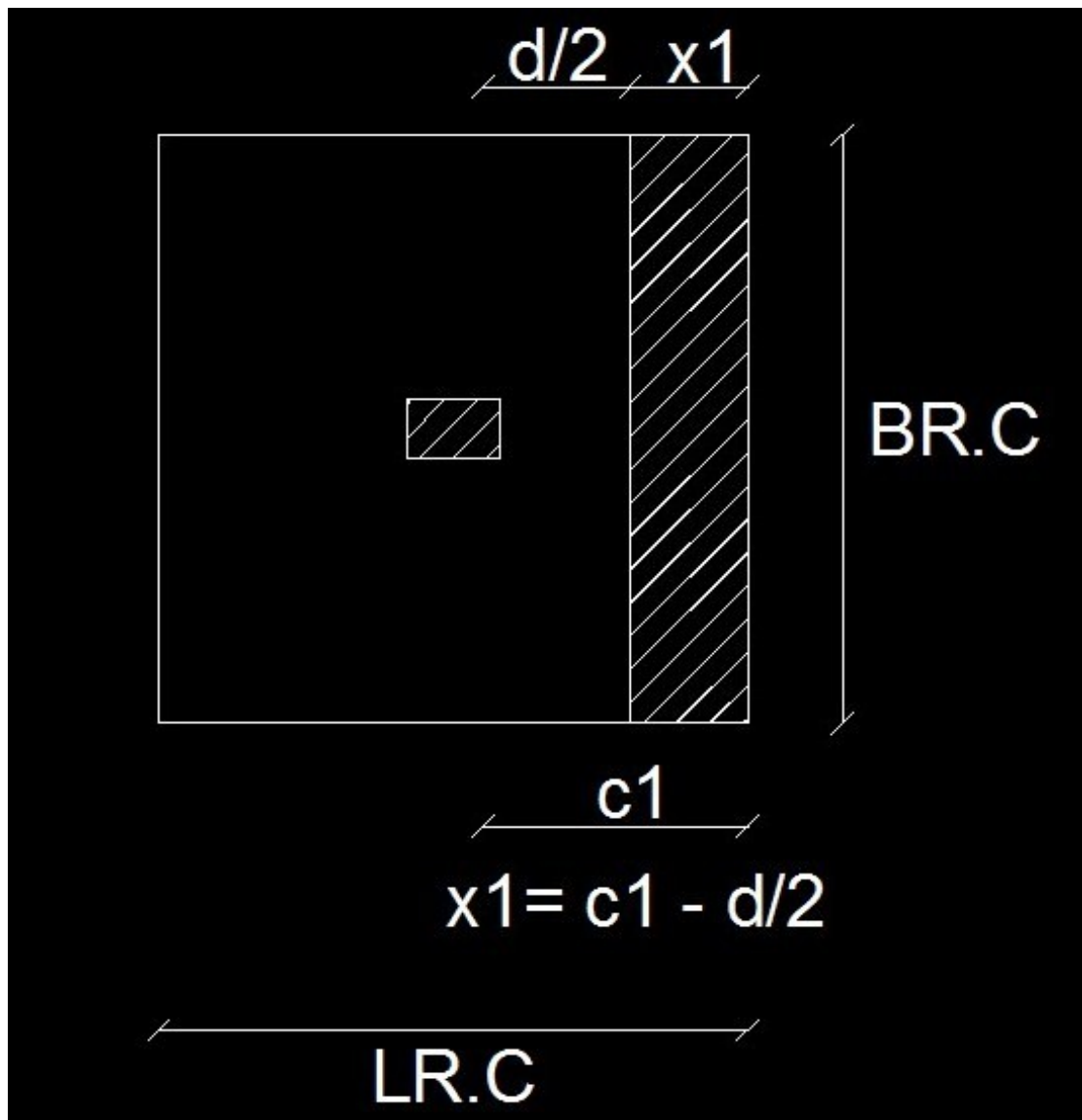
$$\text{cover} = (5 \text{ to } 10 \text{ cm})$$

Take the bigger of $t_{1R.C}$, $t_{2R.C} \rightarrow t_{R.C}$

Check shear:

القطاع الحرج علي مسافة $d/2$ من وش العمود.

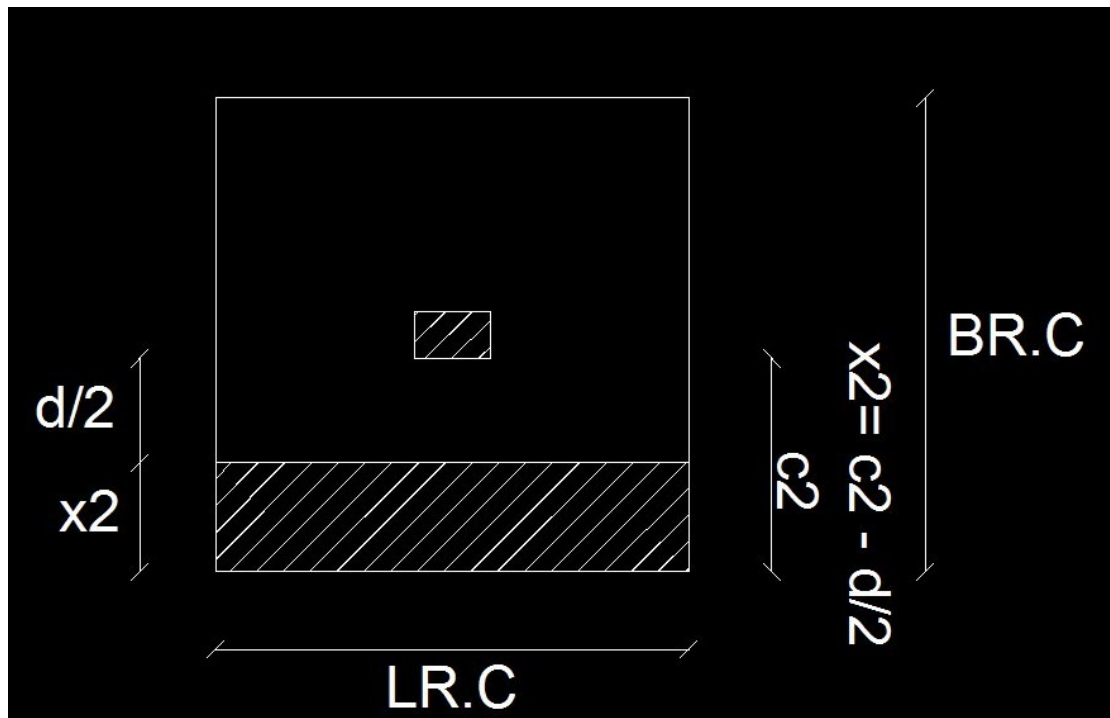
Critical section



$$Q_{sh1} = q_{ult} (B_{R.c} * (c_1 - d/2))$$

$$q_{sh1} = Q_{sh1} / (B_{R.c} * d)$$

$$q_{cu} = 0.4 \sqrt{f_{cu}}$$



$$Q_{sh2} = q_{ult} (L_{R.C} * (c_2 - d/2))$$

$$q_{sh2} = Q_{sh2} / (L_{R.C} * d)$$

$$q_{cu} = 0.4 \sqrt{f_{cu}}$$

Take the bigger of Q_{sh1} , Q_{sh2} and q_{sh1} , q_{sh2}

if $q_{sh} < q_{cu}$ ok safe

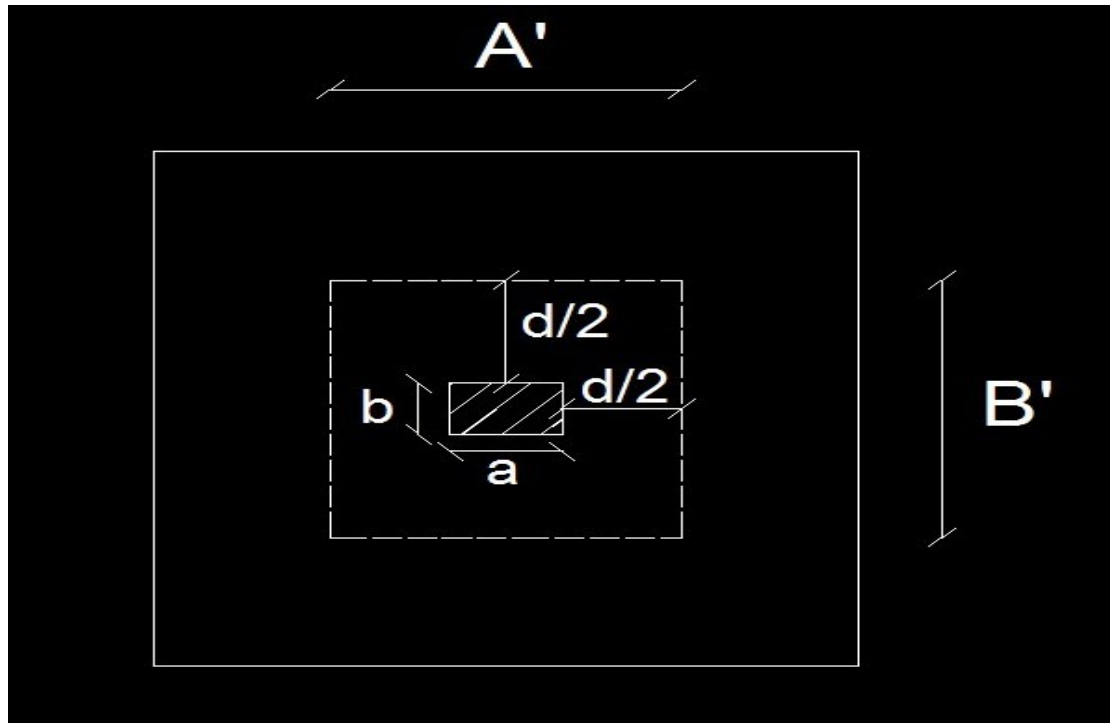
if $q_{sh} > q_{cu}$ not safe increase depth

$$d = Q_{sh} / (q_{cu} * B_{R.C} \text{ OR } L_{R.C})$$

$$t = d + \text{cover}$$

$$\text{cover} = (5 \text{ to } 10 \text{ cm})$$

Check punching:



$$Q_p = p_u - q_{ult} (A' + B')$$

$$A' = a + d, B' = b + d$$

$a \rightarrow$ طول العمود , $b \rightarrow$ عرض العمود

$$q_p = Q_p / (2(A' + B')d)$$

$$q_{pcu} = \left(0.5 + \frac{b}{a}\right) \sqrt{\frac{f_{cu}}{\gamma_c}}$$

If $q_{pcu} > q_p$ ok safe

If $q_{pcu} < q_p$ un safe \rightarrow increase depth

Reinforcement of the footing:

Min 5 y 12 / m

Max 10 y ?? / m

$$A_{s1} = M_{ult1} / J * d * f_y / B_{R.c} \text{ -----(1)}$$

$$A_{s2} = M_{ult2} / J * d * f_y / L_{R.c} \text{ -----(1)}$$

$$A_{s \min} = 5 \text{ y } 12 / \text{m} \text{ -----(2)}$$

$$A_{s \min} = (0.15 / 100) * B * d \text{ -----(3)}$$

نأخذ القيمة الأكبر في القيم 1,2,3

If $A_s \geq A_{s \min} \rightarrow \text{ok}$

If $A_s < A_{s \min} \rightarrow \text{take } A_s = A_{s \min}$

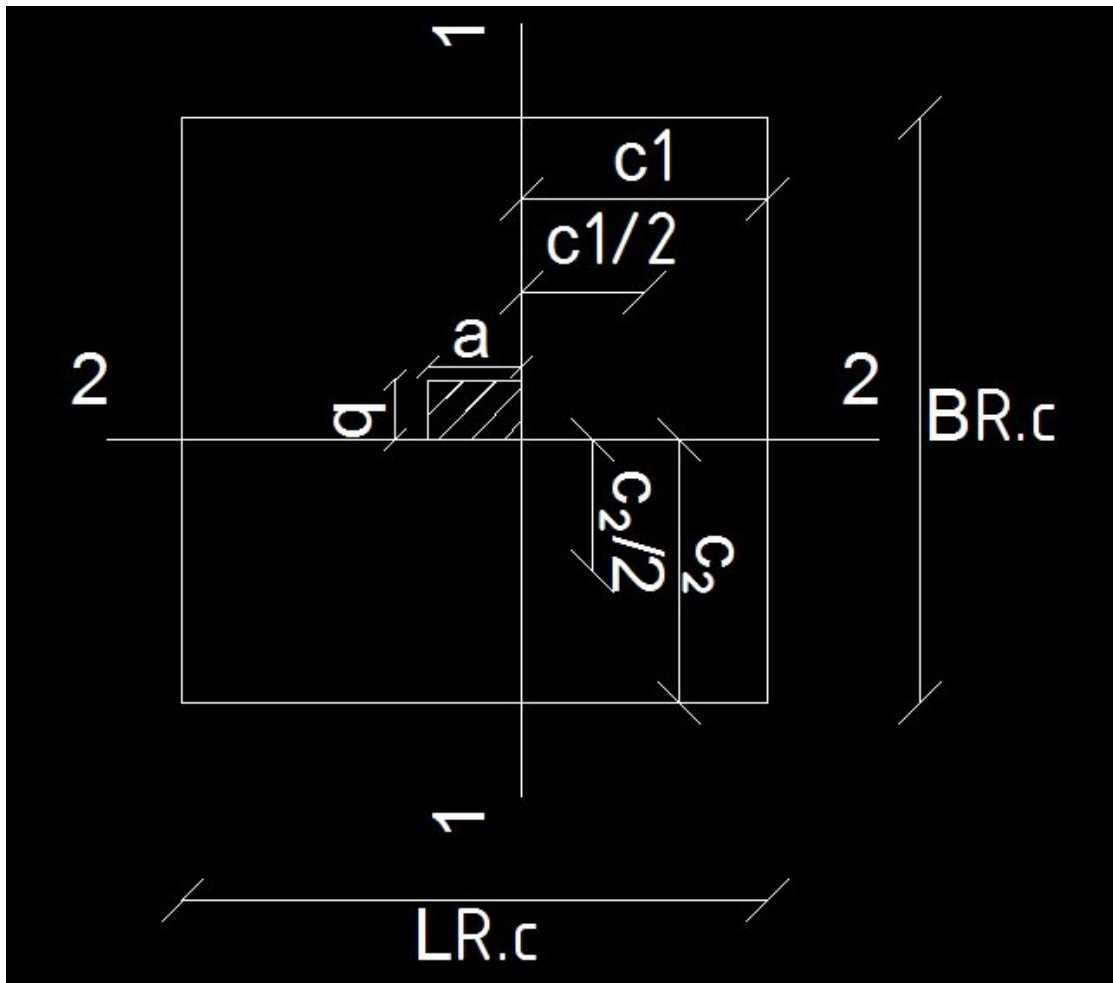
الطريقة الثانية:

نأخذ القطاعات الحرجة للعزوم علي وش العمود في اتجاه واحد فقط ولكن لابد من تحقق الشرط

$$L_{p.c} - B_{p.c} = a - b$$

فيكون $c_1 = c_2$ وبالتالي سيكون $M_{ult 1} = M_{ult 2}$ و من ثم
سيكون $d_1 = d_2$

$$q_{ult} = 1.5 * p_w / (B_{p.c} * L_{p.c}) = \dots \text{ t/m}^2$$



$$C = C_1 = C_2 = (L_{R.C} - a / 2) \text{ OR } (B_{R.C} - b / 2)$$

$$M_{ult1} = M_{ult2} = q_{ult} * C^2 / 2 = \dots \text{ m t/m'}$$

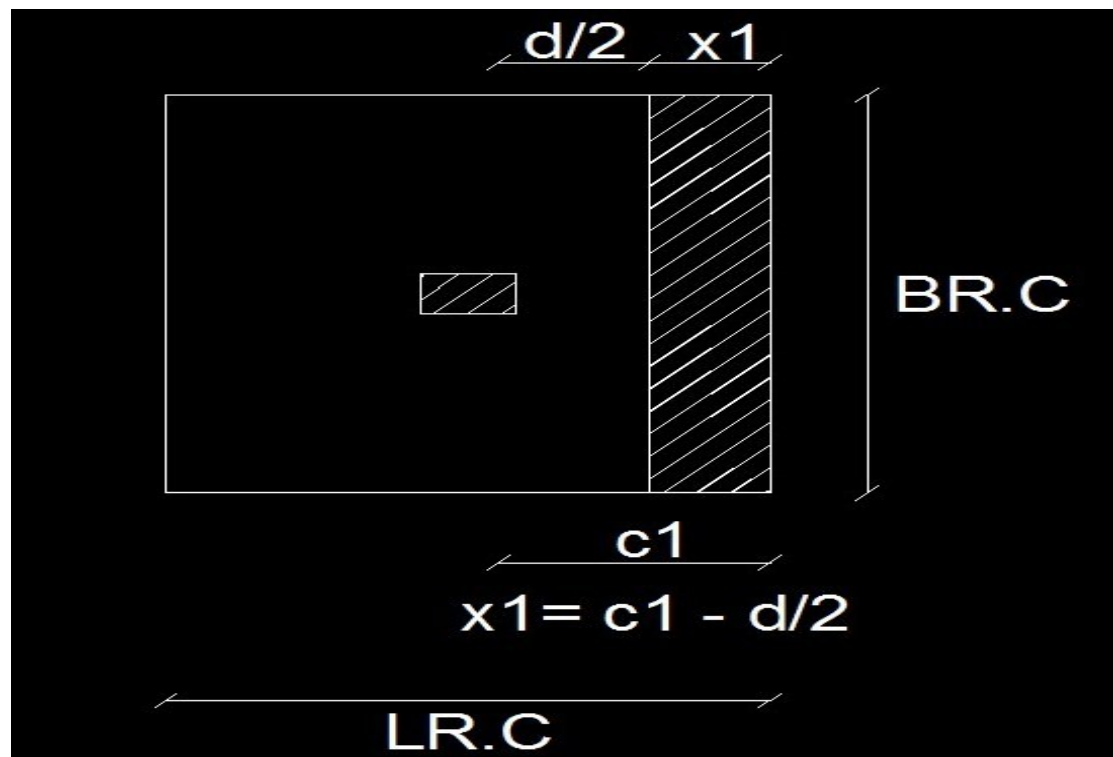
$$d = c_1 \sqrt{\frac{M_{ult1 \text{ or } 2}}{F_{cu} * b}} \cong \text{to the nearest 5cm} = \dots \text{ cm}$$

$$b = 100 \text{ cm شريحة}$$

Check shear:

القطاع الحرج علي مسافة $d/2$ من وش العمود.

Critical section



$$Q_{sh} = q_{ult} (c_1 - d/2) = \dots \text{ ton}$$

$$q_{sh} = Q_{sh} / (b * d) = \dots \text{ Kg/cm}^2$$

$$q_{cu} = 0.4 \sqrt{f_{cu}}$$

if $q_{sh} < q_{cu}$ ok safe

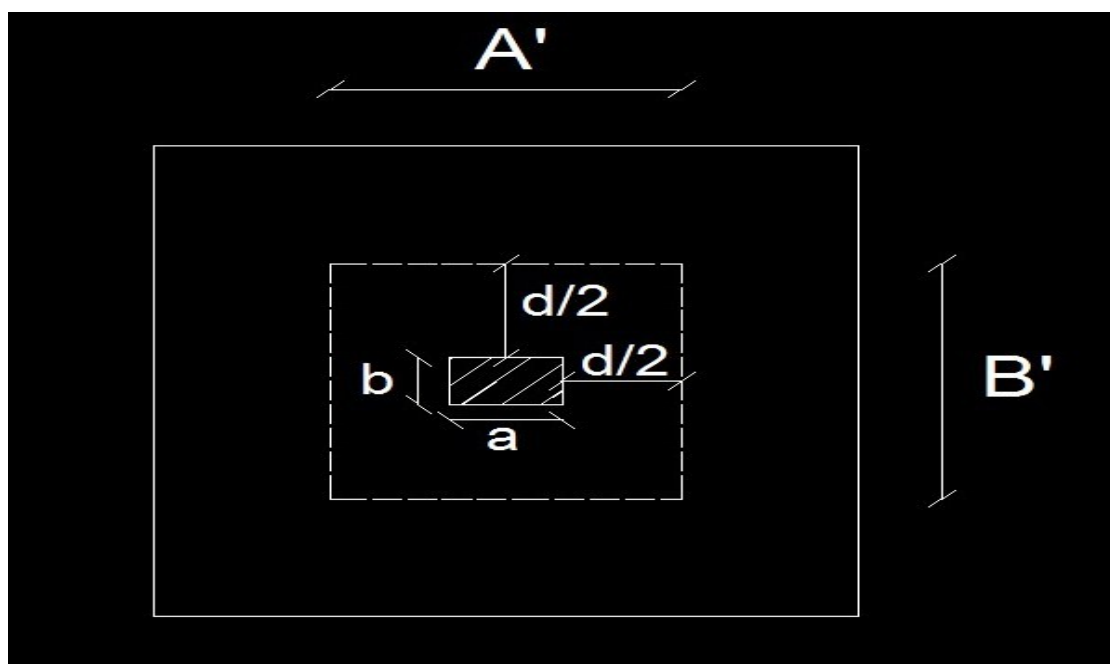
if $q_{sh} > q_{cu}$ not safe increase depth

$$d = Q_{sh} / (q_{cu} * b)$$

$$t = d + \text{cover}$$

$$\text{cover} = (5 \text{ to } 10 \text{ cm})$$

Check punching:



$$Q_p = p_u - q_{ult} (A'+B') = \dots \text{ ton}$$

$$A' = a + d , B' = b + d$$

$a \rightarrow$ طول العمود , $b \rightarrow$ عرض العمود

$$q_p = Q_p / (2(A'+B')d) = \dots \text{ Kg/cm}^2$$

$$q_{pcu} = \left(0.5 + \frac{b}{a}\right) \sqrt{\frac{f_{cu}}{\gamma_c}} = \dots \text{ Kg/cm}^2$$

If $q_{pcu} > q_p$ ok safe

If $q_{pcu} < q_p$ un safe \rightarrow increase depth

$$t = d + \text{cover}$$

$$\text{cover} = (5 \text{ to } 10 \text{ cm})$$

Reinforcement of the footing:

$$\text{Min } 5 \text{ y } 12 / \text{ m}$$

$$\text{Max } 10 \text{ y } ?? / \text{ m}$$

$$A_{s1} = A_{s2} = M_{ult} / J * d * f_y = \dots \text{ cm}^2 / \text{ m}' \text{ ---(1)}$$

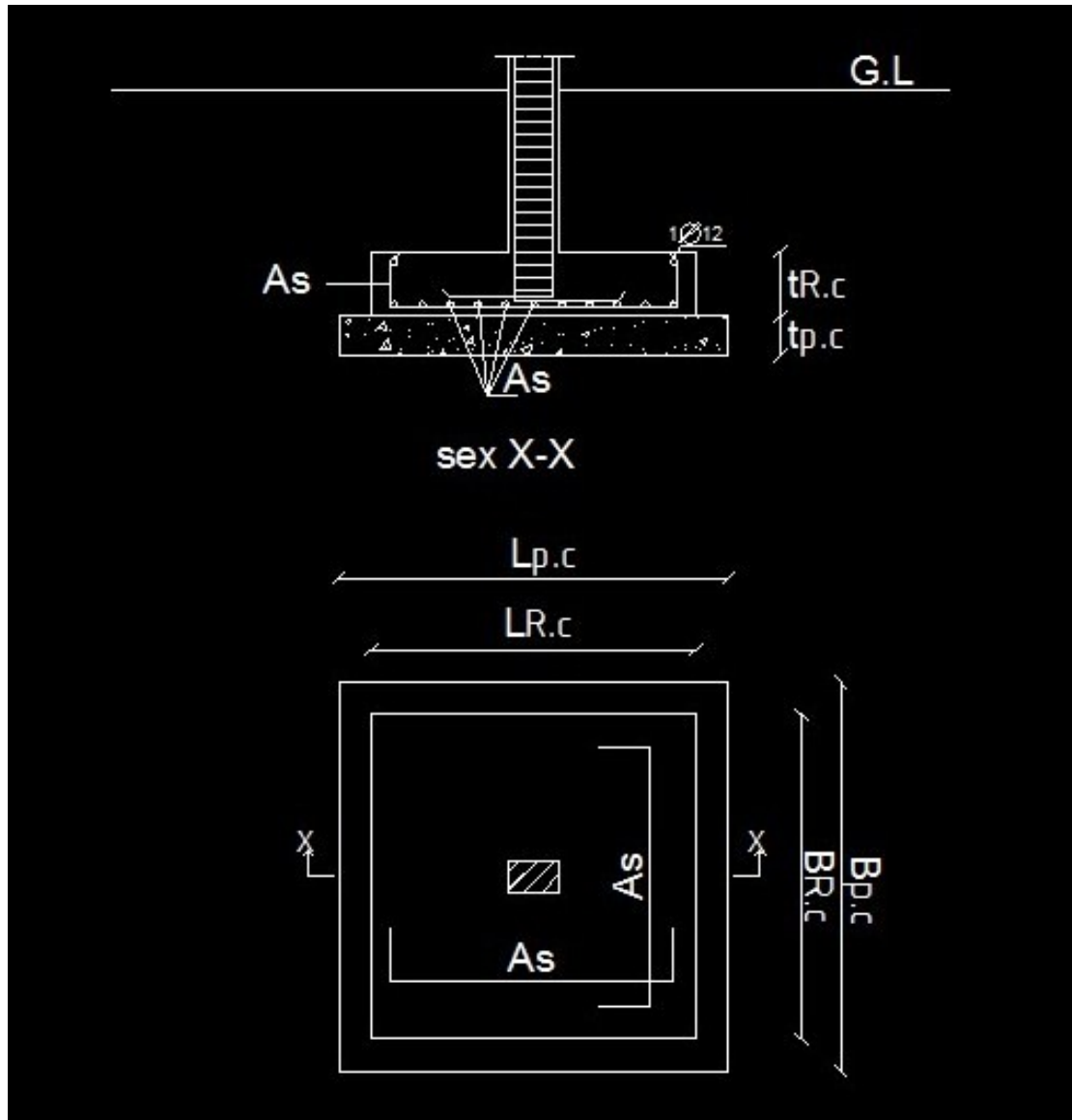
$$A_{s \text{ min}} = 5 \text{ y } 12 / \text{ m}' \text{ ---(2)}$$

$$A_{s \text{ min}} = (0.15 / 100) * b * d = \dots \text{ cm}^2 / \text{ m}' \text{ ---(3)}$$

نأخذ القيمة الأكبر في القيم 1,2,3

If $A_s \geq A_{s \text{ min}} \rightarrow \text{ok}$

If $A_s < A_{s \text{ min}} \rightarrow \text{take } A_s = A_{s \text{ min}}$



Example: 1

Given : $f_{cu} = 250 \text{ kg/cm}^2$, $P_{ult} = 1800 \text{ kN}$,

Col 30x70 cm , $f_y = 3600 \text{ kg/cm}^2$, $t_{p,c} = 50 \text{ cm}$, B/C ($q_{all} = 150 \text{ kN / m}^2$)

Req : Design of strip footing that carry the given line load.

Solution

$$100 \text{ kN / m}^2 = 10 \text{ t / m}^2 = 1 \text{ kg / cm}^2$$

$$P_{ult} = 1800 \text{ KN} \rightarrow 180 \text{ ton}$$

$$q_{all} = 150 \text{ KN/m}^2 \rightarrow 15 \text{ t/m}^2$$

$$t_{p.c} > 20 \text{ cm}$$

$$50 > 20 \text{ cm} \rightarrow \text{Consider p.c in design}$$

$$P_w = \frac{p_{ult}}{1.5} = \frac{180}{1.5} = 120 \text{ Ton}$$

$$P_t = P_w * 1.1 = 120 * 1.1 = 132 \text{ ton}$$

$$A_{p.c} = P_t / q_{all} = 132 / 15 = 8.8 \text{ m}^2$$

هنالك طريقتين لإيجاد قيمة أبعاد القاعدة العادية:

الطريقة الأولى أسهل و أسرع من الطريقة الثانية والنتيجة نفسها.

الطريقة الأولى:

$$a - b = 0.7 - 0.3 = 0.4 \text{ m}$$

$$L_{p.c} = \sqrt{A_{p.c}} + (a - b / 2)$$

$$B_{p.c} = \sqrt{A_{p.c}} - (a - b / 2)$$

$$\sqrt{A_{p.c}} = \sqrt{8.8} = 2.97 \cong 3 \text{ m}$$

$$L_{p.c} = 3 + 0.2 = 3.2 \text{ m}$$

$$B_{p.c} = 3 - 0.2 = 2.8 \text{ m}$$

الطريقة الثانية:

$$A_{p.c} = P_t / q_{all} = 132 / 15 = 8.8 \text{ m}^2 = L_{p.c} * B_{p.c}$$

$$L_{p.c} * B_{p.c} = 8.8$$

$$L_{p.c} = 8.8 / B_{p.c} \dots\dots\dots 1$$

$$L_{p.c} - B_{p.c} = a - b$$

$$L_{p.c} - B_{p.c} = 0.7 - 0.3 = 0.4$$

$$L_{p.c} = B_{p.c} + 0.4 \dots\dots\dots 2$$

بالتعويض عن $L_{p.c}$ في المعادلة رقم 1

$$8.8 / B_{p.c} - B_{p.c} = 0.4$$

بالضرب في $B_{p.c}$

$$8.8 - (B_{p.c})^2 = 0.4 B_{p.c}$$

$$B_{p.c}^2 + 0.4 B_{p.c} - 8.8 = 0$$

$$ax^2 + bx + c = 0$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$B_{p.c}^2 + 0.4 B_{p.c} - 8.8 = 0$$

$$B_{p.c} = \frac{-0.4 \pm \sqrt{(0.4)^2 - (4 * 1 * (-8.8))}}{2 * 1}$$

$$B_{p.c} = 2.77 \text{ m} \cong 2.8 \text{ m}$$

في التعويض بالمعادلة مرة بالسالب ومرة بالموجب
والنتيجة السالبة مرفوض.

بالتعويض بالمعادلة رقم 2 بقيمه $B_{p.c}$ لإيجاد $L_{p.c}$

$$L_{p.c} = B_{p.c} + 0.4$$

$$L_{p.c} = 2.8 + 0.4 = 3.2 \text{ m}$$

Check stresses on plain concrete:

$$q_{ult} = 1.5 * p_w / (B_{p.c} * L_{p.c}) = \frac{180}{3.2 * 2.8} = 20 \text{ t / m}^2$$

$$M_{ult} = (q_{ult} * (X^2)) / 2 = \frac{20 * (0.5)^2}{2} = 2.5 \text{ mt}$$

$$F_t = 6 * M_{ult} / 100 * (t_{p.c})^2 = \frac{6 * (2.5 * 10^5)}{100 * (50)^2} = 6 \text{ kg/cm}^2$$

$$F_{tcu} = \frac{0.75 * (f_{cu})^{\frac{2}{3}}}{1.5} = \frac{0.75 * (250)^{\frac{2}{3}}}{1.5} = 19.8 \text{ kg/cm}^2$$

$$F_t < F_{tcu}$$

6 < 19.8 ok safe

ملاحظة:

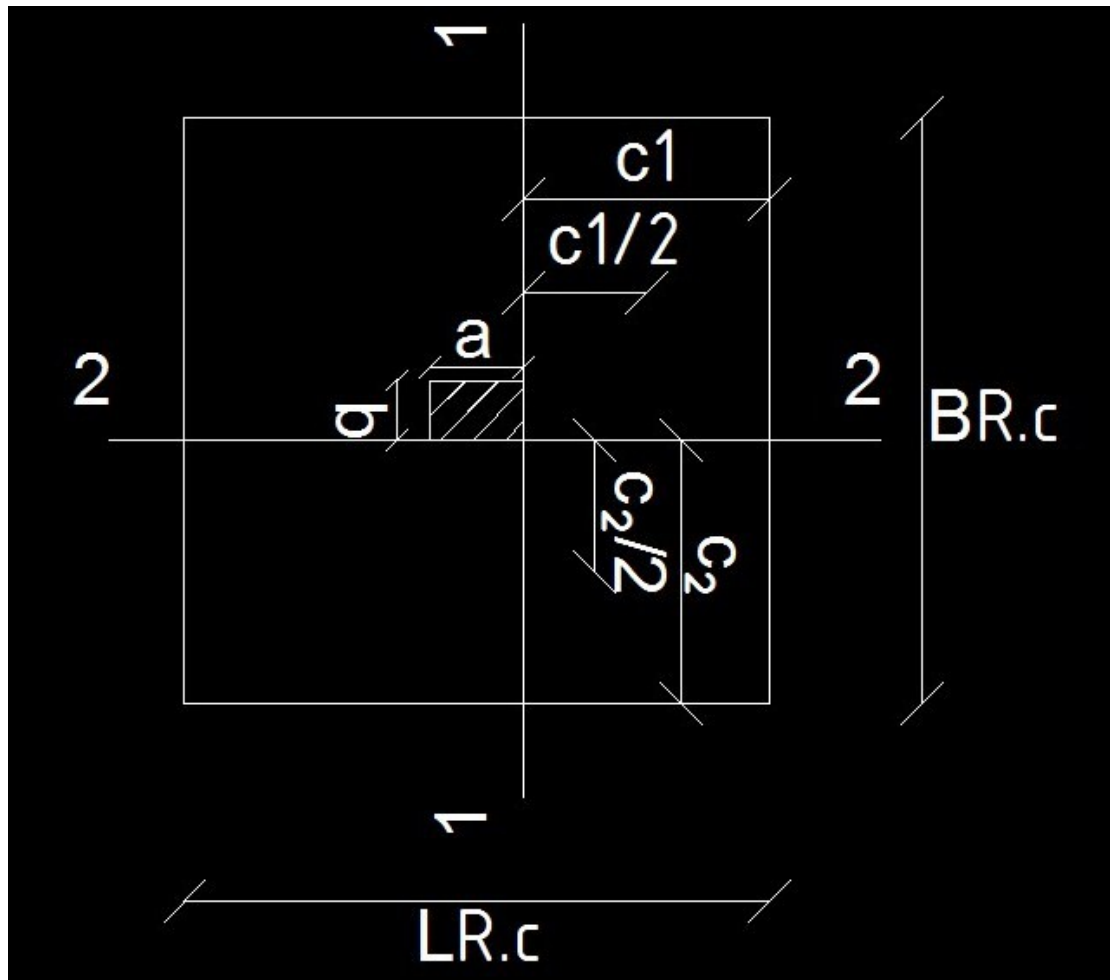
لإيجاد قيمة $L_{R.C}$ و $B_{R.C}$ يمكن إيجادها قبل Check stresses on plain concrete و لكن يتم إيجادها بعد علشان $L_{R.C}$ و $B_{R.C}$ يعتمد علي $t_{p.c}$ لو ال check طلع

un safe يتم نقل بروز الخرسانة العادية ($t_{p.c}$)

$$L_{R.C} = L_{p.c} - 2 t_{p.c} = 3.2 - (2 * 0.5) = 2.2 \text{ m}$$

$$B_{R.C} = B_{p.c} - 2 t_{p.c} = 2.8 - (2 * 0.5) = 1.8 \text{ m}$$

$$q_{ult} = 1.5 * p_w / (B_{R.c} * L_{R.c}) = \frac{180}{2.2 * 1.8} = 45.5 \text{ t / m}^2$$



$$C = (L_{R.c} - a / 2) = \frac{2.2 - 0.7}{2} = 0.75$$

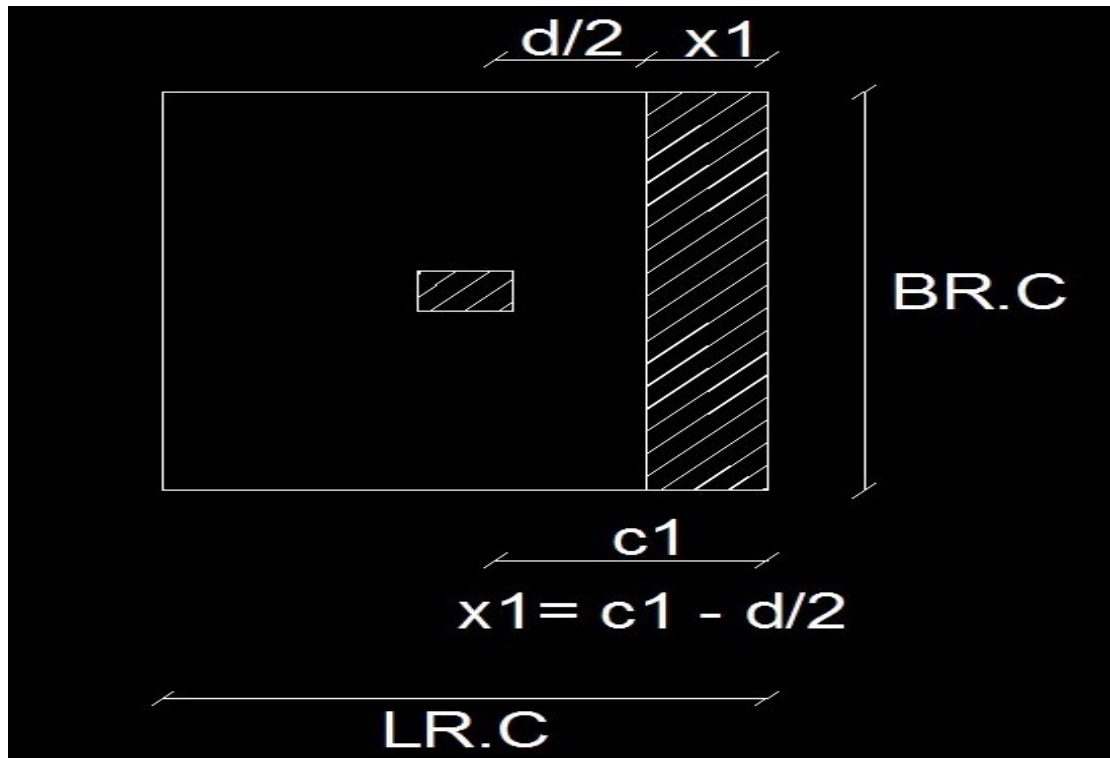
$$M_{ult} = q_{ult} * C^2 / 2 = \frac{45.5 * (0.75)^2}{2} = 12.8 \text{ m t/m'}$$

$$d = c_1 \sqrt{\frac{M_{ult}}{F_{cu} * b}} = 5 \sqrt{\frac{12.8 * 10^5}{250 * 100}} = 35.7 \text{ cm} \cong 40 \text{ cm}$$

Check shear:

القطاع الحرج علي مسافة $d/2$ من وش العمود.

Critical section



$$Q_{sh} = q_{ult}(c - d/2) = 45.5(0.75 - 0.4/2) = 25 \text{ ton}$$

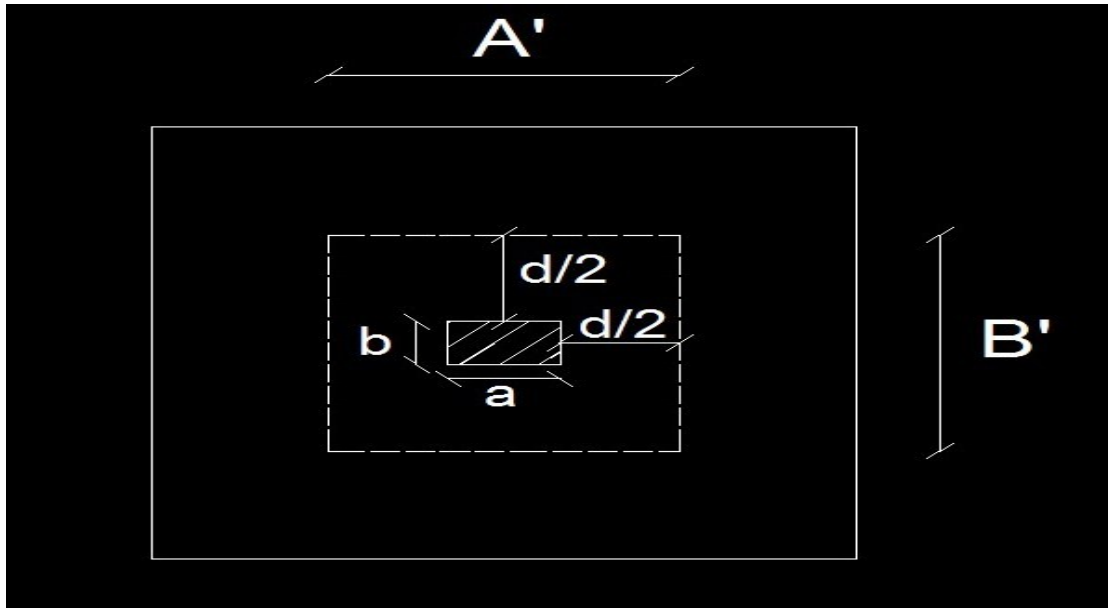
$$q_{sh} = Q_{sh}/(b*d) = \frac{25*10^3}{100*40} = 6.25 \text{ Kg/cm}^2$$

$$q_{cu} = 0.4 \sqrt{f_{cu}} = 0.4 \sqrt{250} = 6.3 \text{ Kg/cm}^2$$

$$q_{sh} < q_{cu}$$

6.25 < 6.3 ok safe

Check punching:



$$Q_p = p_u - q_{ult} (A' + B') =$$

$$A' = a + d = 0.7 + 0.4 = 1.1 \text{ m}$$

$$B' = b + d = 0.3 + 0.4 = 0.7 \text{ m}$$

$$Q_p = p_u - q_{ult} (A' + B') = 180 - 45.5 (1.1 * 0.7) = 145 \text{ ton}$$

$$q_p = Q_p / (2(A' + B')d) = \frac{145 * 10^3}{(2(110 + 70) * 40)} = 10 \text{ Kg/cm}^2$$

$$q_{pcu} = \left(0.5 + \frac{b}{a}\right) \sqrt{\frac{f_{cu}}{\gamma_c}} = \left(0.5 + \frac{0.3}{0.7}\right) \sqrt{\frac{250}{1.5}} = 12 \text{ Kg/cm}^2$$

$$q_{pcu} > q_p$$

12 > 10 ok safe

$$t = d + \text{cover} = 40 + 10 = 50 \text{ cm}$$

Reinforcement of the footing:

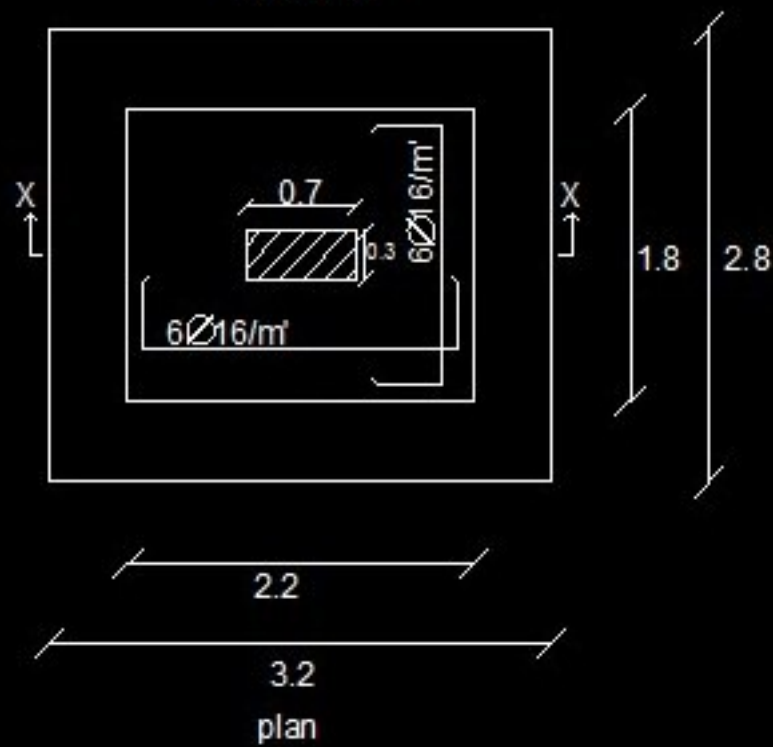
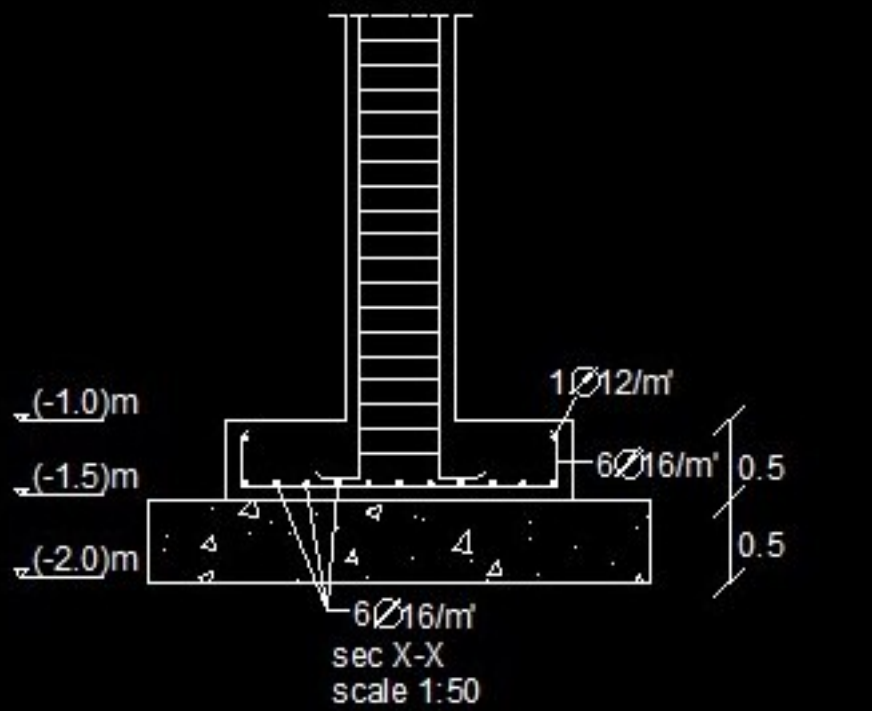
$$A_{s1}=A_{s2}=\frac{\text{Mult}}{J*d*fy}=\frac{12.8*10^5}{0.826*40*3600}=10.76 \text{ cm}^2/\text{m}'$$

$$A_{s \text{ min}} = 5y12/\text{m} = 5.65 \text{ cm}^2 / \text{m}'$$

$$A_{s \text{ min}}=\frac{0.15}{100}*b*d=\frac{0.15}{100}*100*40 = 6 \text{ cm}^2/\text{m}'$$

take $A_s = 10.76 \text{ cm}^2/\text{m}'$

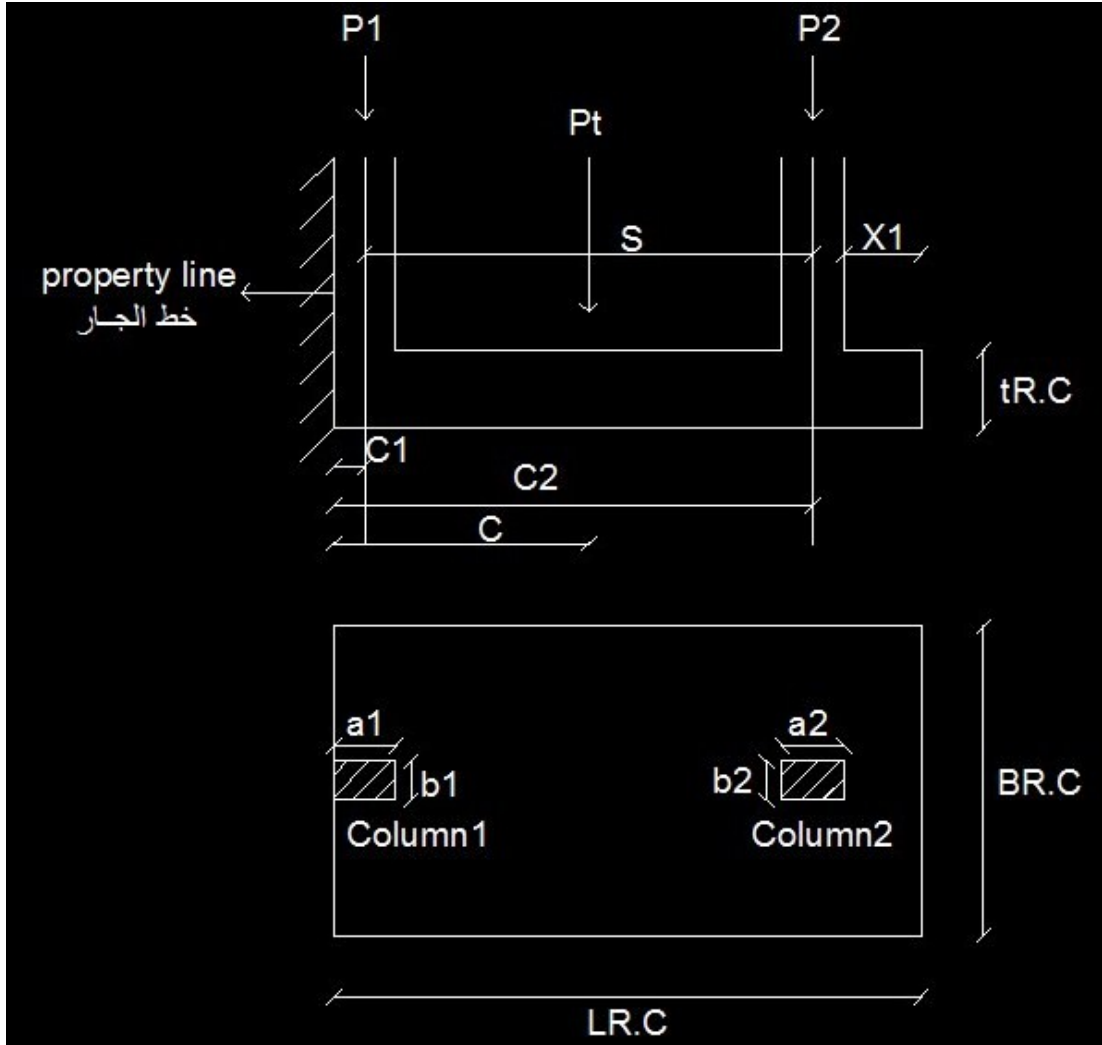
use 6 y 16 /m



Combined Footing:

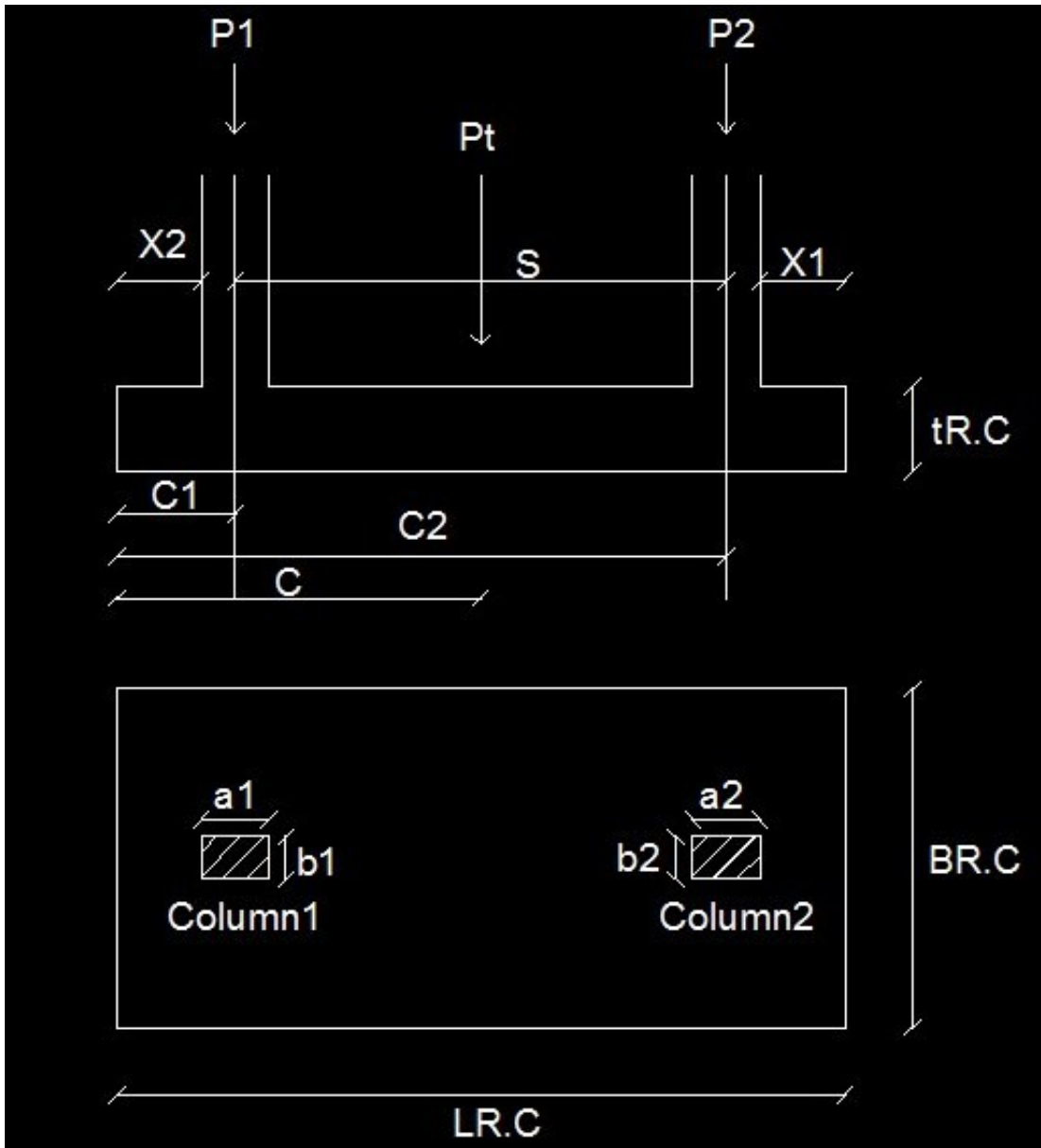
Types of Combined Footing:

1- قاعدة بعمود داخلي مع عمود جار:



البروز من ناحية واحدة فقط.

2- عمودان داخليان:



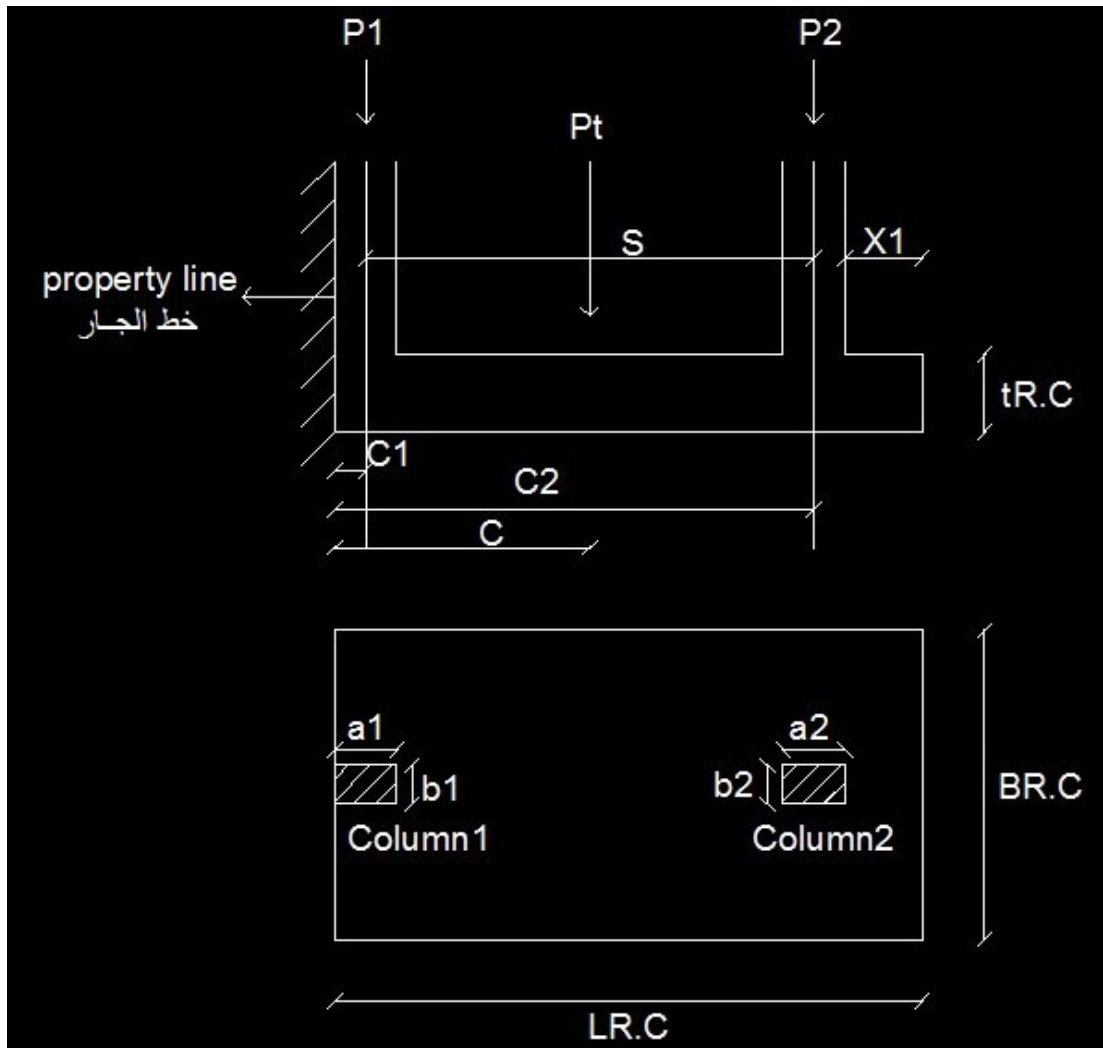
البروز من ناحيتين.

نأخذ C1 من ناحية العمود الأقل بالحمل $P1 < P2$

Take C1 = 1 m if not given.

Steps of Design:

1) Dimension of Footing (working Loads):



$$P_t = (P_1 + P_2) * 1.1 = \dots \text{ Ton}$$

$(P_1 + P_2) \rightarrow$ Working Loads حيث أن

Working Loads to ultimate Loads * 1.5

Ultimate Loads to Working Loads / 1.5

$$\text{Area of Footing } (A_{R.C}) = \frac{P_t}{q_{all}} = L * B = m^2$$

لا تدخل الخرسانة العادية في الحسابات في حالة الجار لعدم وجود سماح ببروز من ناحية الجار.

Take $C_1 =$ من خط الجار إلي نص العمود

$$C_2 = C_1 + S = \dots m$$

$$C = \frac{(c_1 * p_1) + (c_2 * p_2)}{p_t} = \dots m$$

حيث أن:

$C \rightarrow$ مكان تأثير

$P_t \rightarrow$ محصله القوي

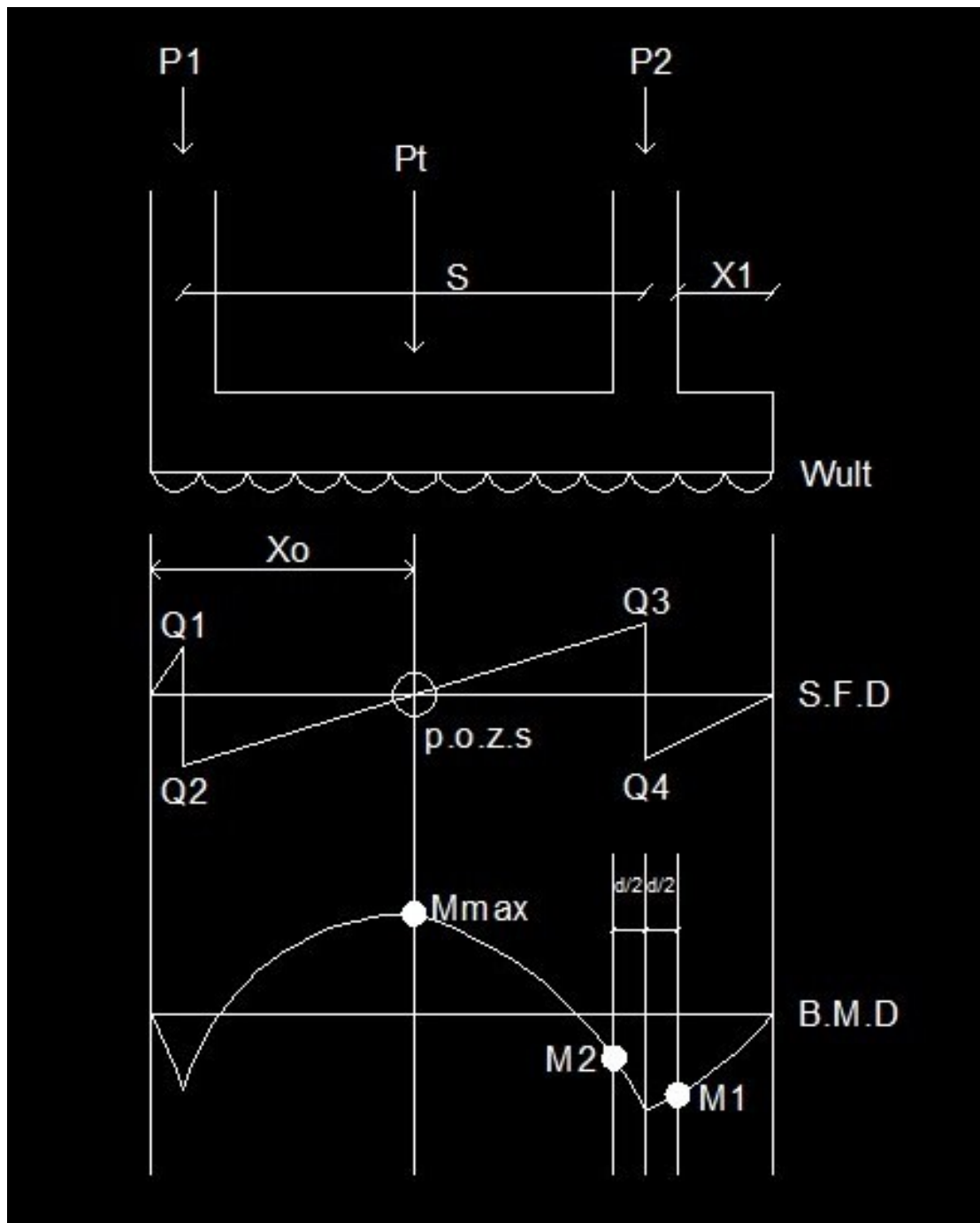
حتى تكون المحصلة في نصف القاعدة

$$L_{R.C} = 2 * C = \dots m \cong \text{to nearest } 5 \text{ cm}$$

$$B_{R.C} = \frac{A.R.C}{L.R.C} = \dots m \cong \text{to nearest } 5 \text{ cm}$$

End of Working Loads

2) Ultimate stress & Draw B.M.D & S.F.D:



$$q_{ult} = \frac{(p1+p2)*1.5}{LR.C*BR.C} = \dots \text{ t/m}^2$$

$$W_{ult} = q_{ult} * B_{R.C} = \dots \text{ t/m'}$$

$$Q_1 = W_{ult} * C_1 = \dots \text{ Ton}$$

$$Q_2 = Q_1 - P_{1u} = \dots \text{ Ton}$$

$$Q_3 = W_{ult} * C_2 - P_{1u} = \dots \text{ Ton}$$

$$Q_4 = Q_3 - P_{2u} = \dots \text{ Ton}$$

Moment يحسب عند وش العمود M_1, M_2

Max Moment at point of zero shear

At p.o.z.s

$$X_0 = \frac{P_{1u}}{W_u} = \dots \text{ m}$$

$$X_1 = L_{R.C} - \left(C_2 + \frac{b^2 \text{ or } a^2}{2} \right) = \dots \text{ m}$$

حيث أن:

مسافة من خط الجار إلي point of zero shear

p.o.z.s → point of zero shear

a → طول العمود

b → عرض العمود

b² or a² → حسب اتجاه العمود

$$M_1 = W_u * \frac{(X1)^2}{2} = \dots \text{ mt}$$

$$M_2 = W_u * \frac{(X1+a2 \text{ or } b2)^2}{2} - P_{2u} * \frac{a2 \text{ or } b2}{2} = \dots \text{ mt}$$

حيث أن:

a → طول العمود

b → عرض العمود

b2 or a2 → حسب اتجاه العمود

$$M_{\max} = P_{1u} * (X_o - C_1) - (W_u * \frac{(X_o)^2}{2}) = \dots \text{ mt}$$

3) Calculation the Depth:

$$d = c1 \sqrt{\frac{M_u}{F_{cu} * B * R.C}}$$

حيث أن:

c1 → 5

M_u → Max Moment

4) Check shear:

Critical section at $\frac{d}{2}$ من وش العمود

$$Q_{sh} = Q_{Max} - W_u \left(\frac{d}{2} + \frac{a1 \text{ or } a2 \text{ or } b1 \text{ or } b2}{2} \right) = \dots \text{ Ton}$$

حيث أن:

a → طول العمود

b → عرض العمود

Q_{Max} حسب اتجاه العمود → b^2 or a^2 و حسب

$Q_{Max} \rightarrow \text{Max of } Q_1, Q_2, Q_3, Q_4$

$$q_{sh} = \frac{Q_{sh}}{B.R.C * d} = \dots \text{ kg/cm}^2$$

$$q_{cu} = 0.4 * \sqrt{F_{cu}} = \dots \text{ kg/cm}^2$$

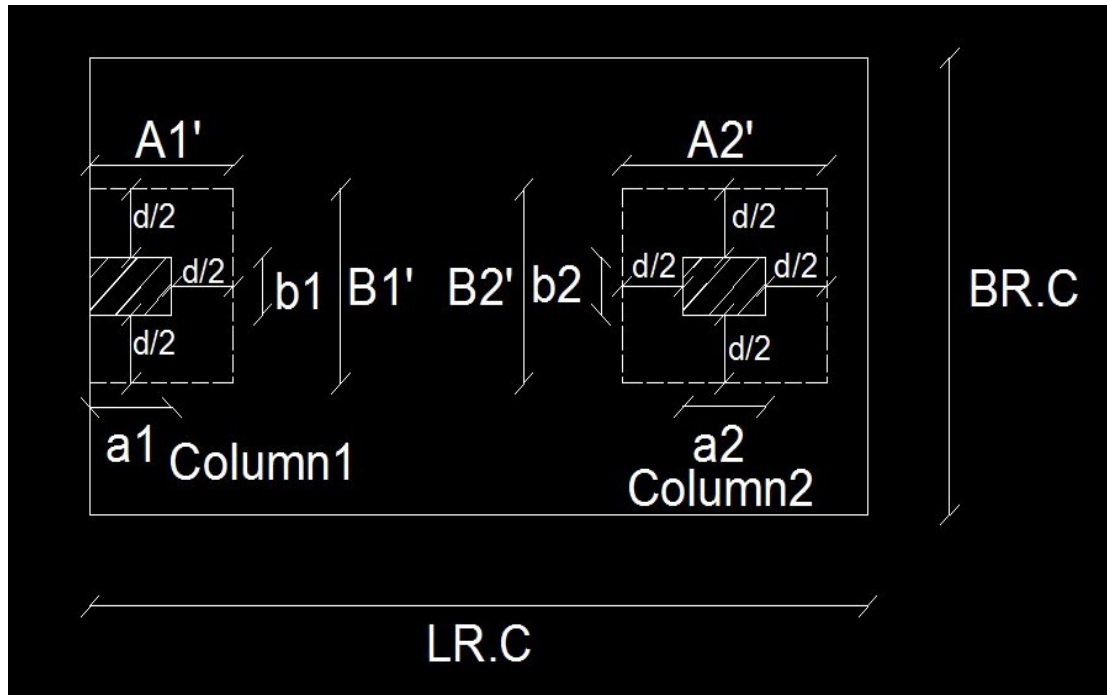
If $q_{cu} > q_{sh}$ ok safe

If $q_{cu} < q_{sh}$ un safe increase depth

$$\text{Take } d = \frac{Q_{sh}}{(q_{cu} * B_{R.C})} = \dots \text{ cm}$$

5) Check Punching:

الحالة الأولى:



For Column 1:

$$Q_{P1} = P_{u1} - q_U (A_1' * B_1') = \dots \text{ Ton}$$

حيث أن :

$$A_1' = (a_1 + \frac{d}{2}) = \dots \text{ m}$$

$$B_1' = (b_1 + d) = \dots \text{ m}$$

For Column 2:

$$Q_{P2} = P_{u2} - q_U (A_2' * B_2') = \dots \text{ Ton}$$

حيث أن :

$$A_2' = (a_2 + d) = \dots \text{ m}$$

$$B_2' = (b_2 + d) = \dots \text{ m}$$

$$q_p = \frac{Q_{p\text{Max}}}{2*(A_{1\text{or}2'} + B_{1\text{or}2'}) * d} = \dots \text{ kg/cm}^2$$

حيث أن:

$$Q_{p\text{Max}} = \text{Max of } Q_{p1} \text{ \& } Q_{p2}$$

If $Q_{p\text{Max}} \rightarrow Q_{p1}$ Take A_1' , B_1'

If $Q_{p\text{Max}} \rightarrow Q_{p2}$ Take A_2' , B_2'

$$q_{pcu} = \left(0.5 + \frac{b_{1\text{or}2}}{a_{1\text{or}2}} \right) \sqrt{\frac{F_{cu}}{\gamma_c}} = \dots \text{ kg/cm}^2$$

حسب أن:

If $Q_{p\text{Max}} \rightarrow Q_{p1}$ Take b_1 , b_2

If $Q_{p\text{Max}} \rightarrow Q_{p2}$ Take a_1 , a_2

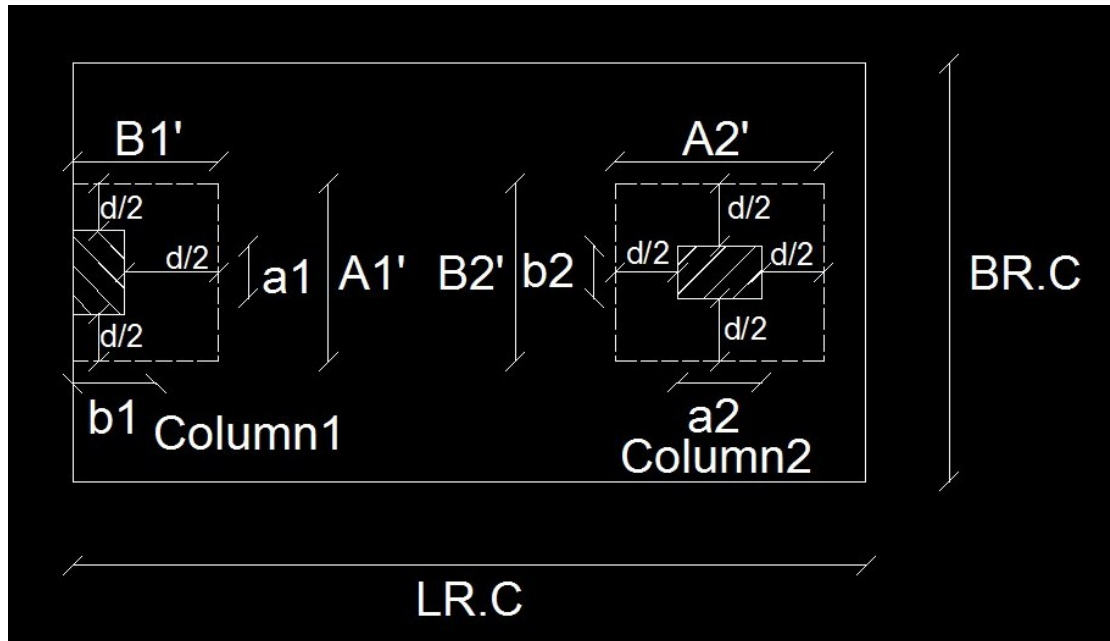
If $q_{pcu} > q_p$ ok safe

If $q_{pcu} < q_p$ un safe \rightarrow increase depth

$$t = d + \text{cover}$$

$$\text{cover} = (5 \text{ to } 10 \text{ cm})$$

الحالة الثانية:



For Column 1:

$$Q_{P1} = P_{u1} - q_U (A_1' * B_1') = \dots \text{Ton}$$

حيث أن :

$$A_1' = (a_1 + d) = \dots \text{m}$$

$$B_1' = (b_1 + \frac{d}{2}) = \dots \text{m}$$

والباقى نفس الشئ

6) Reinforcement of the footing:

in Long Direction:

$$A_{s \text{ Top}} = \frac{M_{\text{max}}}{J * d * F_y} = \dots \text{ cm}^2 / B_{R.C} = \dots \text{ cm}^2 / \text{m}'$$

$$A_{s \text{ min}} = 0.15 * d = \dots \text{ cm}^2 / \text{m}'$$

If $A_{s \text{ Top}} \geq A_{s \text{ min}} \rightarrow \text{ok}$

If $A_{s \text{ Top}} < A_{s \text{ min}} \rightarrow \text{take } A_{s \text{ Top}} = A_{s \text{ min}}$

$$A_{s \text{ Bot}} = \frac{M_{1 \text{ or } M_2}}{J * d * F_y} = \dots \text{ cm}^2 / B_{R.C} = \dots \text{ cm}^2 / \text{m}'$$

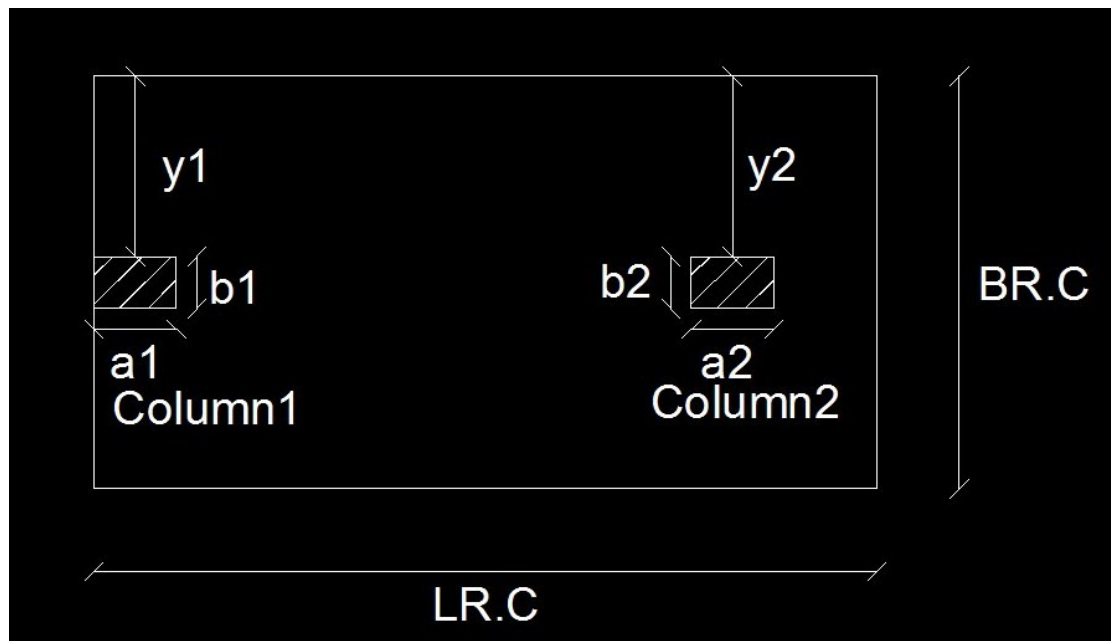
Take Max Moment of M_1 & M_2

$$A_{s \text{ min}} = 0.15 * d = \dots \text{ cm}^2 / \text{m}'$$

If $A_{s \text{ Bot}} \geq A_{s \text{ min}} \rightarrow \text{ok}$

If $A_{s \text{ Bot}} < A_{s \text{ min}} \rightarrow \text{take } A_{s \text{ Bot}} = A_{s \text{ min}}$

In Short Direction:

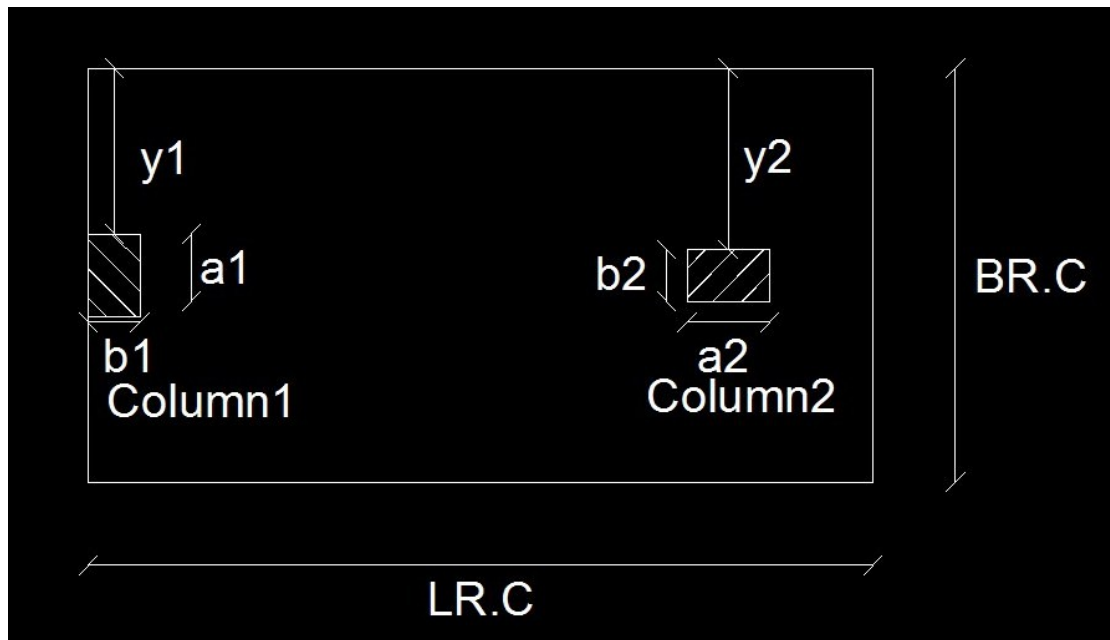


$$M_u = q_{ult} * \frac{(y_{1or2})^2}{2} = \dots \text{ mt}$$

Take y Max of y_1 & y_2

$$Y_1 = \frac{BR.C - b_1}{2} = \dots \text{ m}$$

$$Y_2 = \frac{BR.C - b_2}{2} = \dots \text{ m}$$



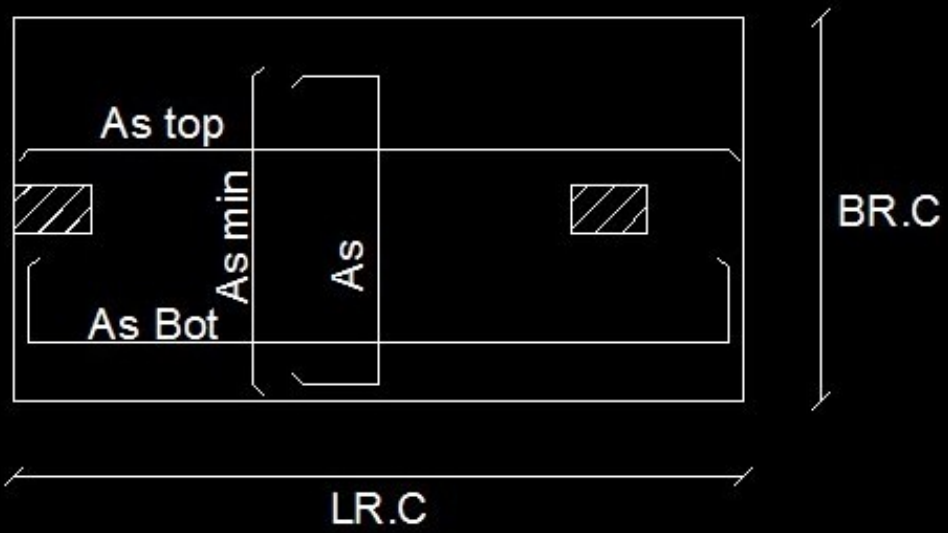
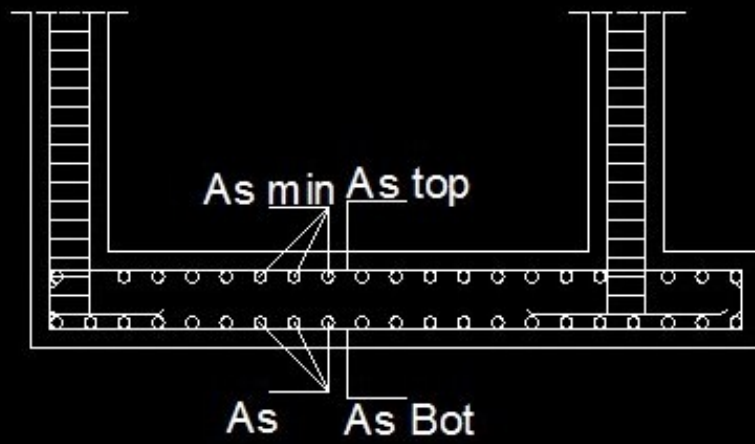
$$Y_1 = \frac{BR.C - a1}{2} = \dots \text{ m}$$

$$Y_2 = \frac{BR.C - b2}{2} = \dots \text{ m}$$

$$A_s = \frac{Mu}{J * d * F_y} = \dots \text{ cm}^2 / \text{m}'$$

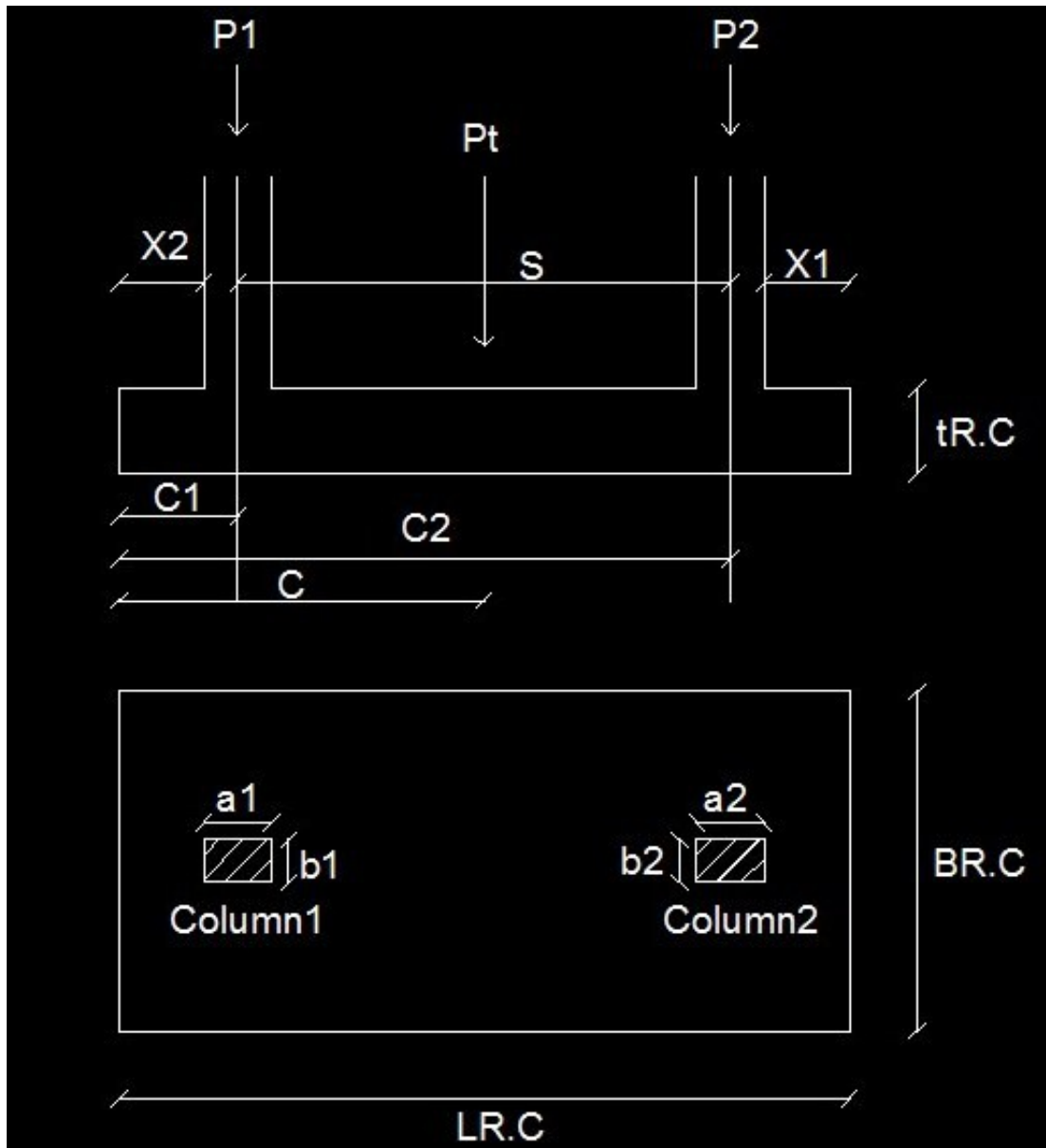
If $A_s \geq A_{s \text{ min}} \rightarrow \text{ok}$

If $A_s < A_{s \text{ min}} \rightarrow \text{take } A_s = A_{s \text{ min}}$



Steps of Design:

1) Dimension of Footing (working Loads):



$$P_t = (P_1 + P_2) * 1.1 = \dots \text{ Ton}$$

$(P_1 + P_2) \rightarrow$ Working Loads حيث أن

Working Loads to ultimate Loads * 1.5

Ultimate Loads to Working Loads / 1.5

$$\text{Area of Footing } (A_{R.C}) = \frac{P_t}{q_{all}} = L * B = m^2$$

Take $C_1 = 1$ m if not given.

$$C_2 = C_1 + S = \dots \text{ m}$$

$$C = \frac{(c_1 * p_1) + (c_2 * p_2)}{p_t} = \dots \text{ m}$$

حيث أن:

$C \rightarrow$ مكان تأثير

$P_t \rightarrow$ محصله القوي

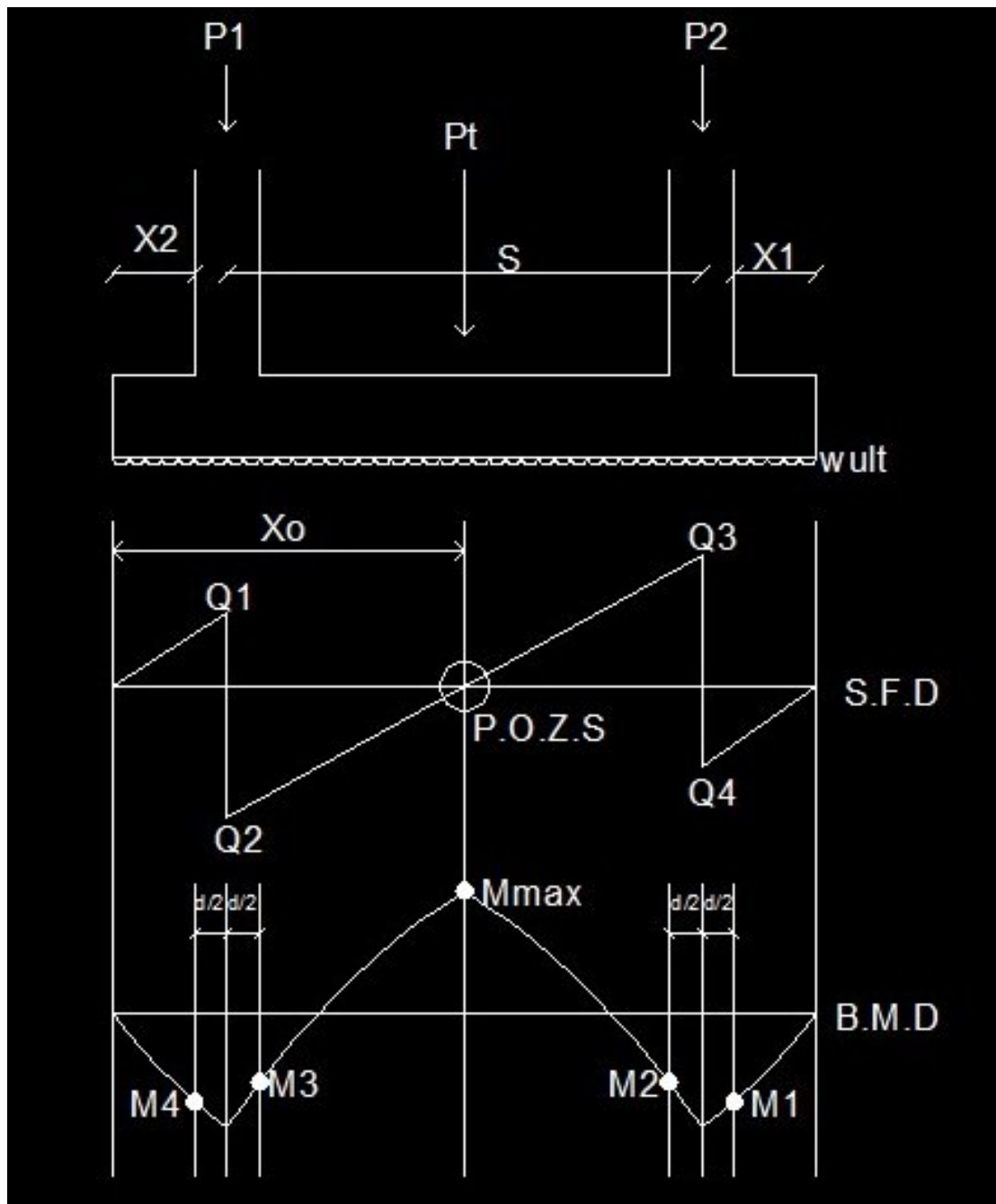
حتى تكون المحصلة في نصف القاعدة

$$L_{R.C} = 2 * C = \dots \text{ m} \cong \text{to nearest 5 cm}$$

$$B_{R.C} = \frac{A_{R.C}}{L_{R.C}} = \dots \text{ m} \cong \text{to nearest 5 cm}$$

End of Working Loads

2) Ultimate stress & Draw B.M.D & S.F.D:



$$q_{ult} = \frac{(p_1 + p_2) * 1.5}{LR.C * BR.C} = \dots \text{ t/m}^2$$

$$W_{ult} = q_{ult} * B_{R.C} = \dots \text{ t/m'}$$

$$Q_1 = W_{ult} * C_1 = \dots \text{ Ton}$$

$$Q_2 = Q_1 - P_{1u} = \dots \text{ Ton}$$

$$Q_3 = W_{ult} * C_2 - P_{1u} = \dots \text{ Ton}$$

$$Q_4 = Q_3 - P_{2u} = \dots \text{ Ton}$$

Moment يحسب عند وش العمود M_1, M_2

Max Moment at point of zero shear

At p.o.z.s

$$X_0 = \frac{P_{1u}}{W_u} = \dots \text{ m}$$

$$X_1 = L_{R.C} - \left(C_2 + \frac{b_2 \text{ or } a_2}{2} \right) = \dots \text{ m}$$

$$X_2 = C_1 - \frac{b_1 \text{ or } a_1}{2} = \dots \text{ m}$$

حيث أن:

مسافة من خط الجار إلي point of zero shear

p.o.z.s → point of zero shear

a → طول العمود

b → عرض العمود

b₂ or a₂ → حسب اتجاه العمود

$$M_1 = W_u * \frac{(X1)^2}{2} = \dots \text{ mt}$$

$$M_2 = W_u * \frac{(X1+a2 \text{ or } b2)^2}{2} - P_{2u} * \frac{a2 \text{ or } b2}{2} = \dots \text{ mt}$$

$$M_4 = W_u * \frac{(X2)^2}{2} = \dots \text{ mt}$$

$$M_3 = W_u * \frac{(X2+a1 \text{ or } b1)^2}{2} - P_{1u} * \frac{a1 \text{ or } b1}{2} = \dots \text{ mt}$$

حيث أن:

a → طول العمود

b → عرض العمود

b2 or a2 → حسب اتجاه العمود

$$M_{\max} = P_{1u} * (X_o - C_1) - (W_u * \frac{(X_o)^2}{2}) = \dots \text{ mt}$$

3) Calculation the Depth:

$$d = c1 \sqrt{\frac{M_u}{F_{cu} * B * R.C}}$$

حيث أن:

c1 → 5

M_u → Max Moment

4) Check shear:

Critical section at $\frac{d}{2}$ من وش العمود

$$Q_{sh} = Q_{Max} - W_u \left(\frac{d}{2} + \frac{a1 \text{ or } a2 \text{ or } b1 \text{ or } b2}{2} \right) = \dots \text{ Ton}$$

حيث أن:

a → طول العمود

b → عرض العمود

Q_{Max} حسب اتجاه العمود → b^2 or a^2 و حسب

$Q_{Max} \rightarrow \text{Max of } Q_1, Q_2, Q_3, Q_4$

$$q_{sh} = \frac{Q_{sh}}{B.R.C * d} = \dots \text{ kg/cm}^2$$

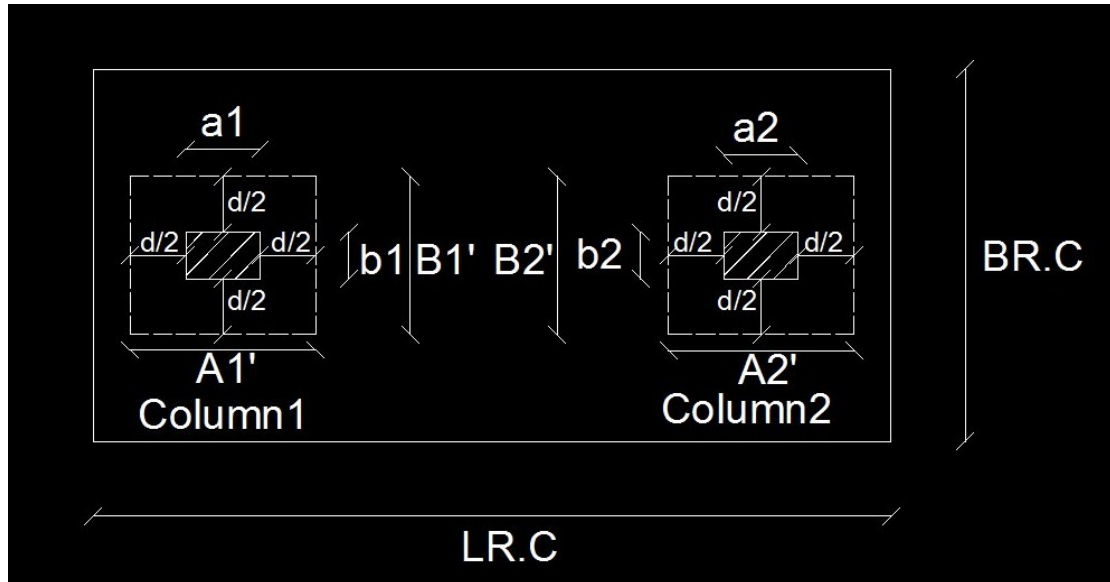
$$q_{cu} = 0.4 * \sqrt{F_{cu}} = \dots \text{ kg/cm}^2$$

If $q_{cu} > q_{sh}$ ok safe

If $q_{cu} < q_{sh}$ un safe increase depth

$$\text{Take } d = \frac{Q_{sh}}{(q_{cu} * B_{R.C})} = \dots \text{ cm}$$

5) Check Punching:



For Column 1:

$$Q_{P1} = P_{u1} - q_U (A_1' * B_1') = \dots \text{ Ton}$$

حيث أن :

$$A_1' = (a_1 + d) = \dots \text{ m}$$

$$B_1' = (b_1 + d) = \dots \text{ m}$$

For Column 2:

$$Q_{P2} = P_{u2} - q_U (A_2' * B_2') = \dots \text{ Ton}$$

حيث أن :

$$A_2' = (a_2 + d) = \dots \text{ m}$$

$$B_2' = (b_2 + d) = \dots \text{ m}$$

$$q_p = \frac{Q_{p\text{Max}}}{2*(A_{1\text{or}2'} + B_{1\text{or}2'})*d} = \dots \text{ kg/cm}^2$$

حيث أن:

$$Q_{p\text{Max}} = \text{Max of } Q_{P1} \text{ \& } Q_{P2}$$

If $Q_{p\text{Max}} \rightarrow Q_{P1}$ Take A_1' , B_1'

If $Q_{p\text{Max}} \rightarrow Q_{P2}$ Take A_2' , B_2'

$$q_{pcu} = \left(0.5 + \frac{b_{1\text{or}2}}{a_{1\text{or}2}}\right) \sqrt{\frac{F_{cu}}{\lambda_c}} = \dots \text{ kg/cm}^2$$

حسب أن:

If $Q_{p\text{Max}} \rightarrow Q_{P1}$ Take b_1 , b_2

If $Q_{p\text{Max}} \rightarrow Q_{P2}$ Take a_1 , a_2

If $q_{pcu} > q_p$ ok safe

If $q_{pcu} < q_p$ un safe \rightarrow increase depth

$$t = d + \text{cover}$$

$$\text{cover} = (5 \text{ to } 10 \text{ cm})$$

6) Reinforcement of the footing:

in Long Direction:

$$A_{s \text{ Top}} = \frac{M_{\text{max}}}{J * d * F_y} = \dots \text{ cm}^2 / B_{\text{R.C}} = \dots \text{ cm}^2 / \text{m}'$$

$$A_{s \text{ min}} = 0.15 * d$$

If $A_{s \text{ Top}} \geq A_{s \text{ min}} \rightarrow \text{ok}$

If $A_{s \text{ Top}} < A_{s \text{ min}} \rightarrow \text{take } A_{s \text{ Top}} = A_{s \text{ min}}$

$$A_{s \text{ Bot}} = \frac{M_1 \text{ or } M_2 \text{ or } M_3 \text{ or } M_4}{J * d * F_y} = \dots \text{ cm}^2 / B_{\text{R.C}} = \dots \text{ cm}^2 / \text{m}'$$

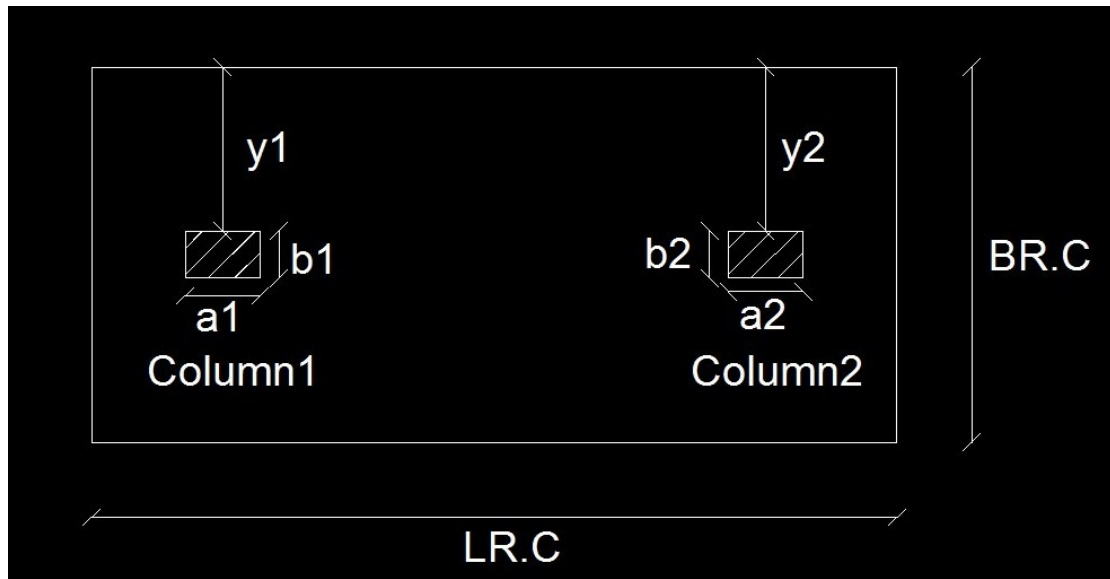
Take Max Moment of M_1 & M_2 & M_3 & M_4

$$A_{s \text{ min}} = 0.15 * d$$

If $A_{s \text{ Bot}} \geq A_{s \text{ min}} \rightarrow \text{ok}$

If $A_{s \text{ Bot}} < A_{s \text{ min}} \rightarrow \text{take } A_{s \text{ Bot}} = A_{s \text{ min}}$

In Short Direction:



$$M_u = q_{ult} * \frac{(y_{1or2})^2}{2} = \dots \text{ mt}$$

Take y Max of y_1 & y_2

$$Y_1 = \frac{BR.C - b_1 \text{ or } a_1}{2} = \dots \text{ m}$$

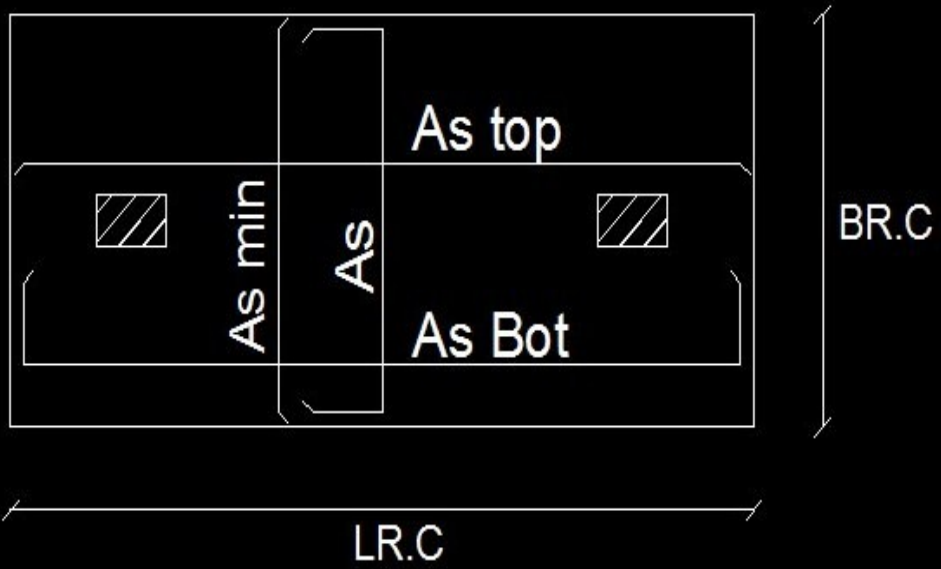
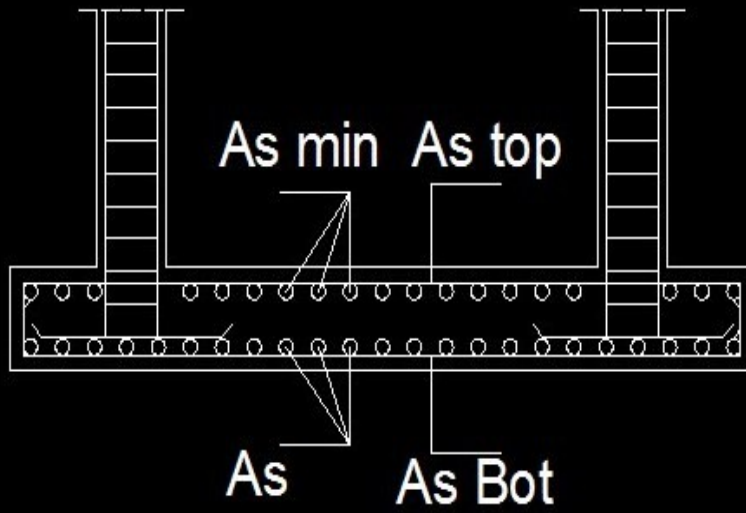
$$Y_2 = \frac{BR.C - b_2 \text{ or } a_2}{2} = \dots \text{ m}$$

$$A_s = \frac{M_u}{J * d * F_y} = \dots \text{ cm}^2 / \text{m}'$$

$$A_{s \text{ min}} = 0.15 * d$$

If $A_s \geq A_{s \text{ min}} \rightarrow \text{ok}$

If $A_s < A_{s \text{ min}} \rightarrow \text{take } A_s = A_{s \text{ min}}$

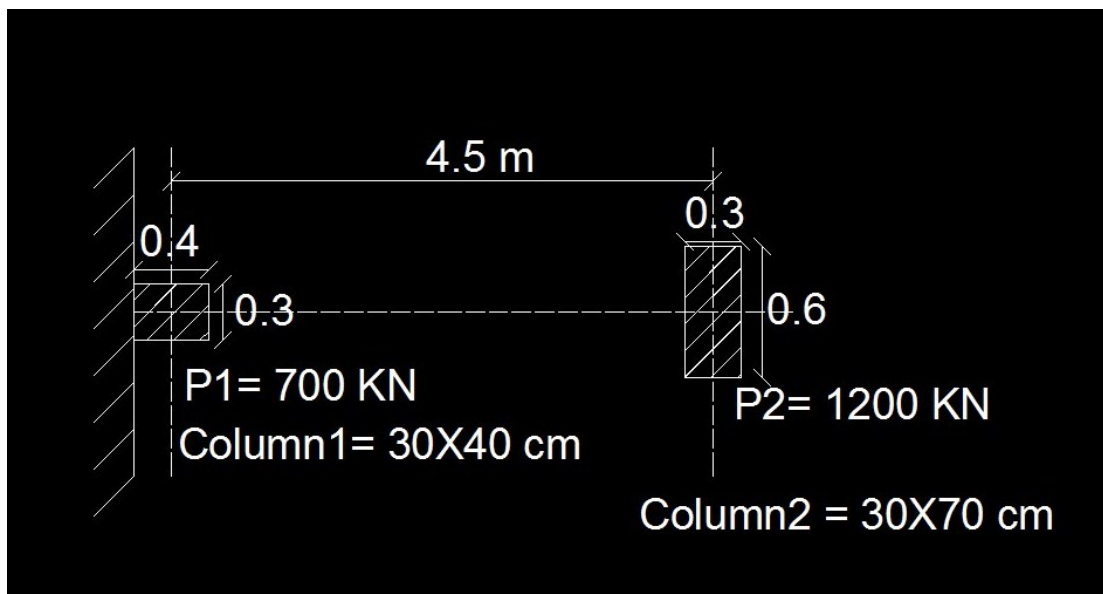


Example: 1

The two column shown in fig are to be supported en a combined footing with the given Dimension.

It is required to:

- 1) Determine the Foundation thickness required to satisfy Max bending Moment and shear.
- 2) Determine the reinforcement steel in both direction.
- 3) Draw net sketch a section elevation and a plan showing concrete dimension and steel details.



Solution

Given: $f_{cu} = 250$ kg/cm², $q_{all} = 150$ kN / m²,

$F_y = 3600$ kg/cm², Foundation depth = 2m

$$P_1 = 700 \text{ KN} = 70 \text{ Ton}$$

$$P_2 = 1200 \text{ KN} = 120 \text{ Ton}$$

$$P_t = 190 \text{ Ton}$$

$$P_{1u} = 70 * 1.5 = 105 \text{ Ton}$$

$$P_{2u} = 120 * 1.5 = 180 \text{ Ton}$$

$$q_{all} = 150 \text{ kN / m}^2 = 15 \text{ t / m}^2$$

1) Dimension of Footing:

$$P_t = (P_1 + P_2) * 1.1 = (70 + 120) * 1.1 = 209 \text{ Ton}$$

$$A_{R.C} = \frac{P_t}{q_{all}} = \frac{209}{15} = 13.93 \text{ m}^2$$

$$C_1 = 0.2 \text{ m}$$

$$C_2 = C_1 + S = 0.2 + 4.5 = 4.7 \text{ m}$$

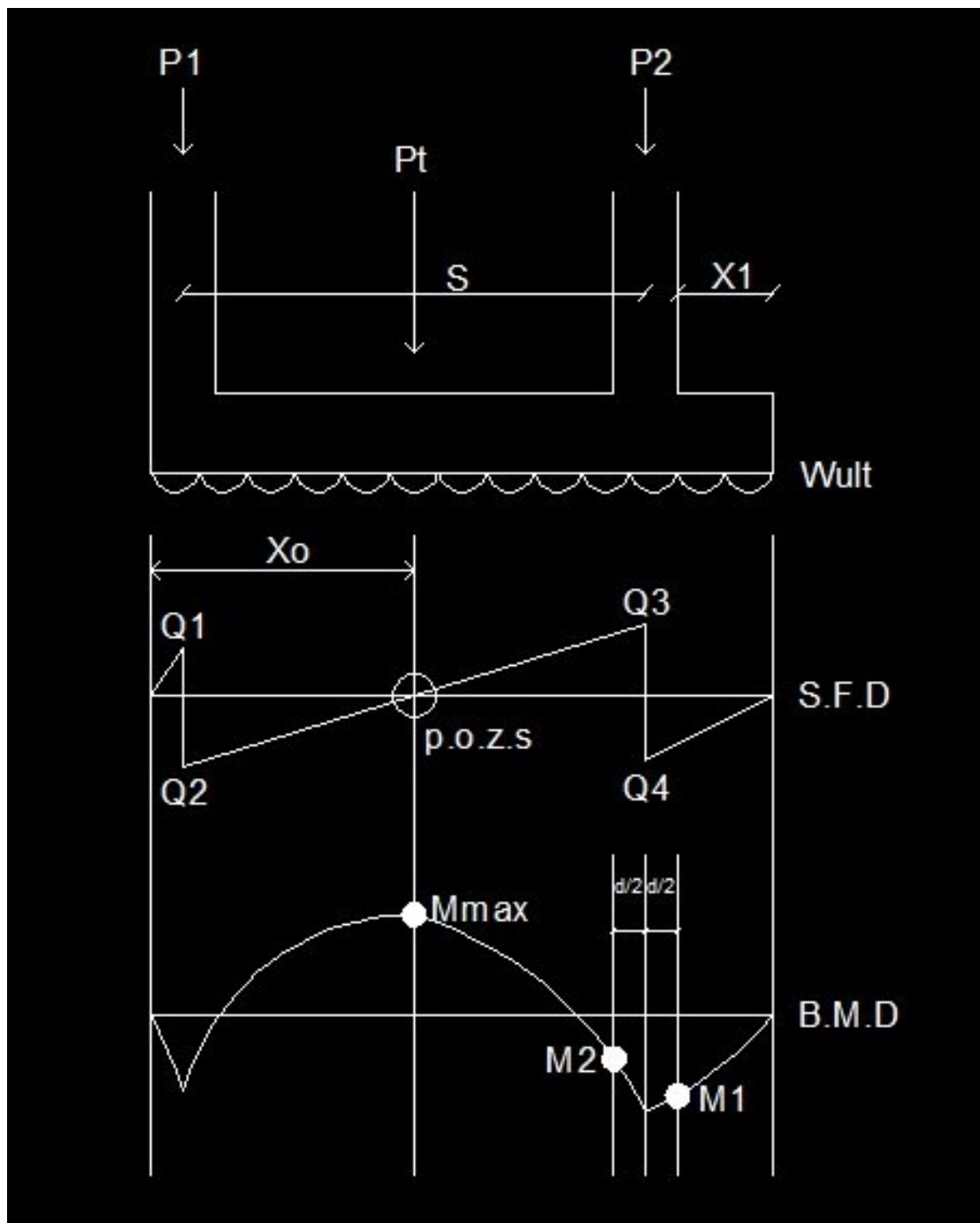
$$C = \frac{(c_1 * p_1) + (c_2 * p_2)}{p_t} = \frac{(0.2 * 70) + (4.7 * 120)}{190} = 3 \text{ m}$$

$$L_{R.C} = 2 * C = 2 * 3 = 6 \text{ m}$$

$$B_{R.C} = \frac{A_{R.C}}{L_{R.C}} = \frac{13.93}{6} = 2.32 \text{ m} \cong 2.35 \text{ m}$$

End of Working Loads

2) Ultimate stress & Draw B.M.D & S.F.D:



$$q_{ult} = \frac{(p1+p2)*1.5}{LR.C*BR.C} = \frac{(70+120)*1.5}{6*2.35} = 20.21 \text{ t/m}^2$$

$$W_{ult} = q_{ult} * B_{R.C} = 20.21 * 2.35 = 47.5 \text{ t/m'}$$

$$Q_1 = W_{ult} * C_1 = 47.5 * 0.2 = 9.5 \text{ Ton}$$

$$Q_2 = Q_1 - P_{1u} = 9.5 - 105 = 95.5 \text{ Ton}$$

$$Q_3 = W_{ult} * C_2 - P_{1u} = 47.5 * 4.7 - 105 = 118.25 \text{ Ton}$$

$$Q_4 = Q_3 - P_{2u} = 118.25 - 180 = 61.75 \text{ Ton}$$

$$X_1 = L_{R.C} - (C_2 + \frac{b_2}{2}) = 6 - (4.7 + \frac{0.3}{2}) = 1.15 \text{ m}$$

$$M_1 = W_u * \frac{(X_1)^2}{2} = 47.5 * \frac{(1.15)^2}{2} = 31.4 \text{ mt}$$

$$M_2 = W_u * \frac{(X_1 + b_2)^2}{2} - P_{2u} * \frac{b_2}{2} = 47.5 * \frac{(1.15 + 0.3)^2}{2} - 180 * \frac{0.3}{2} = 23 \text{ mt}$$

At p.o.z.s

$$X_o = \frac{P_{1u}}{W_u} = \frac{105}{47.5} = 2.2 \text{ m}$$

$$M_{max} = P_{1u} * (X_o - C_1) - (W_u * \frac{(X_o)^2}{2}) = 105 * (2.2 - 0.2) - (47.5 * \frac{(2.2)^2}{2}) = 95.1 \text{ mt}$$

3) Calculation the Depth:

$$d = c1 \sqrt{\frac{Mu}{Fcu * BR.C}} = 5 \sqrt{\frac{95.1 * 10^5}{250 * 235}} = 63.6 \text{ cm} \cong 70 \text{ cm}$$

4) Check shear:

$$Q_{sh} = Q_{Max} - W_u \left(\frac{d}{2} + \frac{b2}{2} \right) = 118.25 - 47.5 \left(\frac{0.7}{2} + \frac{0.3}{2} \right) \\ = 94.5 \text{ Ton}$$

$$q_{sh} = \frac{Q_{sh}}{BR.C * d} = \frac{94.5 * 10^3}{235 * 70} = 5.7 \text{ kg/cm}^2$$

$$q_{cu} = 0.4 * \sqrt{Fcu} = 0.4 * \sqrt{250} = 6.3 \text{ kg/cm}^2$$

$$q_{cu} > q_{sh}$$

6.3 > 5.7 ok safe

5) Check Punching:

For Column 1:

$$Q_{P1} = P_{u1} - q_U (A_1' * B_1')$$

$$A_1' = (a_1 + \frac{d}{2}) = (0.4 + \frac{0.7}{2}) = 0.75 \text{ m}$$

$$B_1' = (b_1 + d) = (0.3 + 0.7) = 1 \text{ m}$$

$$Q_{P1} = 105 - 20.21(0.75 * 1) = 90 \text{ Ton}$$

For Column 2:

$$Q_{P2} = P_{u2} - q_U (A_2' * B_2')$$

$$A_2' = (a_2 + d) = (0.6 + 0.7) = 1.3 \text{ m}$$

$$B_2' = (b_2 + d) = (0.3 + 0.7) = 1 \text{ m}$$

$$Q_{P2} = 180 - 20.21 (1.3 * 1) = 154 \text{ Ton}$$

$$q_p = \frac{Q_{p2}}{2 * (A_2' + B_2') * d} = \frac{154 * 10^3}{2 * (1.3 + 1) * 0.7} = 4.8 \text{ kg/cm}^2$$

$$q_{pcu} = (0.5 + \frac{b_2}{a_2}) \sqrt{\frac{F_{cu}}{\lambda c}}$$
$$= (0.5 + \frac{0.3}{0.6}) \sqrt{\frac{250}{1.5}} = 12.9 \text{ kg/cm}^2$$

$$q_{pcu} > q_p$$

$$12.9 > 4.8 \text{ ok safe}$$

$$t = d + \text{cover} = 70 + 10 = 80 \text{ cm}$$

6) Reinforcement of the footing:

in Long Direction:

$$\begin{aligned} A_{s \text{ Top}} &= \frac{M_{\max}}{J \cdot d \cdot F_y} = \dots \text{ cm}^2 / B_{R.C} = \text{ cm}^2 / \text{m}' \\ &= \frac{95.1 \cdot 10^5}{0.826 \cdot 70 \cdot 3600} = 45.7 / 2.35 = 19.4 \text{ cm}^2 / \text{m}' \end{aligned}$$

$$A_{s \text{ min}} = 0.15 \cdot d = 0.15 \cdot 70 = 10.5 \text{ cm}^2 / \text{m}'$$

$$A_{s \text{ Top}} \geq A_{s \text{ min}} \rightarrow \text{ok}$$

$$\text{Take } A_{s \text{ Top}} = 19.4 \text{ cm}^2 / \text{m}'$$

Use 6y22/m'

$$\begin{aligned} A_{s \text{ Bot}} &= \frac{M_1}{J \cdot d \cdot F_y} = \dots \text{ cm}^2 / B_{R.C} = \dots \text{ cm}^2 / \text{m}' \\ &= \frac{31.4 \cdot 10^5}{0.826 \cdot 70 \cdot 3600} = 15.1 / 2.35 = 6.4 \text{ cm}^2 / \text{m}' \end{aligned}$$

$$A_{s \text{ min}} = 0.15 \cdot d = 0.15 \cdot 70 = 10.5 \text{ cm}^2 / \text{m}'$$

$$A_{s \text{ Bot}} < A_{s \text{ min}} \rightarrow \text{take } A_{s \text{ Bot}} = A_{s \text{ min}}$$

take $A_{s \text{ Bot}} = 10.5 \text{ cm}^2 / \text{m}'$

Use 6y16/m'

In Short Direction:

$$M_u = q_{\text{ult}} * \frac{(y_1)^2}{2} = \dots \text{ mt}$$

$$Y_1 = \frac{\text{BR.C} - b_1}{2} = \frac{2.35 - 0.3}{2} = 1.025 \text{ m}$$

$$Y_2 = \frac{\text{BR.C} - a_2}{2} = \frac{2.35 - 0.6}{2} = 0.875 \text{ m}$$

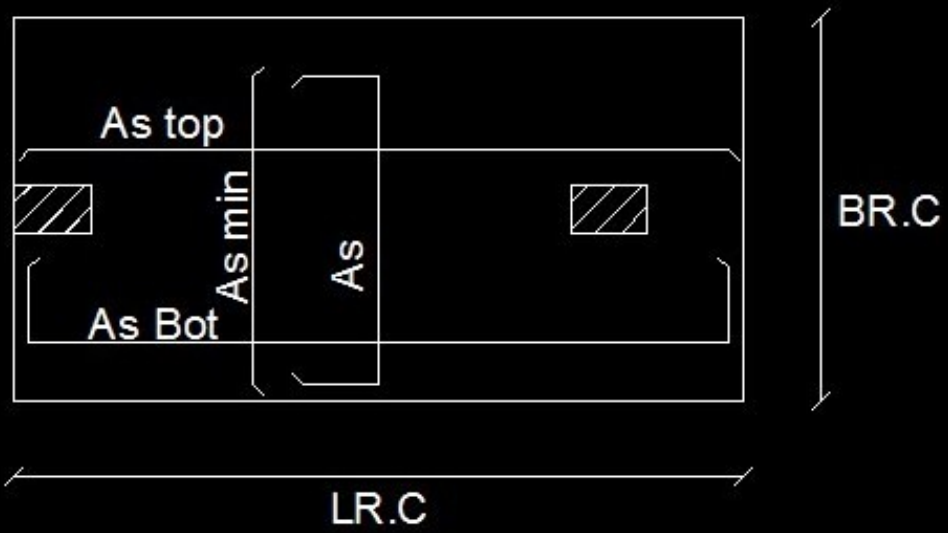
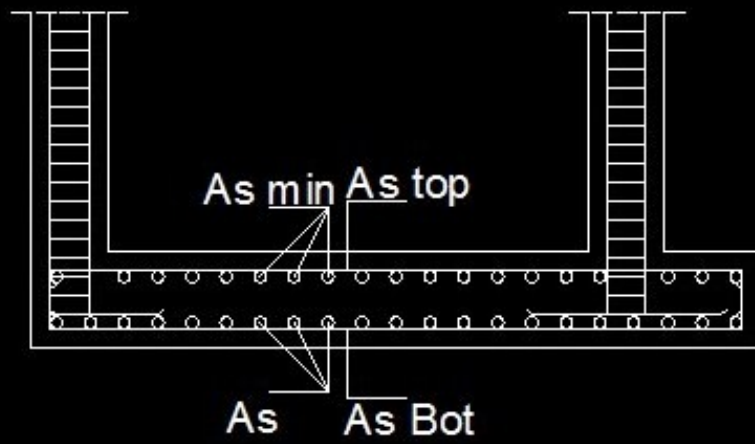
$$M_u = q_{\text{ult}} * \frac{(y_1)^2}{2} = 20.21 * \frac{(1.025)^2}{2} = 10.62 \text{ mt}$$

$$A_s = \frac{M_u}{J * d * F_y} = \frac{10.62 * 10^5}{0.826 * 70 * 3600} = 5.1 \text{ cm}^2 / \text{m}'$$

$A_s < A_{s \text{ min}} \rightarrow \text{take } A_s = A_{s \text{ min}}$

take $A_s = 10.5 \text{ cm}^2 / \text{m}'$

Use 6y16/m'

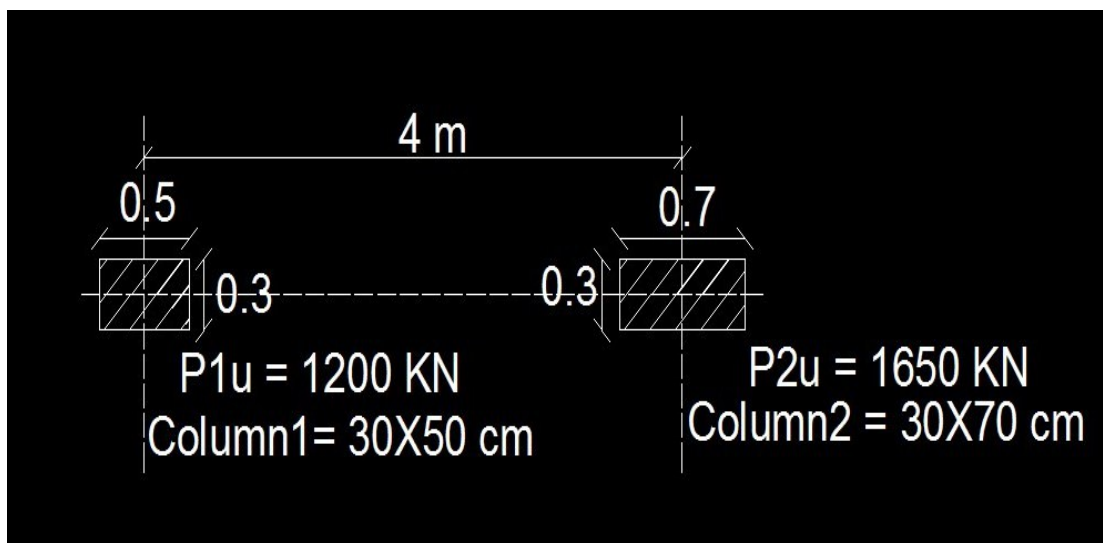


Example: 2

The two interior column shown in fig are to be supported on a combined footing with the given Dimension.

It is required to:

- 1) Determine the Foundation thickness required to satisfy Max bending Moment and shear.
- 2) Determine the reinforcement steel in both direction.
- 3) Draw net sketch a section elevation and a plan showing concrete dimension and steel details.



Solution

Given: $f_{cu} = 200 \text{ kg/cm}^2$, $q_{all} = 120 \text{ kN / m}^2$,

$F_y = 3600 \text{ kg/cm}^2$, Foundation depth = 2m

$$P_{1u} = 1200 \text{ KN} = 120 \text{ Ton}$$

$$P_{2u} = 1650 \text{ KN} = 165 \text{ Ton}$$

$$P_{tu} = 285 \text{ Ton}$$

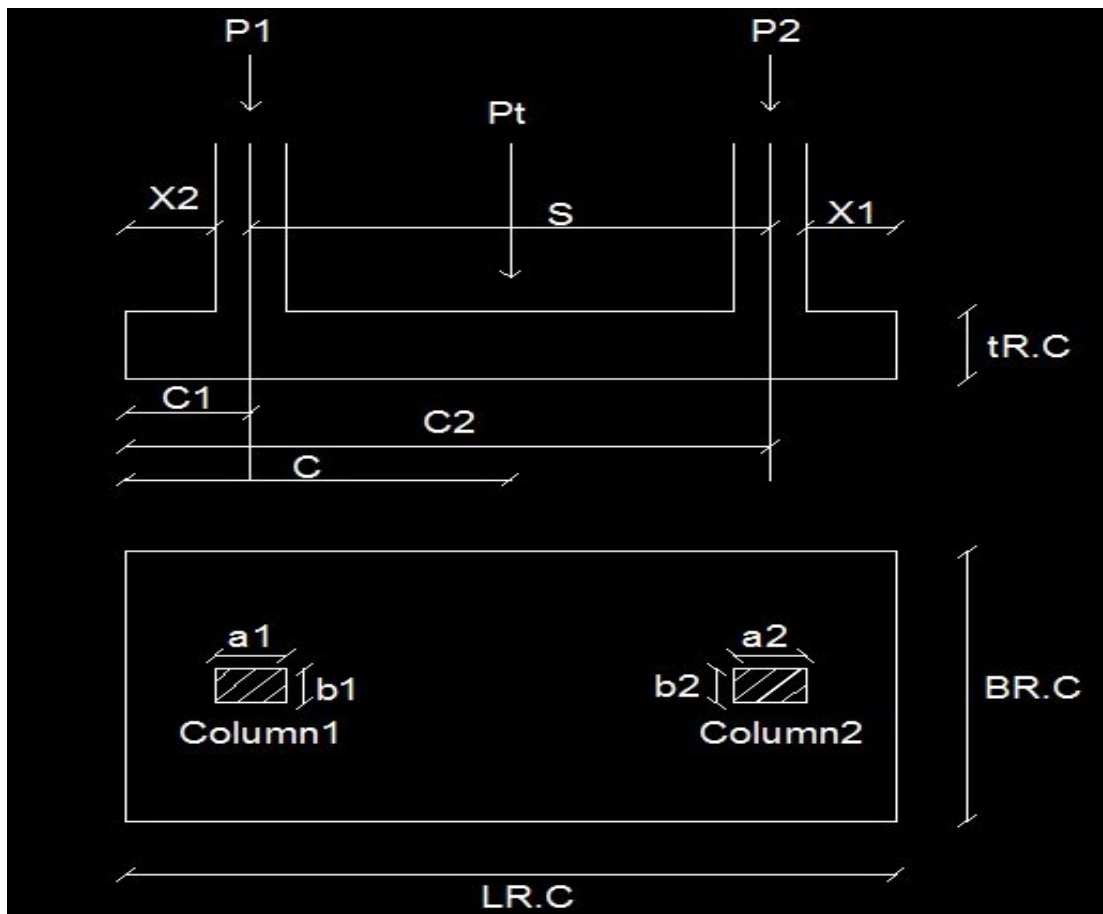
$$P_{1w} = \frac{P_{1u}}{1.5} = \frac{120}{1.5} = 80 \text{ Ton}$$

$$P_{2w} = \frac{P_{2u}}{1.5} = \frac{165}{1.5} = 110 \text{ Ton}$$

$$P_{tw} = 80 + 110 = 190 \text{ Ton}$$

$$q_{all} = 120 \text{ kN / m}^2 = 12 \text{ t / m}^2$$

1) Dimension of Footing (working Loads):



$$P_t = (P_1 + P_2) * 1.1 = (80 + 110) * 1.1 = 209 \text{ Ton}$$

$$A_{R.C} = \frac{P_t}{q_{all}} = \frac{209}{12} = 17.4 \text{ m}^2$$

$$\text{Take } C_1 = 1 \text{ m}$$

$$C_2 = C_1 + S = 1 + 4 = 5 \text{ m}$$

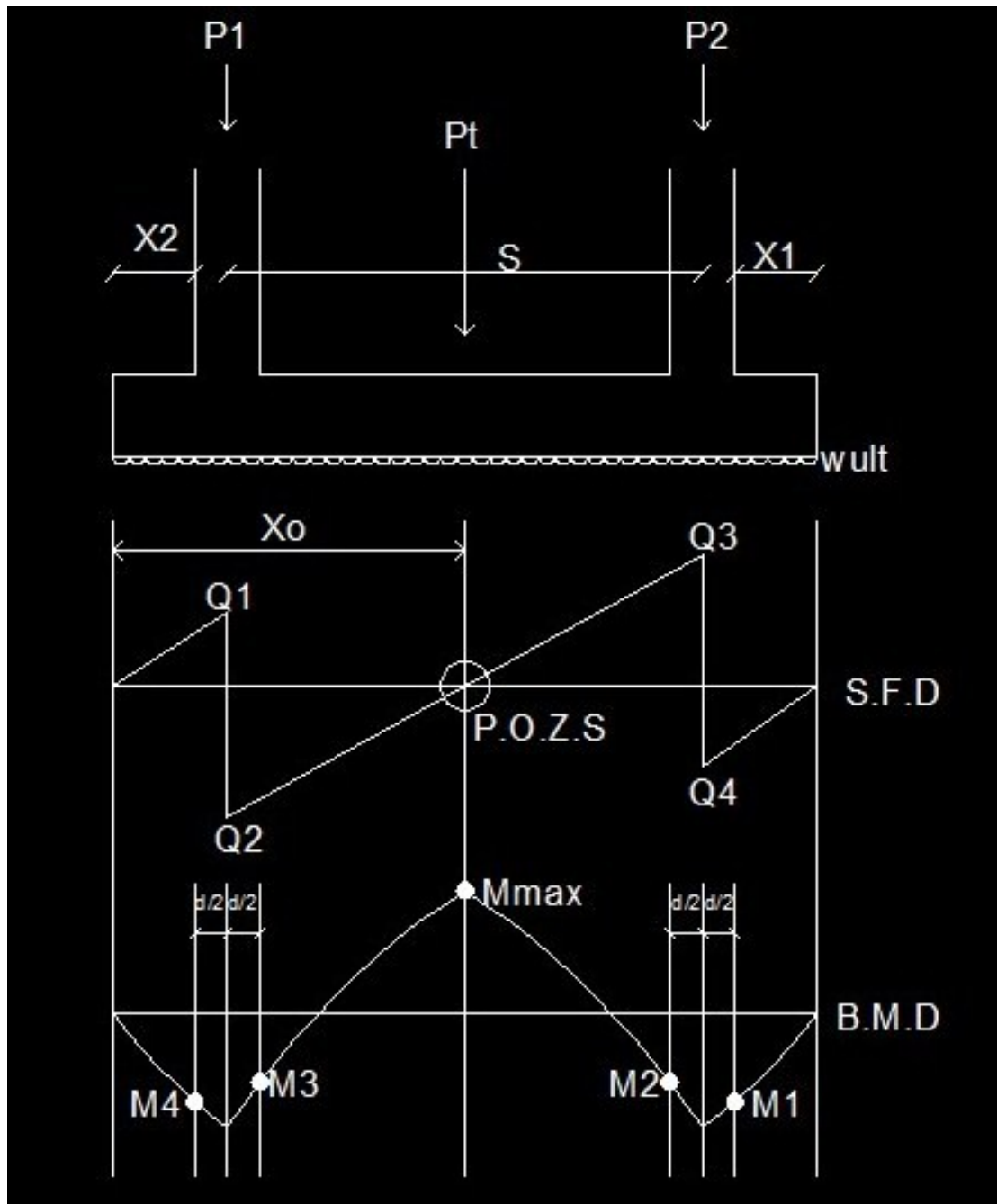
$$C = \frac{(c_1 * p_1) + (c_2 * p_2)}{p_t} = \frac{(1 * 80) + (5 * 110)}{190} = 3.3 \text{ m}$$

$$L_{R.C} = 2 * C = 2 * 3.3 = 6.6 \text{ m}$$

$$B_{R.C} = \frac{A_{R.C}}{L_{R.C}} = \frac{17.4}{6.6} = 2.64 \text{ m} \cong 2.7 \text{ m}$$

End of Working Loads

2) Ultimate stress & Draw B.M.D & S.F.D:



$$q_{ult} = \frac{(p_1 + p_2)}{LR.C * BR.C} = \frac{(120 + 165)}{6.6 * 2.7} = 16 \text{ t/m}^2$$

$$W_{ult} = q_{ult} * B_{R.C} = 16 * 2.7 = 43.2 \text{ t/m'}$$

$$Q_1 = W_{ult} * C_1 = 43.2 * 1 = 43.3 \text{ Ton}$$

$$Q_2 = Q_1 - P_{1u} = 43.2 - 120 = 76.8 \text{ Ton}$$

$$Q_3 = W_{ult} * C_2 - P_{1u} = 43.2 * 5 - 120 = 96 \text{ Ton}$$

$$Q_4 = Q_3 - P_{2u} = 96 - 165 = 69 \text{ Ton}$$

$$X_1 = L_{R.C} - \left(C_2 + \frac{a_2}{2} \right) = 6.6 - \left(5 + \frac{0.7}{2} \right) = 1.25 \text{ m}$$

$$X_2 = C_1 - \frac{a_1}{2} = 1 - \frac{0.5}{2} = 0.75 \text{ m}$$

$$M_1 = W_u * \frac{(X_1)^2}{2} = 43.2 * \frac{(1.25)^2}{2} = 33.75 \text{ mt}$$

$$\begin{aligned} M_2 &= W_u * \frac{(X_1 + a_2)^2}{2} - P_{2u} * \frac{a_2}{2} \\ &= 43.2 * \frac{(1.25 + 0.7)^2}{2} - 165 * \frac{0.7}{2} = 24.38 \text{ mt} \end{aligned}$$

$$M_4 = W_u * \frac{(X_2)^2}{2} = 43.2 * \frac{(0.75)^2}{2} = 12.15 \text{ mt}$$

$$\begin{aligned} M_3 &= W_u * \frac{(X_2 + a_1)^2}{2} - P_{1u} * \frac{a_1}{2} \\ &= 43.2 * \frac{(0.75 + 0.5)^2}{2} - 120 * \frac{0.5}{2} = 3.75 \text{ mt} \end{aligned}$$

At p.o.z.s

$$X_o = \frac{P_{1u}}{W_u} = \frac{120}{43.2} = 2.78 \text{ m}$$

$$M_{\max} = P_{1u} * (X_o - C_1) - (W_u * \frac{(X_o)^2}{2}) = \dots \text{ mt}$$

$$= 120 * (2.78 - 1) - (43.2 * \frac{(2.78)^2}{2}) = 46.7 \text{ mt}$$

3) Calculation the Depth:

$$d = c1 \sqrt{\frac{Mu}{Fcu * BR.C}} = 5 \sqrt{\frac{46.7 * 10^5}{200 * 270}} = 46.5 \cong 50 \text{ cm}$$

4) Check shear:

$$Q_{sh} = Q_{\max} - W_u \left(\frac{d}{2} + \frac{a_2}{2} \right) = \dots \text{ Ton}$$

$$= 96 - 43.2 \left(\frac{0.5}{2} + \frac{0.7}{2} \right) = 70 \text{ Ton}$$

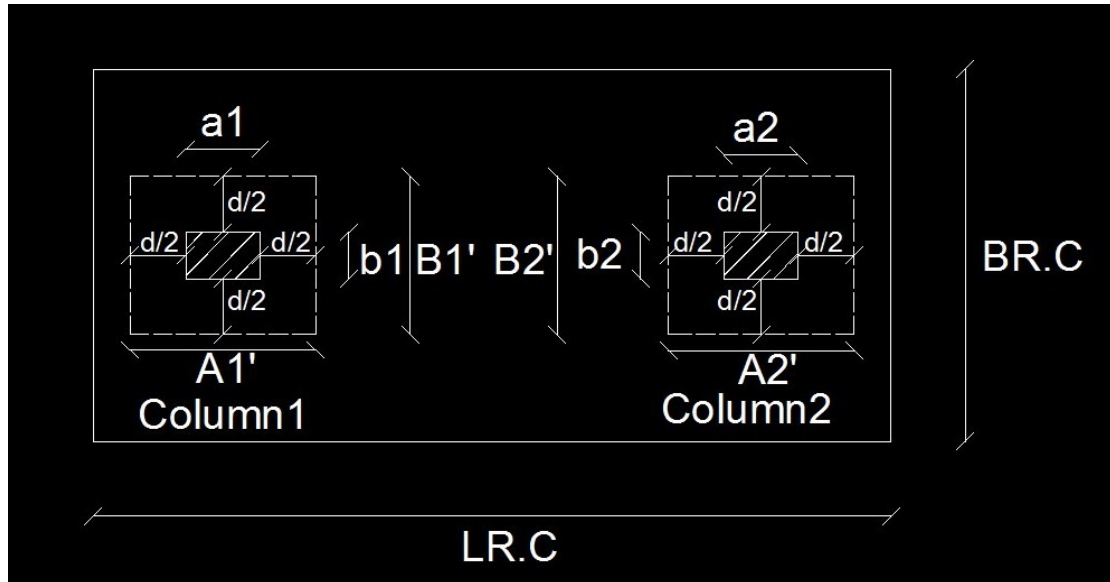
$$q_{sh} = \frac{Q_{sh}}{BR.C * d} = \frac{70 * 10^3}{270 * 50} = 5.18 \text{ kg/cm}^2$$

$$q_{cu} = 0.4 * \sqrt{Fcu} = 0.4 * \sqrt{200} = 5.66 \text{ kg/cm}^2$$

$$q_{cu} > q_{sh}$$

5.66 > 5.18 ok safe

5) Check Punching:



For Column 1:

$$Q_{P1} = P_{u1} - q_U (A_1' * B_1')$$

$$A_1' = (a_1 + d) = (0.5 + 0.5) = 1 \text{ m}$$

$$B_1' = (b_1 + d) = (0.3 + 0.5) = 0.8 \text{ m}$$

$$Q_{P1} = 120 - 16(1 * 0.8) = 107.2 \text{ Ton}$$

For Column 2:

$$Q_{P2} = P_{u2} - q_U (A_2' * B_2')$$

$$A_2' = (a_2 + d) = (0.7 + 0.5) = 1.2 \text{ m}$$

$$B_2' = (b_2 + d) = (0.3 + 0.5) = 0.8 \text{ m}$$

$$Q_{p2} = 165 - 16 (1.2 * 0.8) = 149.64 \text{ Ton}$$

$$q_p = \frac{Q_{p2}}{2 * (A2' + B2') * d} = \frac{149.64 * 10^3}{2 * (120 + 80) * 50} = 7.48 \text{ kg/cm}^2$$

$$q_{pcu} = \left(0.5 + \frac{b2}{a2} \right) \sqrt{\frac{Fcu}{\lambda c}}$$
$$= \left(0.5 + \frac{0.3}{0.7} \right) \sqrt{\frac{200}{1.5}} = 10.7 \text{ kg/cm}^2$$

$$q_{pcu} > q_p$$

10.7 > 7.48 ok safe

$$t = d + \text{cover} = 50 + 10 = 60 \text{ cm}$$

6) Reinforcement of the footing:

in Long Direction:

$$A_{s \text{ Top}} = \frac{M_{\text{max}}}{J \cdot d \cdot F_y} = \dots \text{ cm}^2 / B_{R.C} = \dots \text{ cm}^2 / \text{m}'$$
$$= \frac{46.7 \cdot 10^5}{0.826 \cdot 50 \cdot 3600} = 31.41 / 2.7 = 11.63 \text{ cm}^2 / \text{m}'$$

$$A_{s \text{ min}} = 0.15 \cdot d = 0.15 \cdot 50 = 7.5 \text{ cm}^2 / \text{m}'$$

$$A_{s \text{ Top}} \geq A_{s \text{ min}} \rightarrow \text{ok}$$

$$\text{take } A_{s \text{ Top}} = 11.63 \text{ cm}^2 / \text{m}'$$

Use 6y 16 / m'

$$A_{s \text{ Bot}} = \frac{M_1}{J \cdot d \cdot F_y} = \dots \text{ cm}^2 / B_{R.C} = \dots \text{ cm}^2 / \text{m}'$$
$$= \frac{33.75 \cdot 10^5}{0.826 \cdot 50 \cdot 3600} = 23 \text{ cm}^2 / 2.7 = 8.5 \text{ cm}^2 / \text{m}'$$

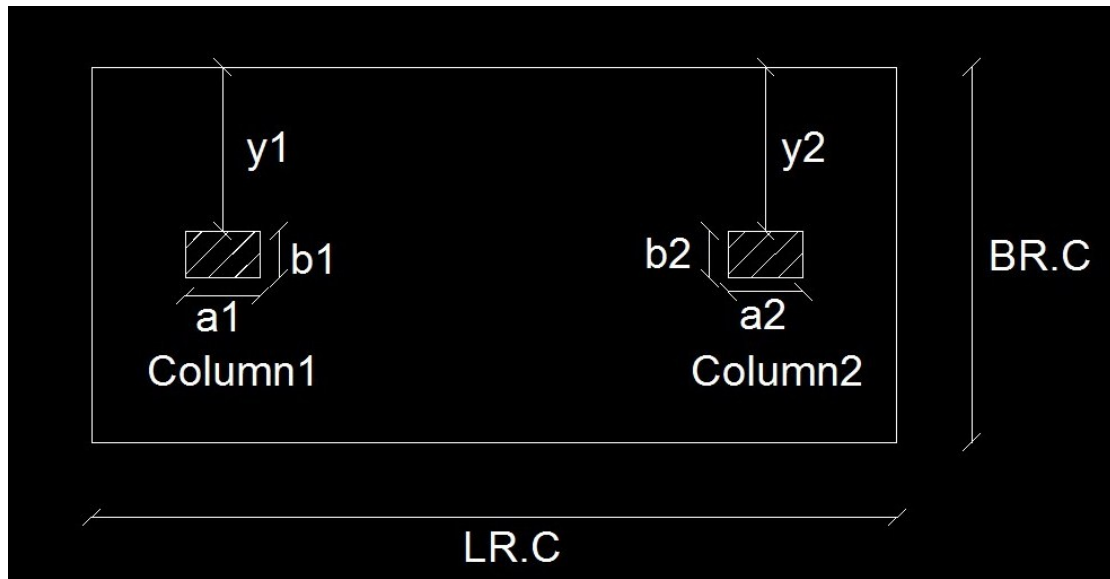
$$A_{s \text{ min}} = 0.15 \cdot d = 0.15 \cdot 50 = 7.5 \text{ cm}^2 / \text{m}'$$

$$A_{s \text{ Bot}} \geq A_{s \text{ min}} \rightarrow \text{ok}$$

$$\text{take } A_{s \text{ Bot}} = 8.5 \text{ cm}^2 / \text{m}'$$

Use 8y 12 / m'

In Short Direction:



$$M_u = q_{ult} * \frac{(y1 \text{ or } 2)^2}{2}$$

$$Y_1 = \frac{BR.C - b1}{2} = \frac{2.7 - 0.3}{2} = 1.2 \text{ m}$$

$$Y_2 = \frac{BR.C - b2}{2} = \frac{2.7 - 0.3}{2} = 1.2 \text{ m}$$

$$M_u = 16 * \frac{(1.2)^2}{2} = 11.52 \text{ mt}$$

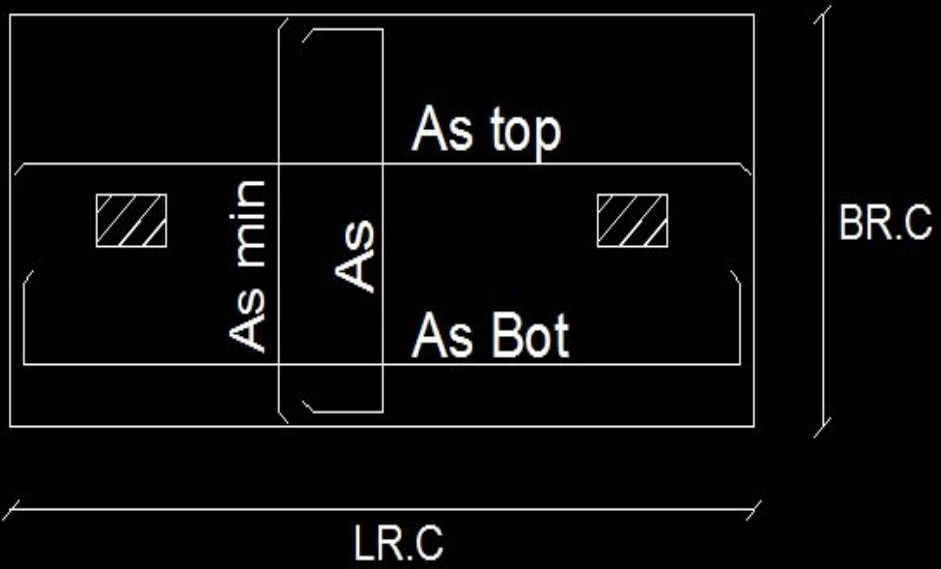
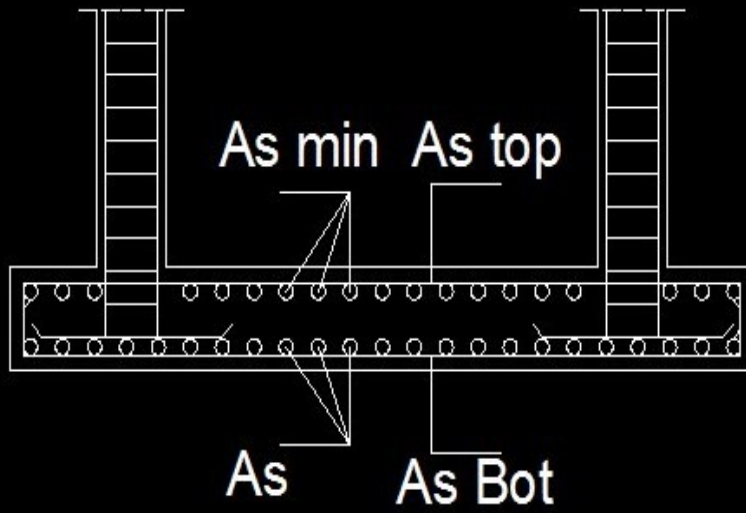
$$A_s = \frac{M_u}{J * d * F_y} = \frac{11.52 * 10^5}{0.826 * 50 * 3600} = 7.75 \text{ cm}^2 / \text{m}'$$

$$A_{s \text{ min}} = 0.15 * d = 0.15 * 50 = 7.5 \text{ cm}^2 / \text{m}'$$

$$A_s \geq A_{s \text{ min}} \rightarrow \text{ok}$$

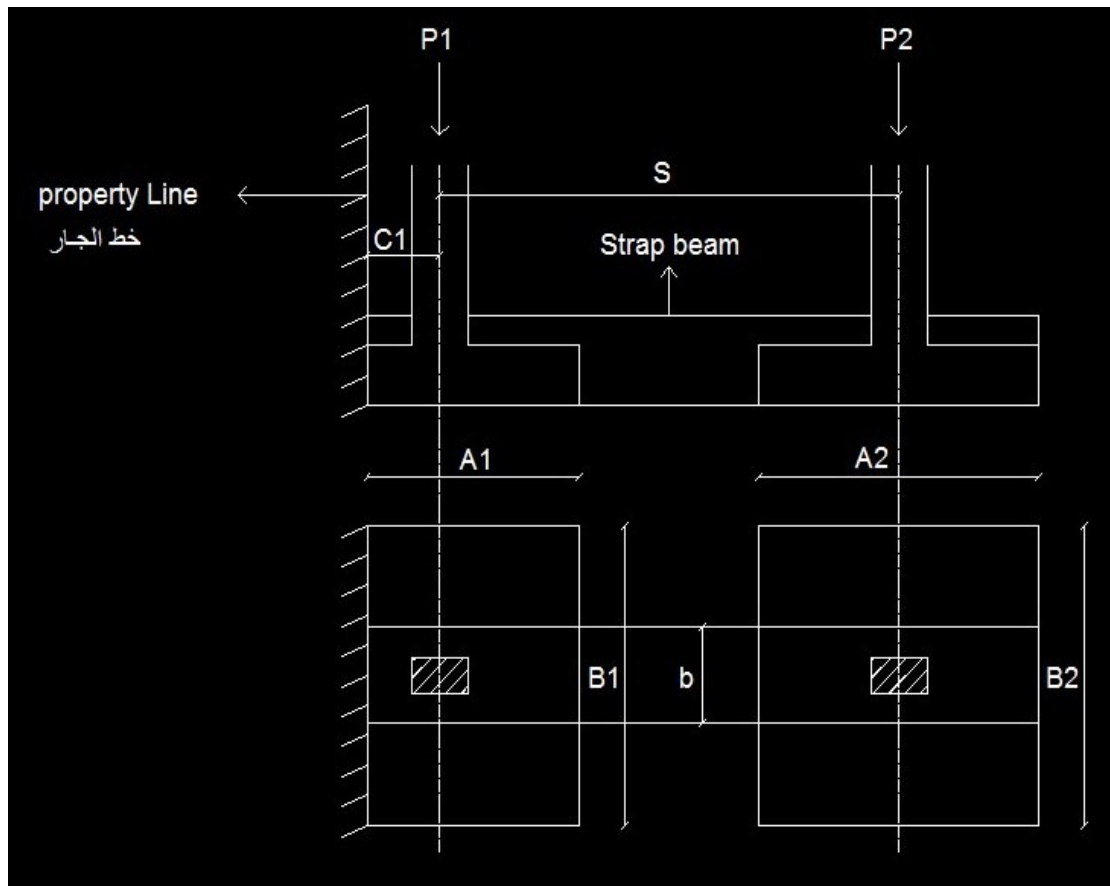
$$\text{take } A_s = 7.75 \text{ cm}^2 / \text{m}'$$

Use 8y 12 / m'



Steps of Design:

1) Dimension of Footing:



$$P_{t1} = 1.2 * P_1 = \dots \text{ton}$$

$$P_{t2} = P_2 = \dots \text{ton}$$

حيث أن:

P_2 و $P_1 \rightarrow$ Working Loads

Take $t_{p.c} = 30 \text{ cm}$

Area of Footing (1):

$$A_{f1} = \frac{Pt1}{q_{all}} = \dots m^2 \rightarrow A_1, B_1$$

حيث أن:

$A_1 \rightarrow$ العرض (البعد الأصغر)

$B_1 \rightarrow$ الطول (البعد الأكبر)

Area of Footing (2):

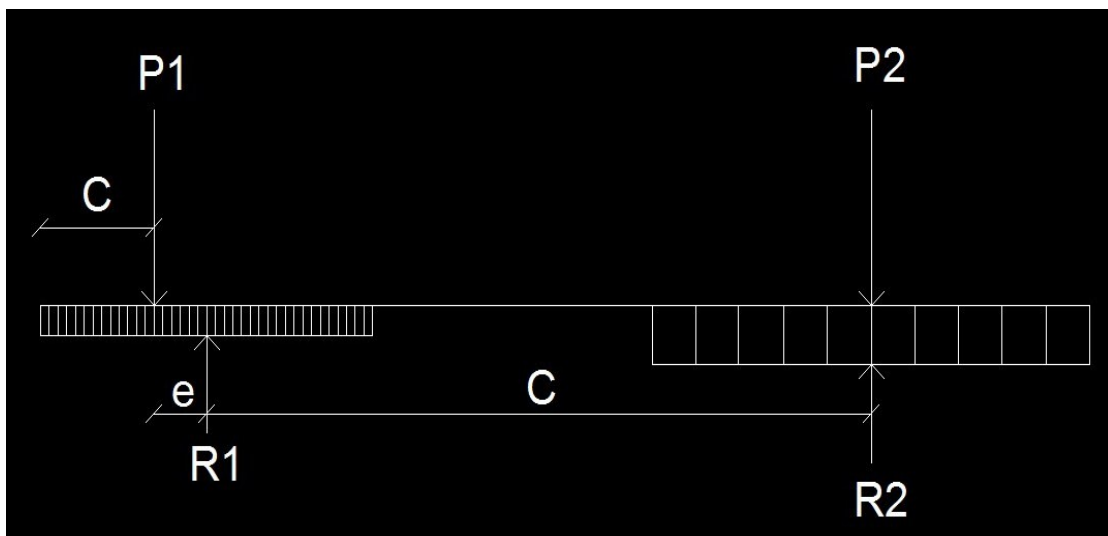
$$A_{f2} = \frac{Pt2}{q_{all}} = \dots m^2 \rightarrow A_2, B_2$$

حيث أن:

$A_2 \rightarrow$ العرض أو الطول حسب وضع العمود

$B_2 \rightarrow$ العرض أو الطول حسب وضع العمود

2) Determination of eccentricity:



نلاحظ أن:

القاعدة الثانية مرتكزة مع العمود فتكون محصلة إجهاد التربة في نفس مكان تأثير حمل العمود.

القاعدة الأولى غير مرتكزة مع العمود ويوجد ترحيل بين P_1 و R_1 .

$$e = \frac{A_1}{2} - C_1 = \dots \text{ m}$$

$$C = s - e = \dots \text{ m}$$

3) Check Area:

$$R_{1u} = P_1 + P_1 * \frac{e}{C} = \dots \text{ ton}$$

$$R_2 = P_2 - P_1 * \frac{e}{C} = \dots \text{ ton}$$

$$q_1 = \frac{R_{1u} * 1.1}{A_1 * B_1} = \dots \text{ t/m}^2 \not\geq q_{all}$$

$$q_2 = \frac{R_2 * 1.1}{A_2 * B_2} = \dots \text{ t/m}^2 \not\geq q_{all}$$

If $q_1 > q_{all}$ increase B_1

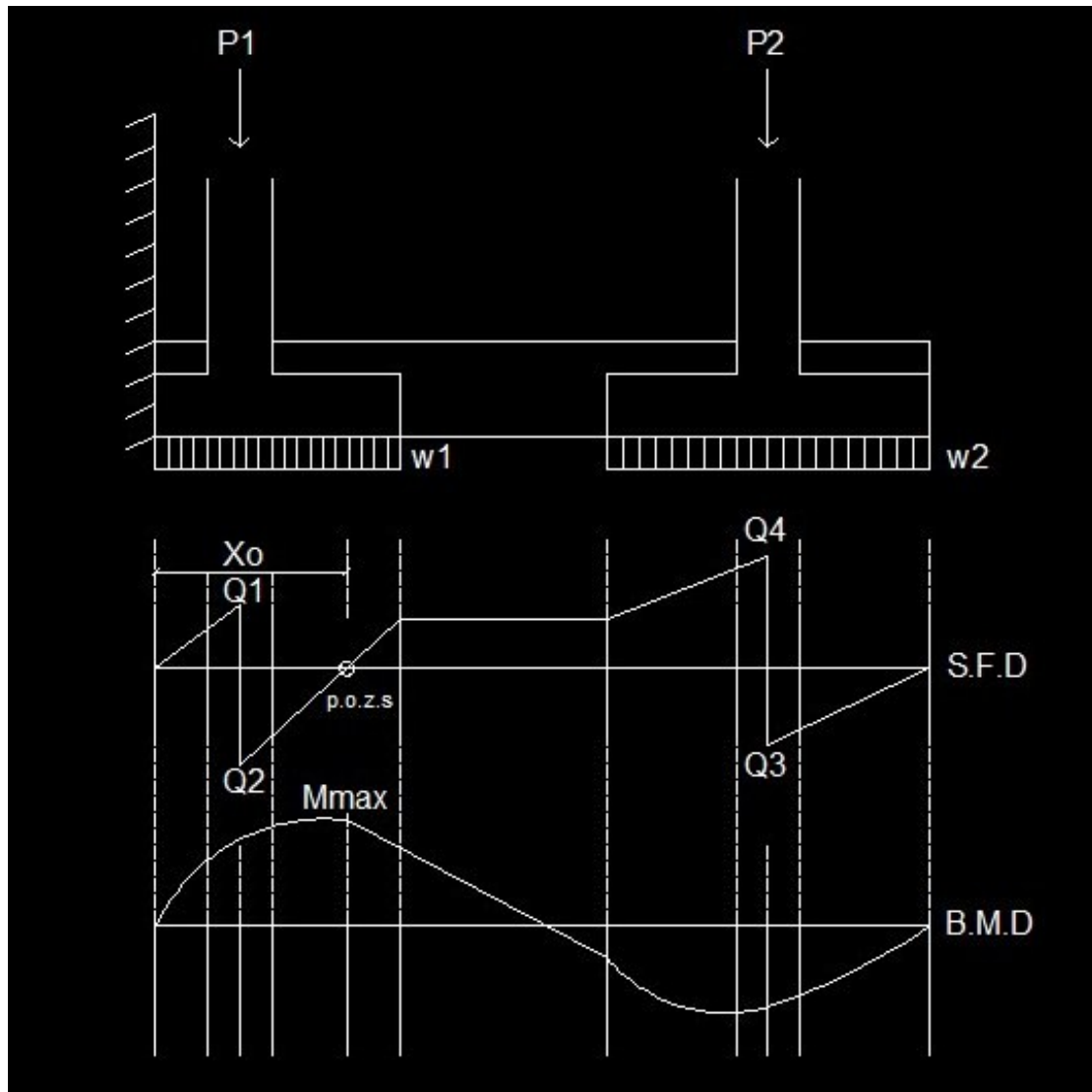
If $q_2 > q_{all}$ increase B_2

End of Working Loads .

4) Design of Strap Beam:

Calculation of Moment and Shear for Strap Beam:

Beam:



$$P_{1u} = 1.5 P_1 = \dots \text{ ton}$$

$$P_{2u} = 1.5 P_2 = \dots \text{ ton}$$

$$R_{1u} = 1.5 R_1 = \dots \text{ ton}$$

$$R_{2u} = 1.5 R_2 = \dots \text{ ton}$$

$$W_1 = \frac{R_{1u}}{A_1} = \dots \text{ t/m'}$$

$$W_2 = \frac{R_{2u}}{A_2} = \dots \text{ t/m'}$$

Point of Zero Shear

At distance X_0

$$X_0 = \frac{P_{1u}}{w_1} = \dots \text{ m}$$

$$M_{\max} = P_{1u} (X_0 - C_1) - W_1 * \left(\frac{(X_0)^2}{2} \right) = \dots \text{ mt}$$

$$d = c_1 \sqrt{\frac{Mult}{Fcu*b}} = \dots \text{ cm}$$

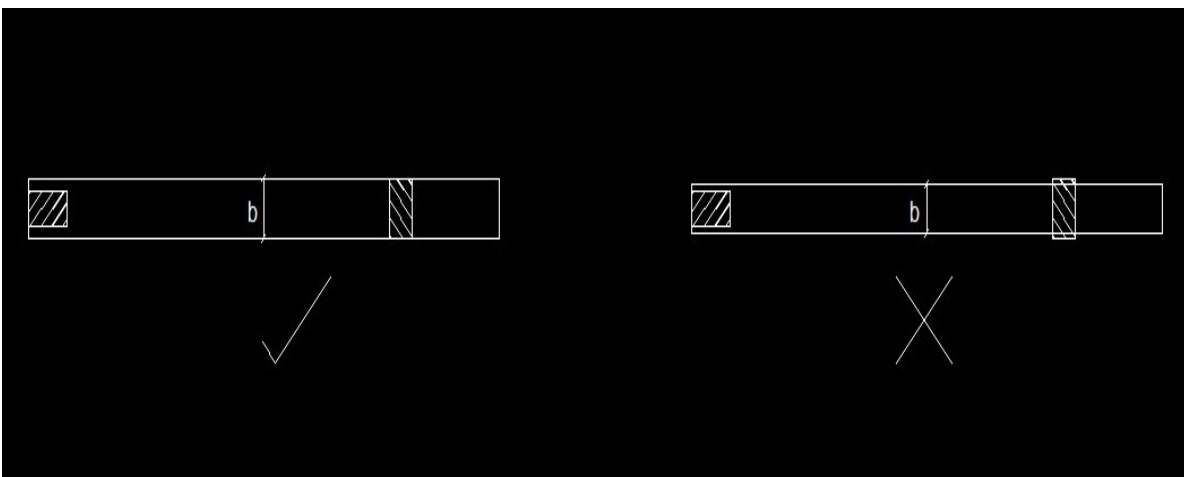
حيث أن:

$c_1 = 4 \rightarrow$ beam

$b \rightarrow$ strap beam عرض

$b = 40 \rightarrow 80 \text{ cm}$

ولا تقل عن بعد العمود في اتجاه strap beam



5) Check Shear:

$$Q_1 = W_1 * C_1 = \dots t$$

$$Q_2 = Q_1 - P_{1u} = \dots t$$

$$Q_3 = W_2 * \frac{A_2}{2} = \dots t$$

$$Q_4 = Q_3 - P_{2u} = \dots t$$

$$Q_{sh1} = Q_1 \text{ or } Q_2 - W_1 * \left(\frac{d}{2} + \frac{a1 \text{ or } b1}{2} \right) = \dots \text{ ton}$$

حيث أن:

Take the bigger of Q_1 or Q_2

a → طول العمود

b → عرض العمود

b1 or a1 → حسب اتجاه العمود

$$Q_{sh2} = Q_3 \text{ or } Q_4 - W_2 * \left(\frac{d}{2} + \frac{a2 \text{ or } b2}{2} \right) = \dots \text{ ton}$$

حيث أن:

Take the bigger of Q_3 or Q_4

a → طول العمود

b → عرض العمود

b² or a² → حسب اتجاه العمود

$$q_{sh} = \frac{Q_{sh1 \text{ or } 2}}{b*d} = \dots \text{ kg/cm}^2$$

حيث أن:

Take the bigger of Q_{sh1} or Q_{sh2}

b → strap beam عرض

$$q_{cu} = 0.75 * \sqrt{\frac{F_{cu}}{\chi\chi_c}} \text{ (for beam) } = \dots \text{ kg/cm}^2$$

حيث أن:

$$\chi_c = 1.5$$

If $q_{cu} > q_{sh}$ ok (use min stirrups 5y8/m')

If $q_{cu} < q_{sh}$ (use min stirrups 7y10/m')

$$t = d + \text{cover}$$

$$\text{cover} = (5 \text{ to } 10 \text{ cm})$$

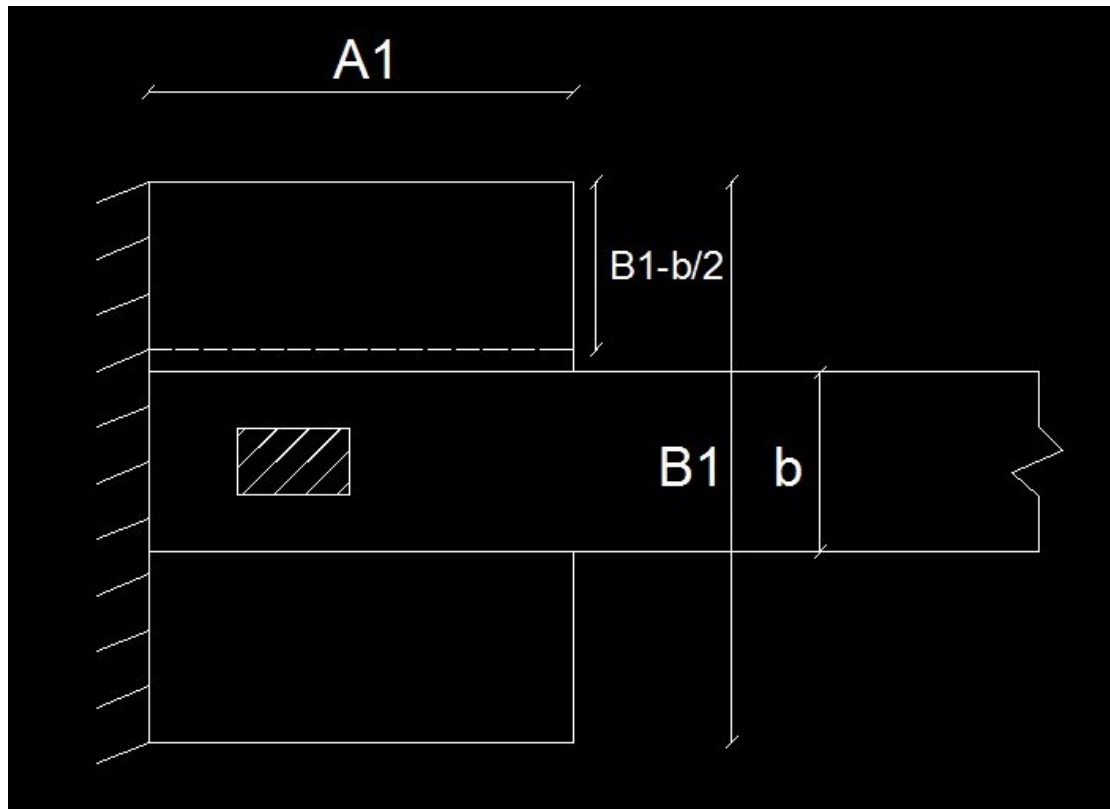
Reinforcement of the Strap beam:

$$A_{s \text{ top}} = \frac{M_{\max}}{J*d*f_y} = \dots \text{ cm}^2$$

$$A_{s \text{ bott}} = 20 \% A_{s \text{ top}} = \dots \text{ cm}^2$$

6) Design of Footing:

Footing 1 (F_1):



$$q_{u1} = \frac{R1u}{A1 * B1} = \dots \text{ t/m}^2$$

$$M_1 = q_{u1} * \frac{\left(\frac{B1-b}{2}\right)^2}{2} = \dots \text{ mt}$$

$$d_1 = c_1 \sqrt{\frac{M1ult}{Fcu * B}} = \dots \text{ cm}$$

حيث أن:

$B = 100 \text{ cm}$, $c_1 = 5$ for Footing

Check Shear:

$$Q_{sh} = q_{u1} * \left(\frac{d}{2} + \frac{B1-b}{2} \right) = \dots \text{ ton}$$

$$q_{sh} = \frac{Q_{sh}}{B * d1} = \dots \text{ kg/cm}^2$$

حيث أن:

$$B = 100 \text{ cm}$$

$$q_{cu} = 0.4 * \sqrt{F_{cu}} = \dots \text{ kg/cm}^2$$

If $q_{cu} > q_{sh}$ ok safe

If $q_{cu} < q_{sh}$ un safe increase depth

$$\text{Take } d = \frac{Q_{sh}}{(q_{cu} * B)} = \dots \text{ cm}$$

$$t = d + \text{cover}$$

$$\text{cover} = (5 \text{ to } 10 \text{ cm})$$

Reinforcement of the footing (1):

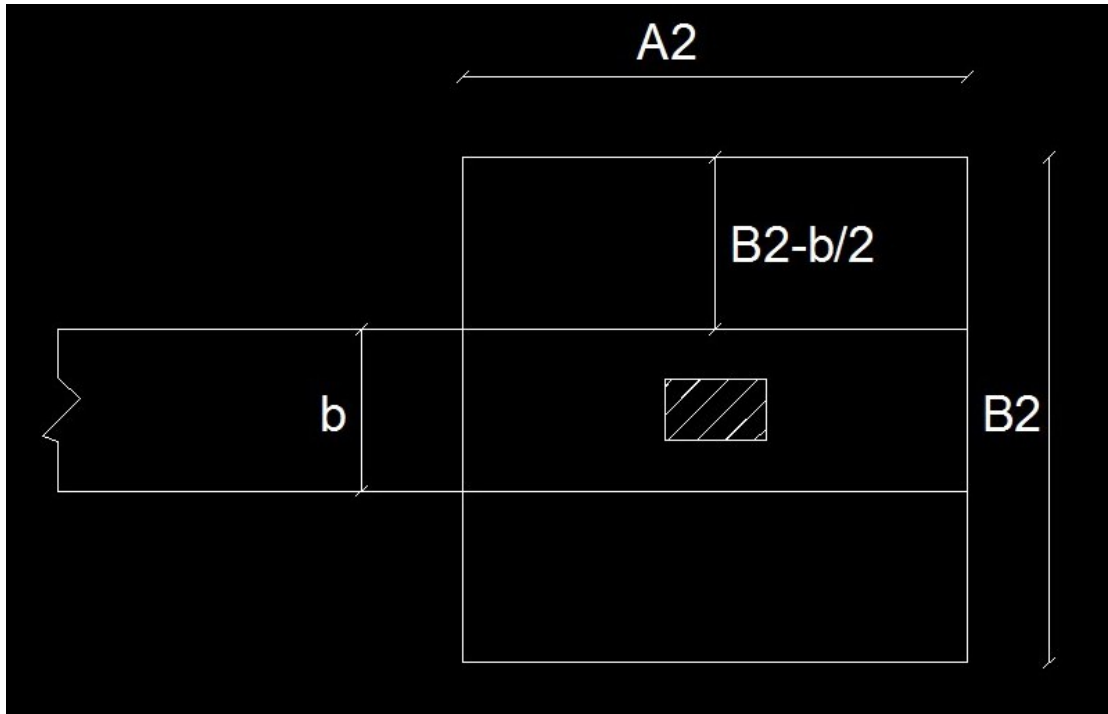
$$A_{s1} = \frac{M1}{J * d1 * Fy} = \dots \text{ cm}^2 / \text{m}'$$

$$A_{s \text{ min}} = 5y12 / \text{m}' = \dots \text{ cm}^2 / \text{m}'$$

If $A_{s1} \geq A_{s \text{ min}} \rightarrow \text{ok}$

If $A_{s1} < A_{s \text{ min}} \rightarrow \text{take } A_{s1} = A_{s \text{ min}}$

Footing 2 (F₂):



$$q_{u2} = \frac{R_{2u}}{A_2 * B_2} = \dots \text{ t/m}^2$$

$$M_2 = q_{u2} * \frac{\left(\frac{B_2 - b}{2}\right)^2}{2} = \dots \text{ mt}$$

$$d_2 = c_1 \sqrt{\frac{M_{2ult}}{F_{cu} * B}} = \dots \text{ cm}$$

حيث أن:

B = 100 cm , c₁ = 5 for Footing

Check Shear:

$$Q_{sh} = q_{u2} * \left(\frac{d}{2} + \frac{B_2 - b}{2}\right) = \dots \text{ ton}$$

$$q_{sh} = \frac{Q_{sh}}{B \cdot d^2} = \dots \text{ kg/cm}^2$$

حيث أن:

$$B = 100 \text{ cm}$$

$$q_{cu} = 0.4 \cdot \sqrt{F_{cu}} = \dots \text{ kg/cm}^2$$

If $q_{cu} > q_{sh}$ ok safe

If $q_{cu} < q_{sh}$ un safe increase depth

$$\text{Take } d = \frac{Q_{sh}}{(q_{cu} \cdot B)} = \dots \text{ cm}$$

$$t = d + \text{cover}$$

$$\text{cover} = (5 \text{ to } 10 \text{ cm})$$

Reinforcement of the footing (2):

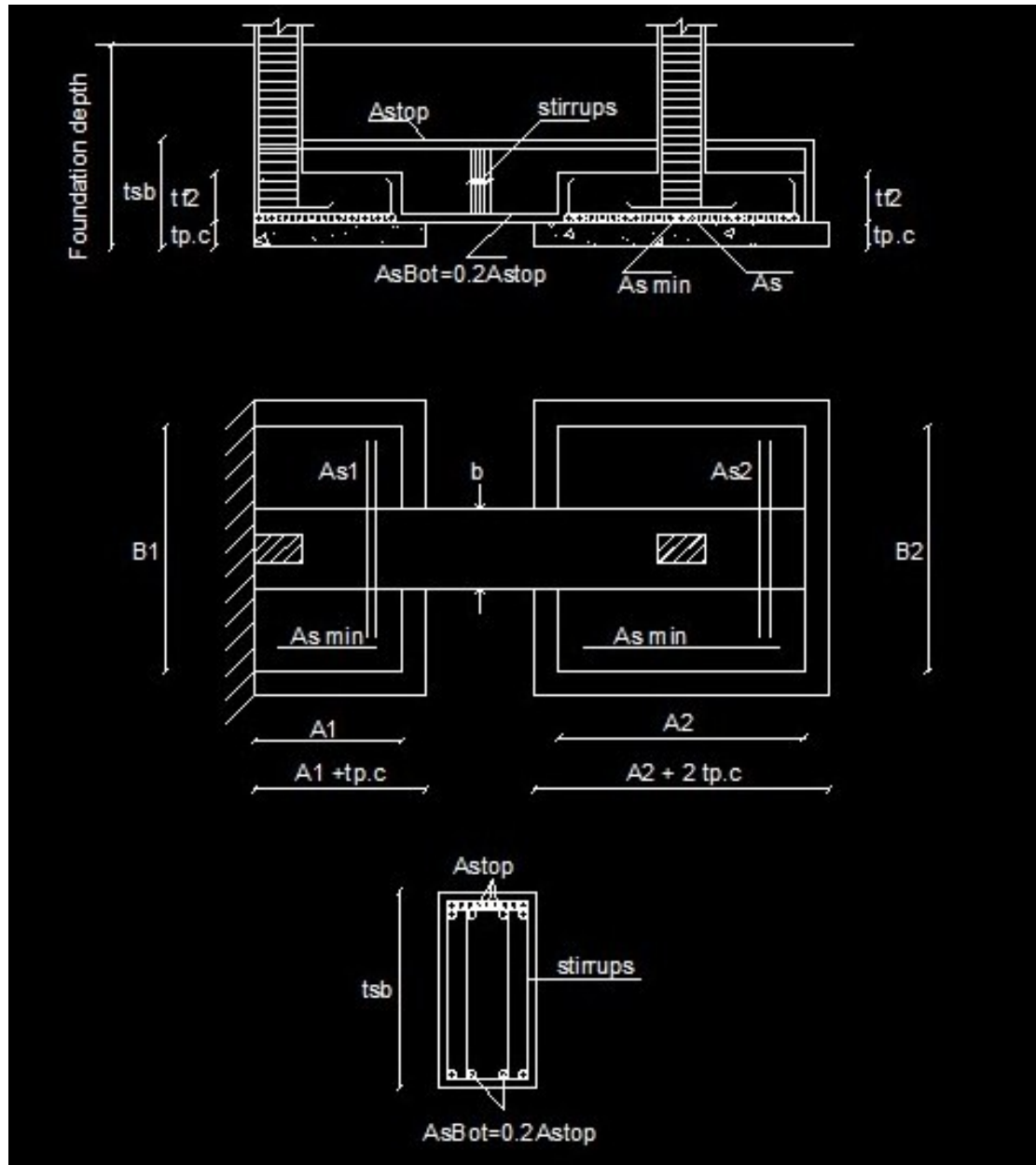
$$A_{s2} = \frac{M_2}{J \cdot d^2 \cdot F_y} = \dots \text{ cm}^2 / \text{m}'$$

$$A_{s \text{ min}} = 5y12 / \text{m}' = \dots \text{ cm}^2 / \text{m}'$$

If $A_{s2} \geq A_{s \text{ min}} \rightarrow \text{ok}$

If $A_{s2} < A_{s \text{ min}} \rightarrow \text{take } A_{s2} = A_{s \text{ min}}$

Details of Reinforcement:

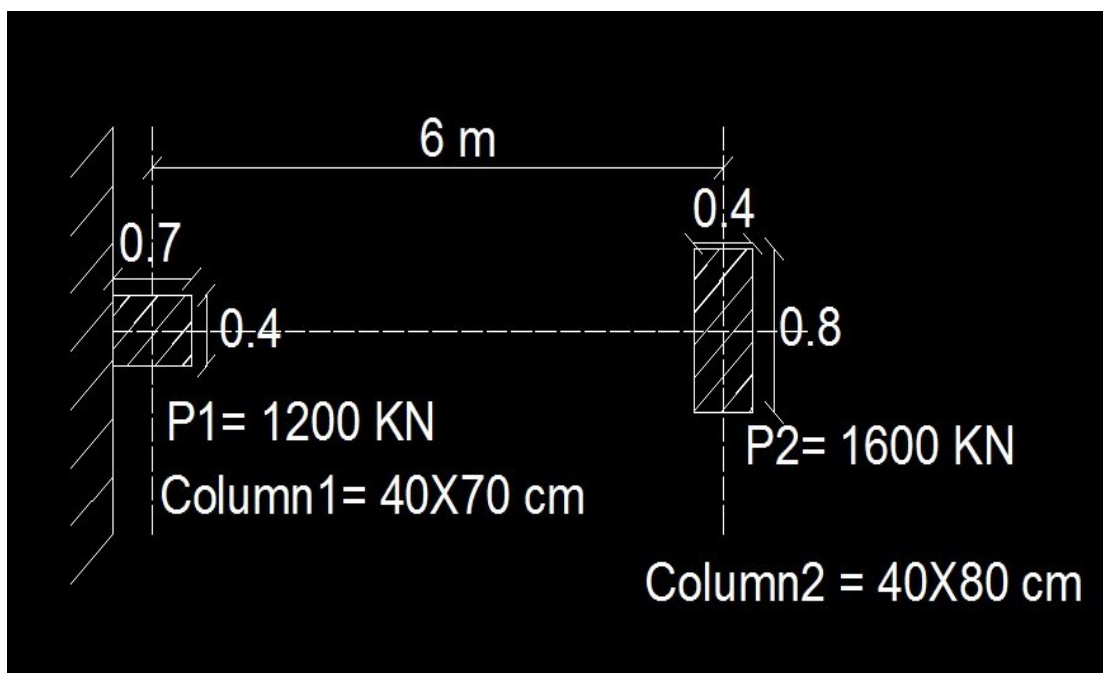


Example: 1

The two columns shown in fig are supported to be connected with a strap beam passing through the outer face of footing (1) to the outer face of footing (2)

It is required to:

- 1) Determine the footing Area.
- 2) Draw bending Moment and shear of the strap beam.
- 3) Determine the depth & reinforcement steel of the strap beam wish satisfy bending Moment and shear .
- 4) Draw clear sketch showing dimensions of strap beam and steel details.



Solution

Given: $f_{cu} = 250 \text{ kg/cm}^2$, $q_{all} = 175 \text{ kN / m}^2$,

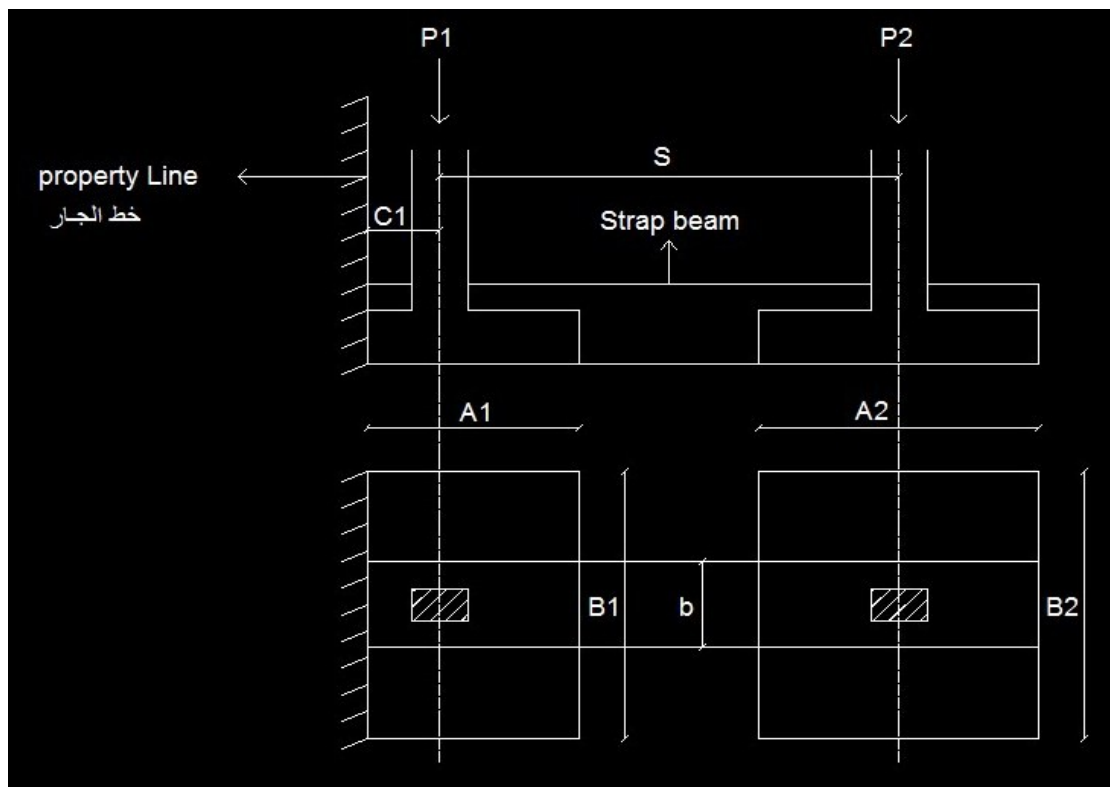
$F_y = 3600 \text{ kg/cm}^2$, Foundation depth = 2m

$P_1 = 1200 \text{ KN} = 120 \text{ Ton}$

$P_2 = 1600 \text{ KN} = 160 \text{ Ton}$

$q_{all} = 175 \text{ kN / m}^2 = 17.5 \text{ t / m}^2$

1) Dimension of Footing:



$$P_{t1} = 1.2 * P_1 = 1.2 * 120 = 144 \text{ ton}$$

$$P_{t2} = P_2 = 160 \text{ ton}$$

$$\text{Take } t_{p.c} = 30 \text{ cm}$$

Area of Footing (1):

$$A_{f1} = \frac{P_{t1}}{q_{all}} = \frac{144}{17.5} = 8.3 \text{ m}^2 \rightarrow A_1, B_1$$

$$B_1 = 3.2 \text{ m}$$

$$A_1 = 2.6 \text{ m}$$

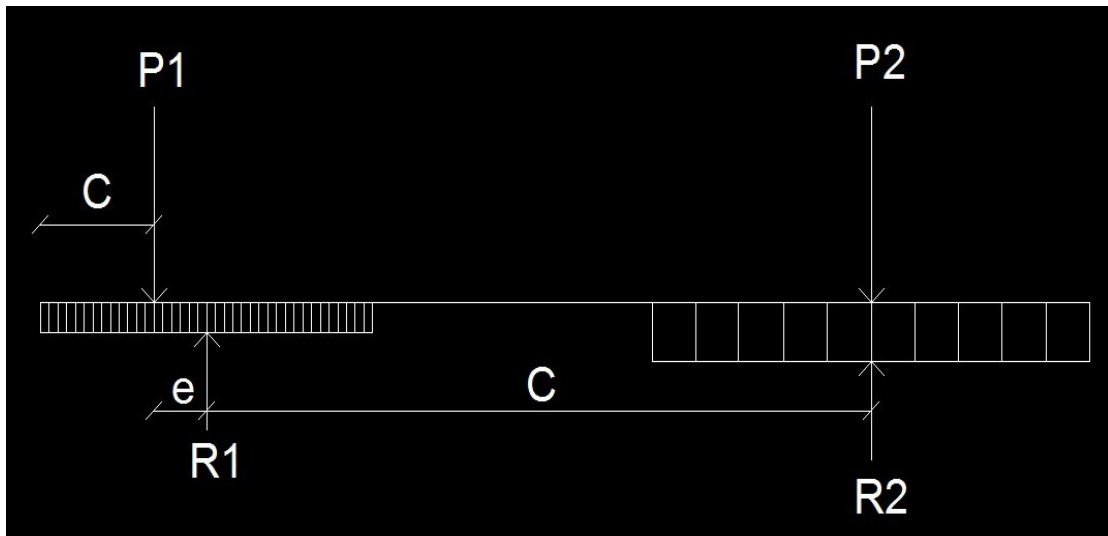
Area of Footing (2):

$$A_{f2} = \frac{P_{t2}}{q_{all}} = \frac{160}{17.5} = 9.15 \text{ m}^2 \rightarrow A_2, B_2$$

$$B_2 = 3.3 \text{ m}$$

$$A_2 = 2.8 \text{ m}$$

2) Determination of eccentricity:



$$e = \frac{A_1}{2} - C_1 = \frac{2.6}{2} - 0.35 = 0.95 \text{ m}$$

$$C = s - e = 6 - 0.95 = 5.05 \text{ m}$$

3) Check Area:

$$R_{1u} = P_1 + P_1 * \frac{e}{C} = 120 + 120 * \frac{0.95}{5.05} = 142.6 \text{ ton}$$

$$R_2 = P_2 - P_1 * \frac{e}{C} = 160 - 120 * \frac{0.95}{5.05} = 137.4 \text{ ton}$$

$$q_1 = \frac{R_{1u} * 1.1}{A_1 * B_1} = \frac{142.6 * 1.1}{2.6 * 3.2} = 18.85 \text{ t/m}^2$$

$$q_1 > q_{all}$$

$$18.85 > 17.5 \text{ increase } B_1$$

$$q_1 = \frac{R_{1u} * 1.1}{A_1 * B_1}$$

$$17.5 = \frac{142.6 * 1.1}{2.6 * B_1}$$

$$17.5 * 2.6 B_1 = 142.6 * 1.1$$

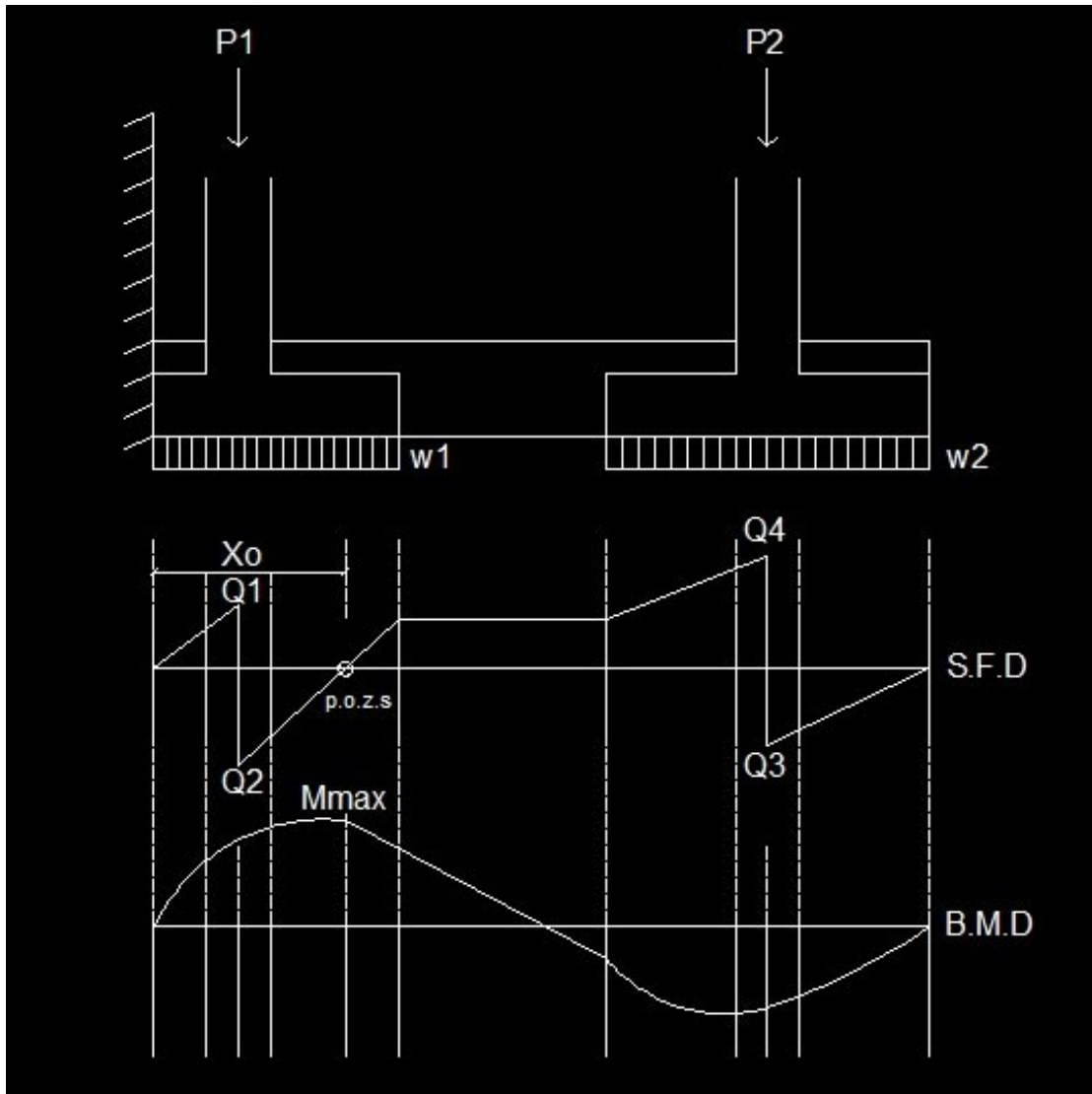
$$B_1 = 3.5 \text{ m}$$

$$q_2 = \frac{Rt_2 * 1.1}{A_2 * B_2} = \frac{137.4 * 1.1}{2.8 * 3.3} = 16.3 \text{ t/m}^2 > q_{\text{all}} \text{ ok}$$

End of Working Loads .

4) Design of Strap Beam:

Calculation of Moment and Shear for Strap Beam:



$$P_{1u} = 1.5 P_1 = 120 * 1.5 = 180 \text{ Ton}$$

$$P_{2u} = 1.5 P_2 = 160 * 1.5 = 240 \text{ Ton}$$

$$R_{1u} = 1.5 R_1 = 1.5 * 142.6 = 213.9 \text{ Ton}$$

$$R_{2u} = 1.5 R_2 = 1.5 * 137.4 = 206 \text{ Ton}$$

$$W_1 = \frac{R_{1u}}{A_1} = \frac{213.9}{2.6} = 82 \text{ t/m'}$$

$$W_2 = \frac{R_{2u}}{A_2} = \frac{206}{2.8} = 73.6 \text{ t/m'}$$

Point of Zero Shear

At distance X_0

$$X_0 = \frac{p1u}{w1} = \frac{180}{82} = 2.195 \text{ m}$$

$$M_{\max} = 180(2.195 - 0.35) - 82 * \left(\frac{(2.195)^2}{2} \right) = 135 \text{ mt}$$

$$d = c_1 \sqrt{\frac{Mult}{Fcu * b}}$$

Take $b = 80 \text{ cm}$

$$d = 4 \sqrt{\frac{135 * 10^5}{250 * 80}} = 104 \cong 110 \text{ cm}$$

5) Check Shear:

$$Q_1 = W_1 * C_1 = 82 * 0.35 = 28.7 \text{ t}$$

$$Q_2 = Q_1 - P_{1u} = 28.7 - 180 = 151.3 \text{ t}$$

$$Q_3 = W_2 * \frac{A2}{2} = 73.6 * \frac{2.8}{2} = 103 \text{ t}$$

$$Q_4 = Q_3 - P_{2u} = 103 - 240 = 137 \text{ t}$$

$$Q_{sh1} = Q_2 - W_1 * \left(\frac{d}{2} + \frac{a1}{2} \right)$$

$$= 151.3 - 82 * \left(\frac{1.1}{2} + \frac{0.7}{2} \right) = 77.5 \text{ ton}$$

$$Q_{sh2} = Q_4 - W_2 * \left(\frac{d}{2} + \frac{b_2}{2} \right)$$

$$= 137 - 73.6 * \left(\frac{1.1}{2} + \frac{0.4}{2} \right) = 81.8 \text{ ton}$$

$$q_{sh} = \frac{Q_{sh2}}{b*d} = \frac{81.8 * 10^3}{80 * 110} = 9.2 \text{ kg/cm}^2$$

$$q_{cu} = 0.75 * \sqrt{\frac{F_{cu}}{\lambda \lambda_c}} = 0.75 * \sqrt{\frac{250}{\lambda 1.5}} = 9.68 \text{ kg/cm}^2$$

If $q_{cu} > q_{sh}$ ok use min stirrups 5y8/m'

$$t = d + \text{cover} = 110 + 10 = 120 \text{ cm}$$

Reinforcement of the Strap beam:

$$A_{s \text{ top}} = \frac{M_{\max}}{J * d * f_y} = \frac{135 * 10^5}{0.826 * 110 * 3600} = 41.3 \text{ cm}^2$$

Use 11 y 22

$$A_{s \text{ bott}} = 20 \% A_{s \text{ top}} = 0.2 * 41.3 = 8.3 \text{ cm}^2$$

Use 5 y 16

6) Design of Footing:

Footing 1 (F_1):

$$q_{u1} = \frac{R1u}{A1*B1} = \frac{213.9}{2.6*3.5} = 23.5 \text{ t/m}^2$$

$$M_1 = q_{u1} * \frac{\left(\frac{B1-b}{2}\right)^2}{2} = 23.5 * \frac{\left(\frac{3.5-0.8}{2}\right)^2}{2} = 21.4 \text{ mt}$$

$$d_1 = c_1 \sqrt{\frac{M1ult}{Fcu*B}} = 5 \sqrt{\frac{21.4*10^5}{250*100}} = 46.26 \cong 50 \text{ cm}$$

Check Shear:

$$Q_{sh} = q_{u1} * \left(\frac{d}{2} + \frac{B1-b}{2}\right) \\ = 23.5 * \left(\frac{0.5}{2} + \frac{3.5-0.8}{2}\right) = 37.6 \text{ ton}$$

$$q_{sh} = \frac{Q_{sh}}{B*d1} = \frac{37.6*10^3}{100*50} = 7.52 \text{ kg/cm}^2$$

$$q_{cu} = 0.4 * \sqrt{Fcu} = 0.4 * \sqrt{250} = 6.32 \text{ kg/cm}^2$$

$$q_{cu} < q_{sh}$$

6.32 < 7.52 un safe increase depth

Take $d_1 = Q_{sh} / (q_{cu} * B)$

$$d_1 = \frac{37.6*10^3}{100*6.32} = 59.49 \cong 65 \text{ cm}$$

$$t_1 = d + \text{cover} = 65 + 10 = 75 \text{ cm}$$

Reinforcement of the footing (1):

$$A_{s1} = \frac{M_1}{J * d_1 * F_y} = \frac{21.4 * 10^5}{0.826 * 65 * 3600} = 11.07 \text{ cm}^2 / \text{m}'$$

Use 6 y 16

$$A_{s \text{ min}} = 5y12 / \text{m}' = 5.65 \text{ cm}^2 / \text{m}'$$

$$\text{take } A_{s1} = 11.07 \text{ cm}^2 / \text{m}'$$

Use 6 y 16

Footing 2 (F_2):

$$q_{u2} = \frac{R_{2u}}{A_2 * B_2} = \frac{206}{2.8 * 3.3} = 22.3 \text{ t/m}^2$$

$$M_2 = q_{u2} * \frac{\left(\frac{B_2 - b}{2}\right)^2}{2} = 22.3 * \frac{\left(\frac{3.3 - 0.8}{2}\right)^2}{2} = 17.4 \text{ mt}$$

$$d_2 = c_1 \sqrt{\frac{M_{2ult}}{F_{cu} * B}} = 5 \sqrt{\frac{17.4 * 10^5}{250 * 100}} = 41.71 \cong 50 \text{ cm}$$

Check Shear:

$$Q_{sh} = q_{u2} * \left(\frac{d}{2} + \frac{B_2 - b}{2}\right) \\ = 22.3 * \left(\frac{0.5}{2} + \frac{3.3 - 0.8}{2}\right) = 33.45 \text{ ton}$$

$$q_{sh} = \frac{Q_{sh}}{B \cdot d_2} = \frac{33.45 \cdot 10^3}{100 \cdot 50} = 6.69 \text{ kg/cm}^2$$

$$q_{cu} = 0.4 \cdot \sqrt{F_{cu}} = 0.4 \cdot \sqrt{250} = 6.32 \text{ kg/cm}^2$$

$$q_{cu} < q_{sh}$$

6.32 < 6.69 un safe increase depth

Take $d_2 = Q_{sh} / (q_{cu} \cdot B)$

$$d_2 = \frac{33.45 \cdot 10^3}{100 \cdot 6.32} = 52.92 \cong 60 \text{ cm}$$

$$t_2 = d_2 + \text{cover} = 60 + 10 = 70 \text{ cm}$$

Reinforcement of the footing (1):

$$A_{s2} = \frac{M_2}{J \cdot d_2 \cdot F_y} = \frac{17.4 \cdot 10^5}{0.826 \cdot 60 \cdot 3600} = 9.75 \text{ cm}^2 / \text{m}'$$

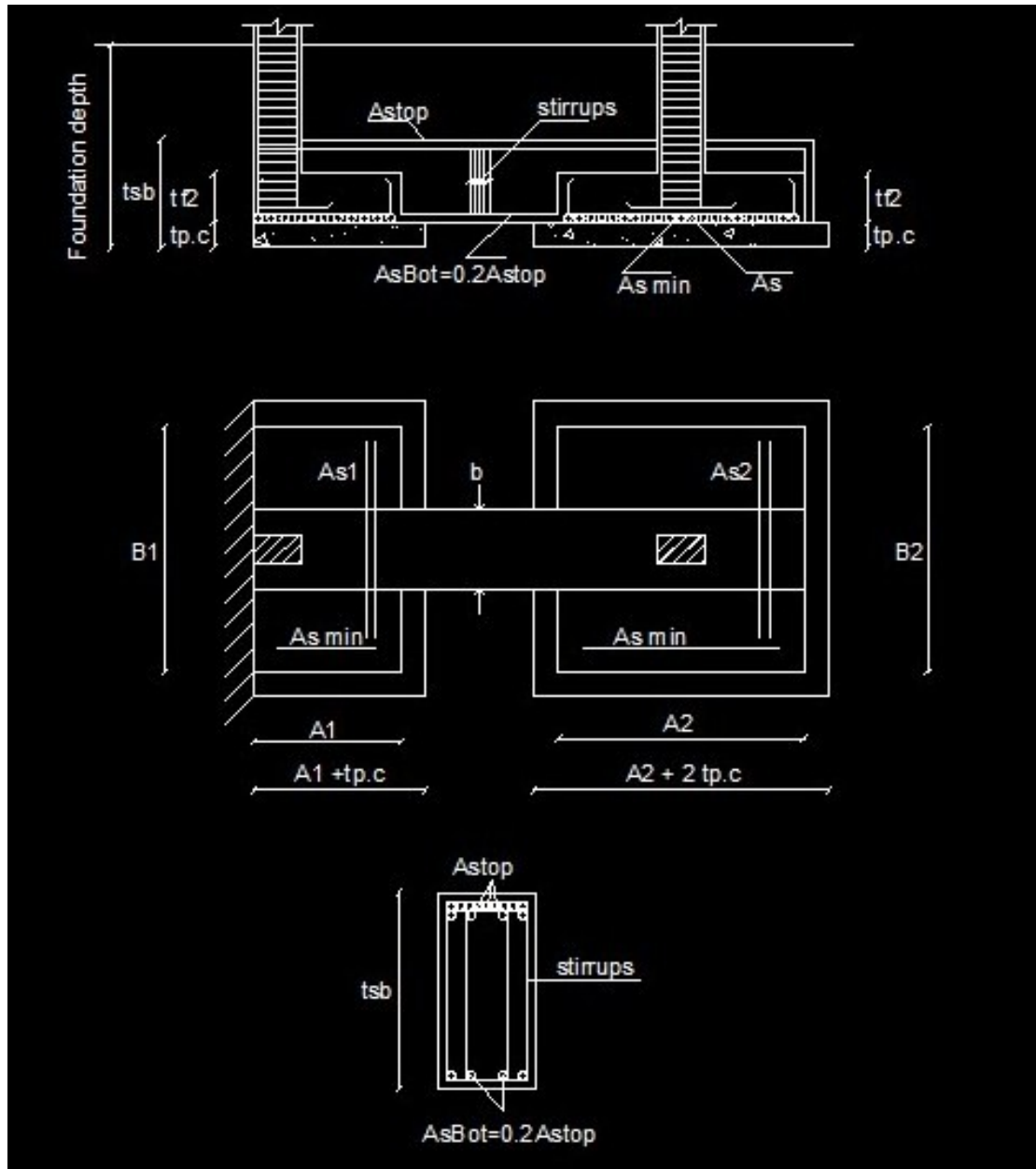
Use 6 y 16

$$A_{s \min} = 5y12 / \text{m}' = 5.65 \text{ cm}^2 / \text{m}'$$

$$\text{take } A_{s1} = 9.75 \text{ cm}^2 / \text{m}'$$

Use 6 y 16

Details of Reinforcement:



Raft Footing:

Calculation of soil pressure under Raft:

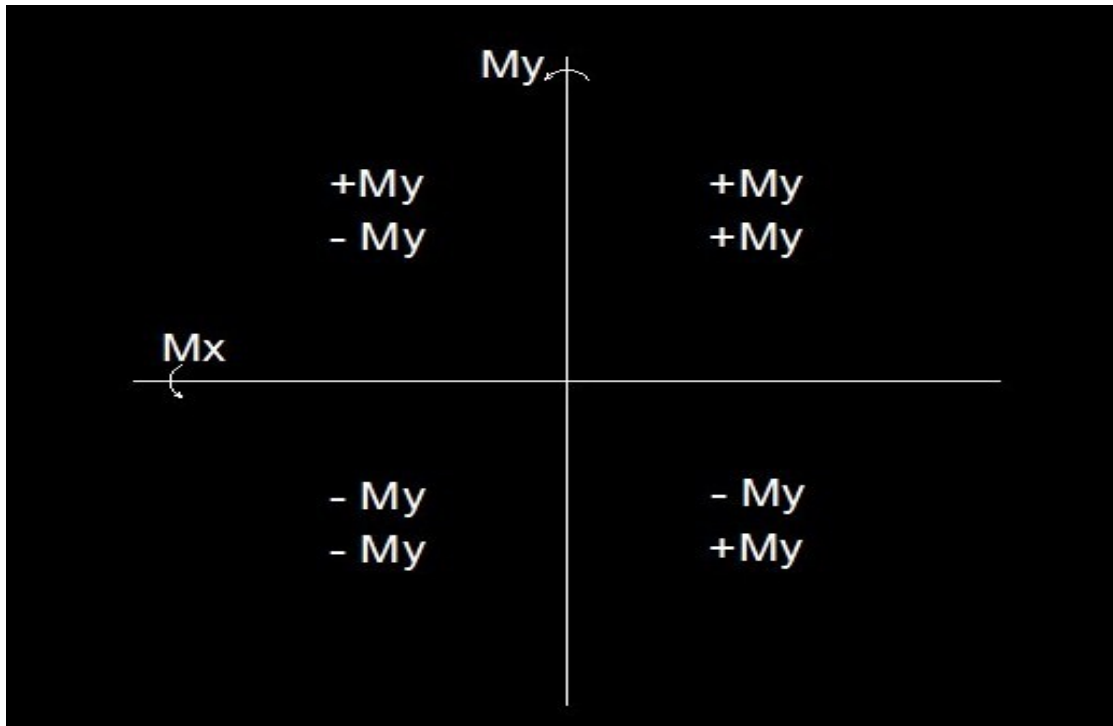
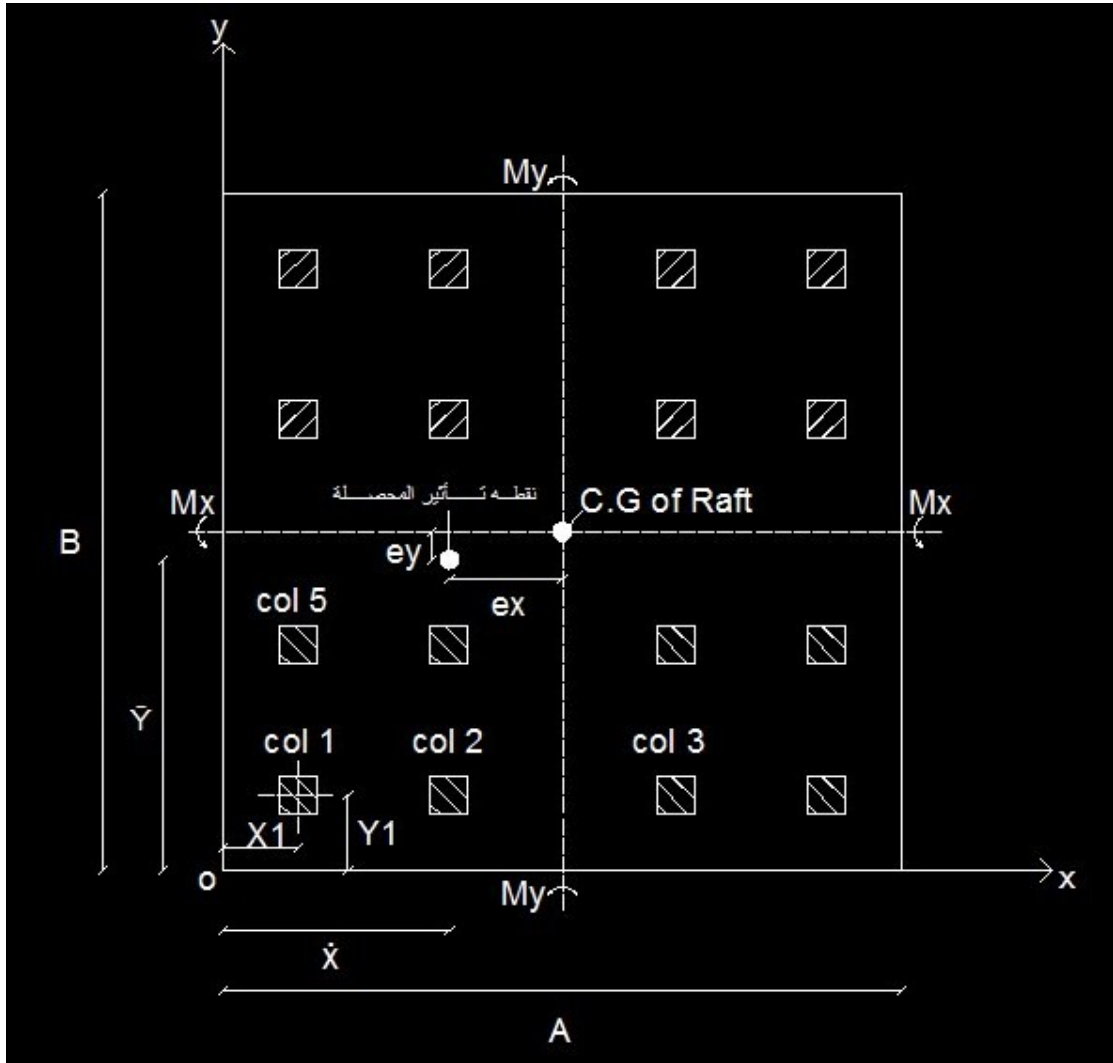
Steps of Calculation:

1) Determination of C.G of Raft:

تحديد C.G للبشة.

2) Determination of Resultant Load and its point of application:

تحديد محصلة القوي (أحمال الأعمدة) ونقطة تأثيرها.



يتم عمل جدول:

Col No.	Load (p)	X	Y	P*X	P*Y
1	P1	X1	Y1	P1* X1	P1* Y1
2	P2	X2	Y2	P2* X2	P2* Y2
3	P3	X3	Y3	P3* X3	P3* Y3
4	P4	X4	Y4	P4* X4	P4* Y4
5	P5	X5	Y5	P5* X5	P5* Y5
6	P6	X6	Y6	P6* X6	P6* Y6
	$\sum P$			$\sum P * X$	$\sum P * Y$

$$\bar{X} = \frac{\sum P * X}{\sum P} = \dots m$$

$$\bar{Y} = \frac{\sum P * Y}{\sum P} = \dots m$$

3) Determination the value and direction determined:

تحديد قيمة واتجاه العزم:

$$e_x = \frac{A}{2} - \bar{X} = \dots m$$

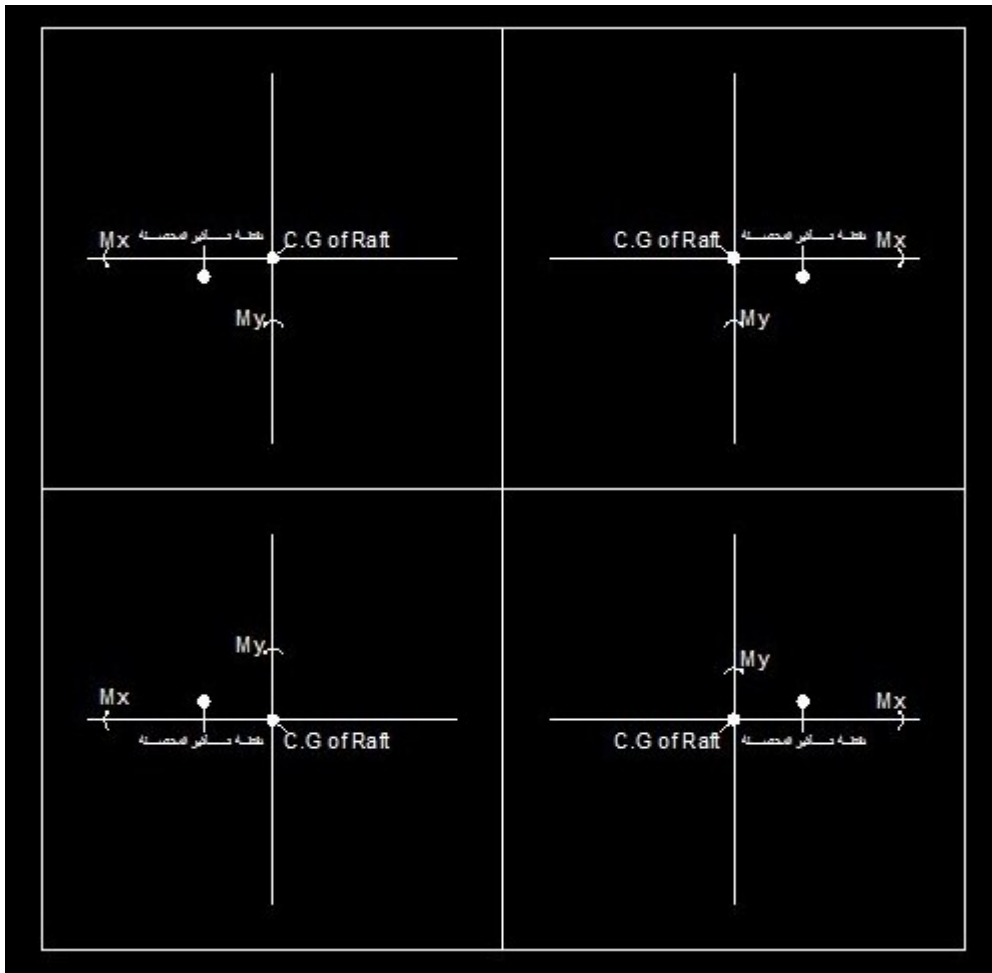
$$e_y = \frac{B}{2} - \bar{Y} = \dots m$$

حيث أن:

$\frac{A}{2}$ → مكان C.G للبشة

$\frac{B}{2}$ → مكان C.G للبشة

اتجاه العزم في الحالات المختلفة:



$$M_x = \sum P * e_y = \dots \text{KN.m}$$

$$M_y = \sum P * e_x = \dots \text{KN.m}$$

4) Calculate the soil pressure at the points required:

$$\sigma = \frac{-N}{A} \pm \frac{M_x}{I_x} * y \pm \frac{M_y}{I_y} * x = \dots \text{KN/m}^2$$

حيث أن:

$$N \rightarrow \sum P$$

إذا كانت النقطة ناحية رأس سهم العزم ← سالب (ضغط)

إذا كانت النقطة ناحية ذيل سهم العزم ← موجب (شد)

A → Area of Raft

$$\text{Area of Raft (A)} = (A * B) = \dots \text{m}^2$$

$$I_x = \frac{A * (B)^3}{12} = \dots \text{m}^4 \quad I_x = \frac{(\text{العمودي}) * (\text{الموازي})^3}{12} = \dots \text{m}^4$$

حيث أن:

الموازي ← البعد الموازي للمحور (X)

$$I_y = \frac{B * (A)^3}{12} = \dots \text{m}^4 \quad I_x = \frac{(\text{العمودي}) * (\text{الموازي})^3}{12} = \dots \text{m}^4$$

حيث أن:

الموازي ← البعد الموازي للمحور (Y)

البعد الأفقي والرأسي من C.G of Raft للنقطة المراد
حساب soil pressure عندها (دائما موجب) $X, Y \leftarrow$

5) If required to Draw the soil pressure on
Nutural axes:

خطوات الرسم :

نوجد مكان Nutural axes (N.A)

أ- نعوض عن $x = 0, \sigma = 0$ ونوجد $y = \checkmark$

$$\sigma = \frac{-N}{A} \pm \frac{M_x}{I_x} * y \pm \frac{M_y}{I_y} * x$$

$$0 = \frac{-N}{A} \pm \frac{M_x}{I_x} * y \pm \frac{M_y}{I_y} * 0$$

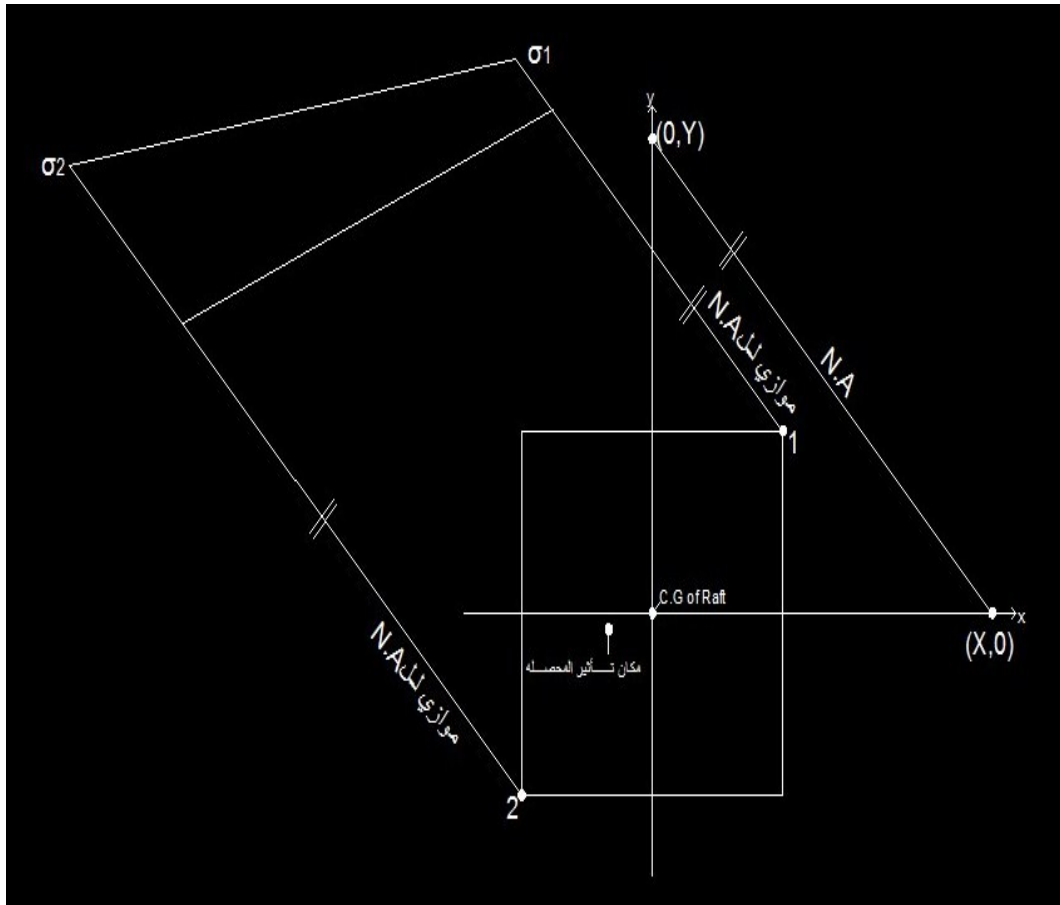
ب- نعوض عن $y = 0, \sigma = 0$ ونوجد $x = \checkmark$

$$\sigma = \frac{-N}{A} \pm \frac{M_x}{I_x} * y \pm \frac{M_y}{I_y} * x$$

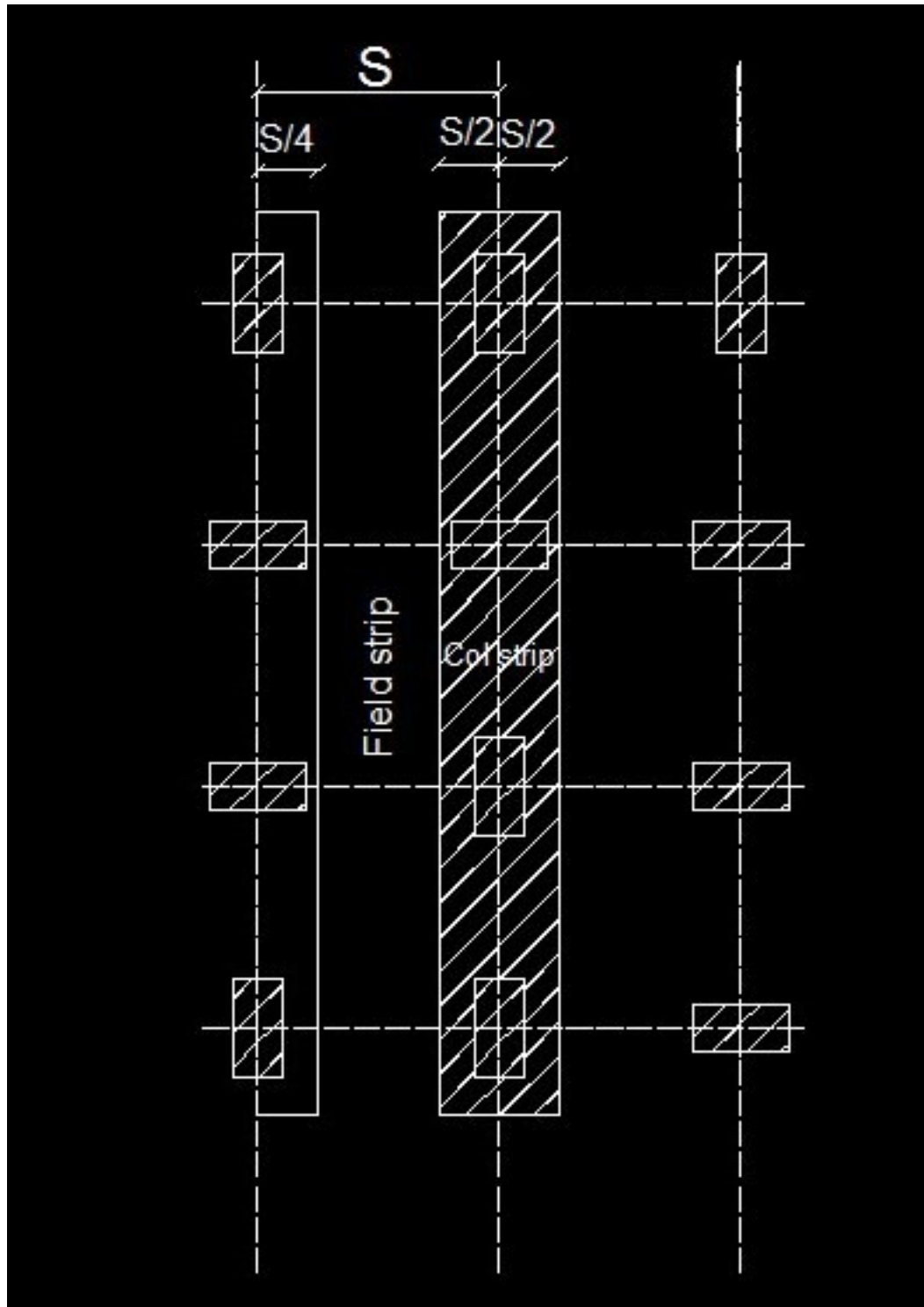
$$0 = \frac{-N}{A} \pm \frac{M_x}{I_x} * 0 \pm \frac{M_y}{I_y} * x$$

ملاحظة:

N.A \leftarrow يظهر خارج حدود اللبشه ويظهر ناحية المربع
المقابل لمربع المحصلة.



6)Raft Foundation Design:



Method (1):

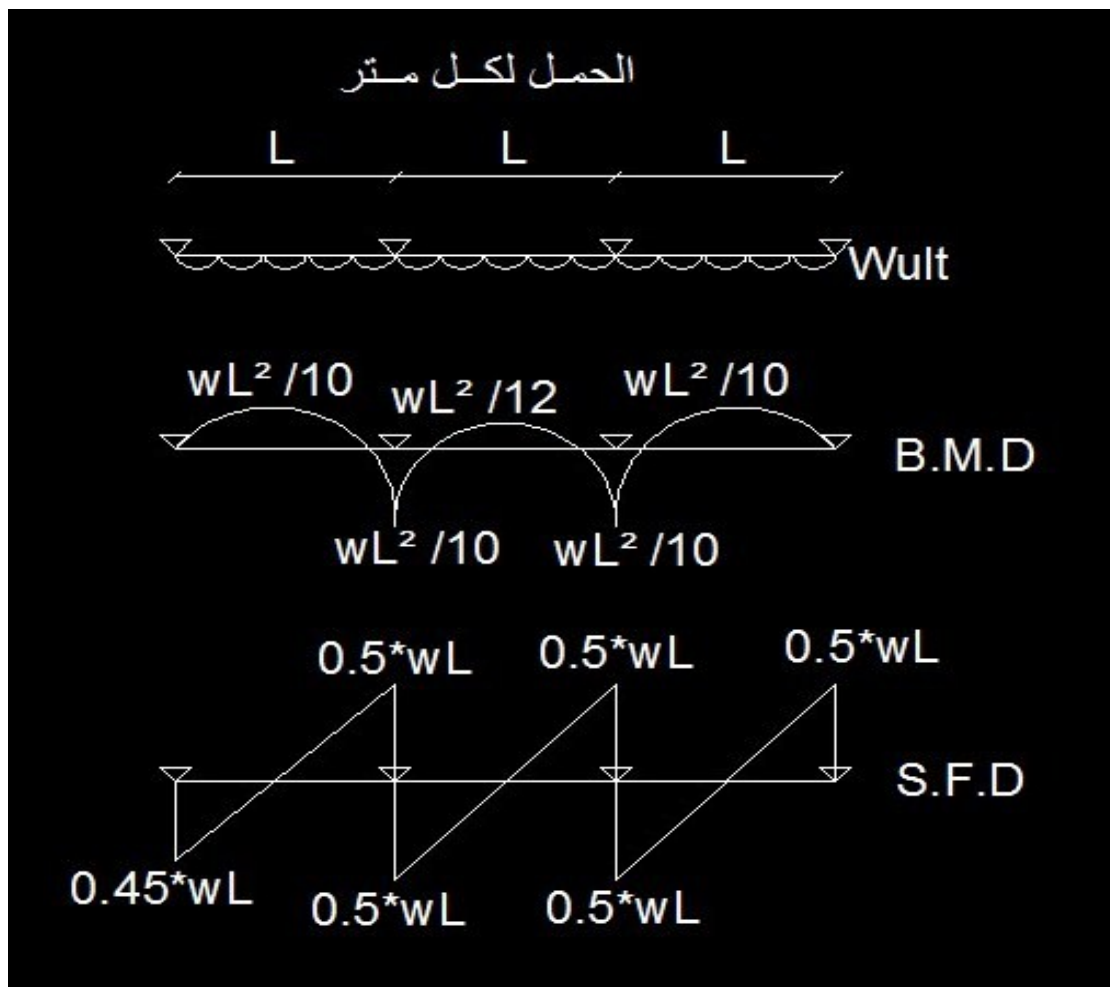
If not given Col strip width take:

Col strip width = $\frac{S}{2}$ عرض الشريحة للأعمدة الداخلية

Col strip width = $\frac{S}{4}$ عرض الشريحة للأعمدة الجار

$$q_{un} = \frac{\sum P_{ult}}{\text{Area}}$$

$$w_{ult} = q_{un} * B = \dots \text{ t/m'}$$



M_{max} = take the bigger Moment from B.M.D

Q_{\max} = take the bigger Shear from S.F.D

$$d = C_1 \sqrt{\frac{Mult}{F_{cu} * B}} = \dots \text{ cm}$$

حيث أن:

$$c_1 = 5$$

$$B = 100 \text{ cm}$$

Check Shear:

$$Q_{sh} = Q_{\max} - \left(\frac{d}{2}\right) * w_{ult} = \dots \text{ ton}$$

$$q_{sh} = \frac{Q_{sh}}{B * d} = \dots \text{ kg/cm}^2$$

حيث أن:

$$B = 100 \text{ cm}$$

$$q_{cu} = 0.4 * \sqrt{F_{cu}} = \dots \text{ kg/cm}^2$$

If $q_{cu} > q_{sh}$ ok safe

If $q_{cu} < q_{sh}$ un safe increase depth

$$\text{Take } d = Q_{sh} / (q_{cu} * B) = \dots \text{ cm}$$

$$t = d + \text{cover}$$

$$\text{cover} = (5 \text{ to } 10 \text{ cm})$$

Check Punching:

$$Q_p = P_u - q_u (A' * B') = \dots \text{ Ton}$$

حيث أن :

$P_u \rightarrow$ أعلى حمل عمود في الشريحة

$$A' = (a_1 + d) = \dots \text{ m}$$

$$B' = (b_1 + d) = \dots \text{ m}$$

$a \rightarrow$ عرض العمود , $b \rightarrow$ طول العمود

$$q_p = \frac{Q_p}{2 * (A' + B') * d} = \dots \text{ kg/cm}^2$$

$$q_{pcu} = \left(0.5 + \frac{b}{a}\right) \sqrt{\frac{F_{cu}}{\lambda_c}} = \dots \text{ kg/cm}^2$$

حيث أن:

If $q_{pcu} > q_p$ ok safe

If $q_{pcu} < q_p$ un safe \rightarrow increase depth

$$t = d + \text{cover}$$

$$\text{cover} = (5 \text{ to } 10 \text{ cm})$$

7) Reinforcement of the footing:

$$A_{s \text{ Top}} = \frac{M_{\text{top}}}{J * d * F_y} = \dots \text{ cm}^2 / \text{m}'$$

$$A_{s \text{ Bot}} = \frac{M_{\text{bot}}}{J * d * F_y} = \dots \text{ cm}^2 / \text{m}'$$

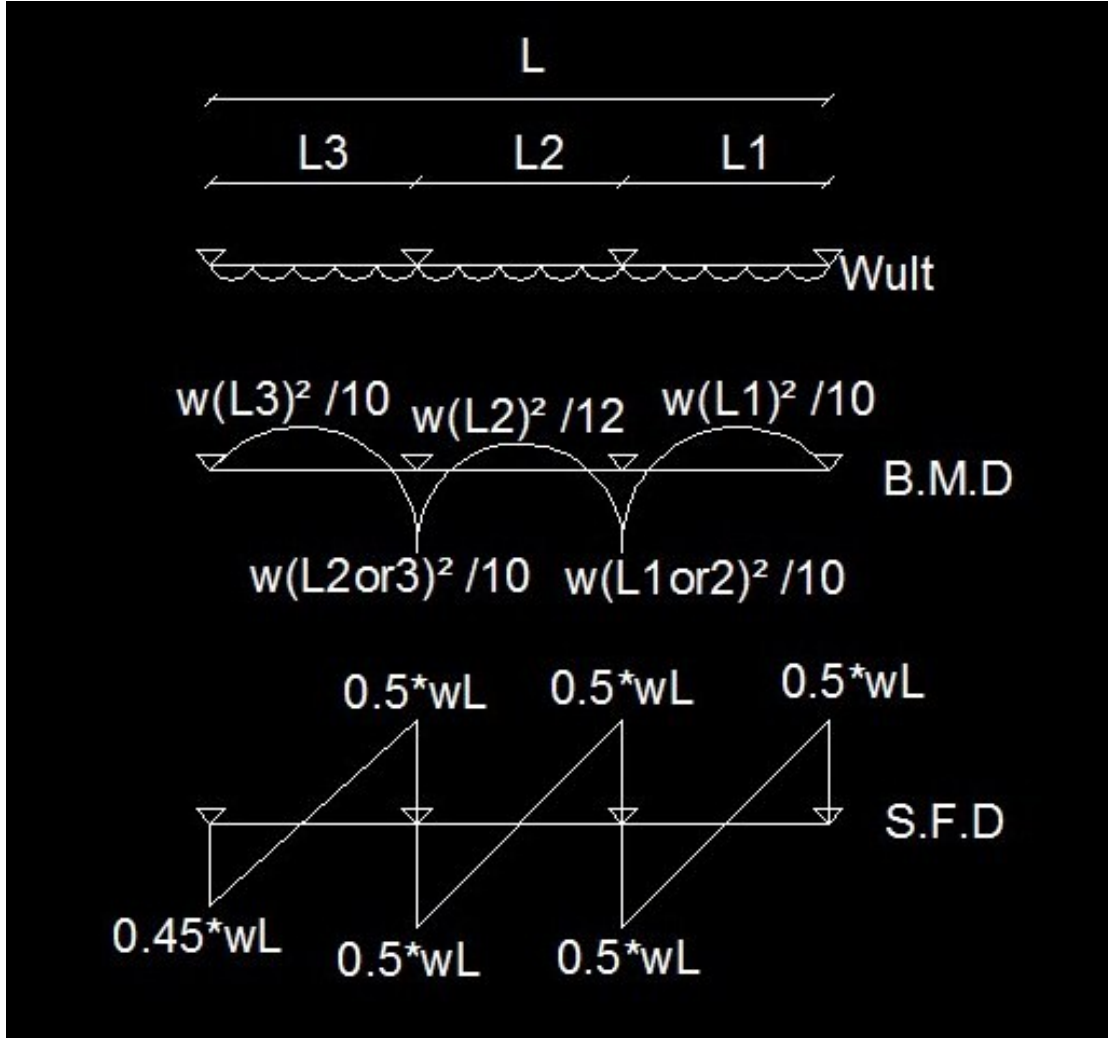
حيث أن:

M_{top} ← أعلي عزم علوي

M_{bot} ← أعلي عزم سفلي

Method (2):

$$W = \frac{\sum Pw}{L} = \dots \text{ KN/B}$$



حيث أن:

$\sum P w \leftarrow$ مجموع أحمال أعمدة Col strip فقط

$B \leftarrow$ عرض شريحة ال Col strip

$L \leftarrow$ طول شريحة ال Col strip

$$W_u = W * 1.5$$

M_{\max} = take the bigger Moment from B.M.D

Q_{\max} = take the bigger Shear from S.F.D

$$d = C_1 \sqrt{\frac{M_{ult}}{F_{cu} * B}} = \dots \text{ cm}$$

حيث أن:

$$C_1 = 5$$

B ← عرض شريحة ال Col strip

Check Shear:

$$Q_{sh} = Q_{\max} - \left(\frac{d}{2}\right) * w_{ult} = \dots \text{ ton}$$

$$q_{sh} = \frac{Q_{sh}}{B * d} = \dots \text{ kg/cm}^2$$

حيث أن:

B ← عرض شريحة ال Col strip

$$q_{cu} = 0.4 * \sqrt{F_{cu}} = \dots \text{ kg/cm}^2$$

If $q_{cu} > q_{sh}$ ok safe

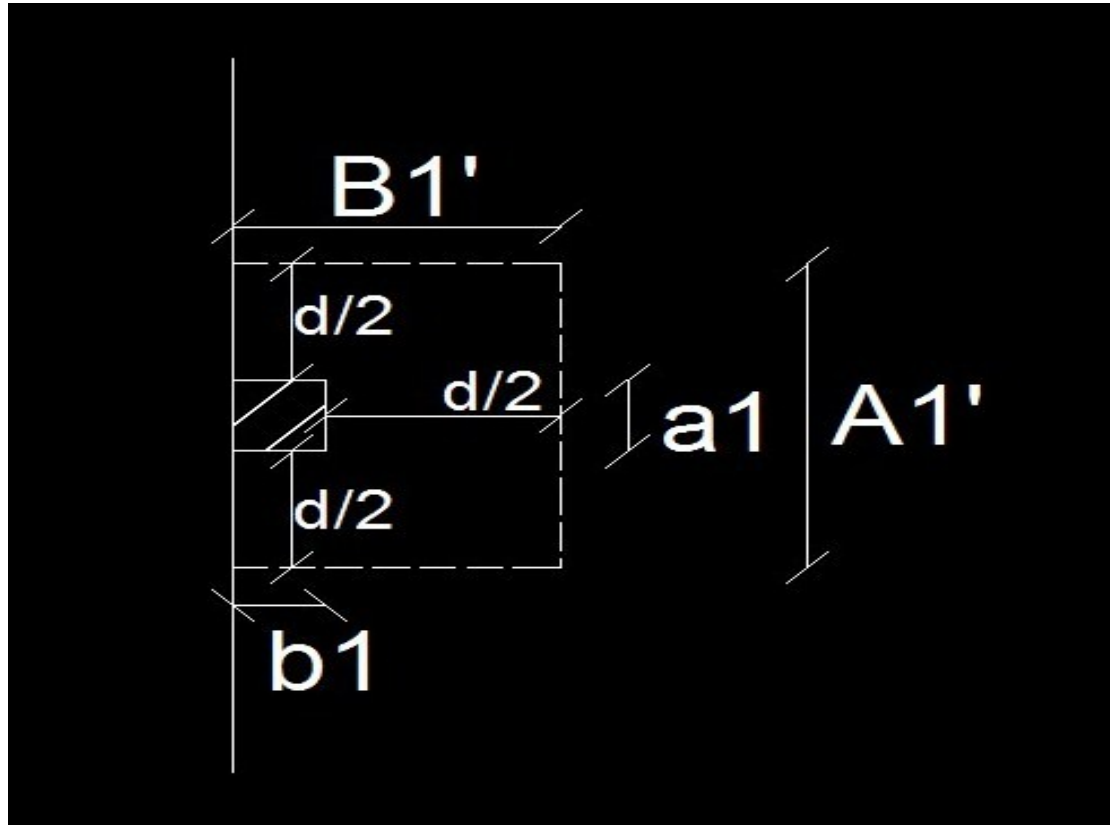
If $q_{cu} < q_{sh}$ un safe increase depth

$$\text{Take } d = \frac{Q_{sh}}{(q_{cu} * B)} = \dots \text{ cm}$$

$$t = d + \text{cover}$$

cover =(5 to 10 cm)

Check Punching:



$$q_{un} = \frac{\sum P_{ult}}{\text{Area}} = \dots \text{ KN/m}^2$$

$$Q_p = P_u - q_u (A' * B') = \dots \text{ Ton}$$

حيث أن :

$P_u \rightarrow$ ton أعلى حمل عمود في الشريحة بوحدّة

$$A' = (a_1 + d) = \dots \text{ m}$$

$$B' = (b_1 + d) = \dots \text{ m}$$

$a \rightarrow$ عرض العمود , $b \rightarrow$ طول العمود

$$q_p = \frac{Q_p}{2*(A'+B')*d} = \dots \text{ kg/cm}^2$$

حيث أن:

$$q_{pcu} = \left(0.5 + \frac{b}{a}\right) \sqrt{\frac{F_{cu}}{\lambda c}} = \dots \text{ kg/cm}^2$$

حيث أن:

If $q_{pcu} > q_p$ ok safe

If $q_{pcu} < q_p$ un safe → increase depth

$t = d + \text{cover}$

cover = (5 to 10 cm)

Reinforcement of the footing:

$$A_{s \text{ Top1}} = \frac{M_{\text{top}}}{J*d*F_y} = \dots \text{ cm}^2 / B' = /m'$$

$$A_{s \text{ Top2}} = \frac{M_{\text{top}}}{J*d*F_y} = \dots \text{ cm}^2 / B' = /m'$$

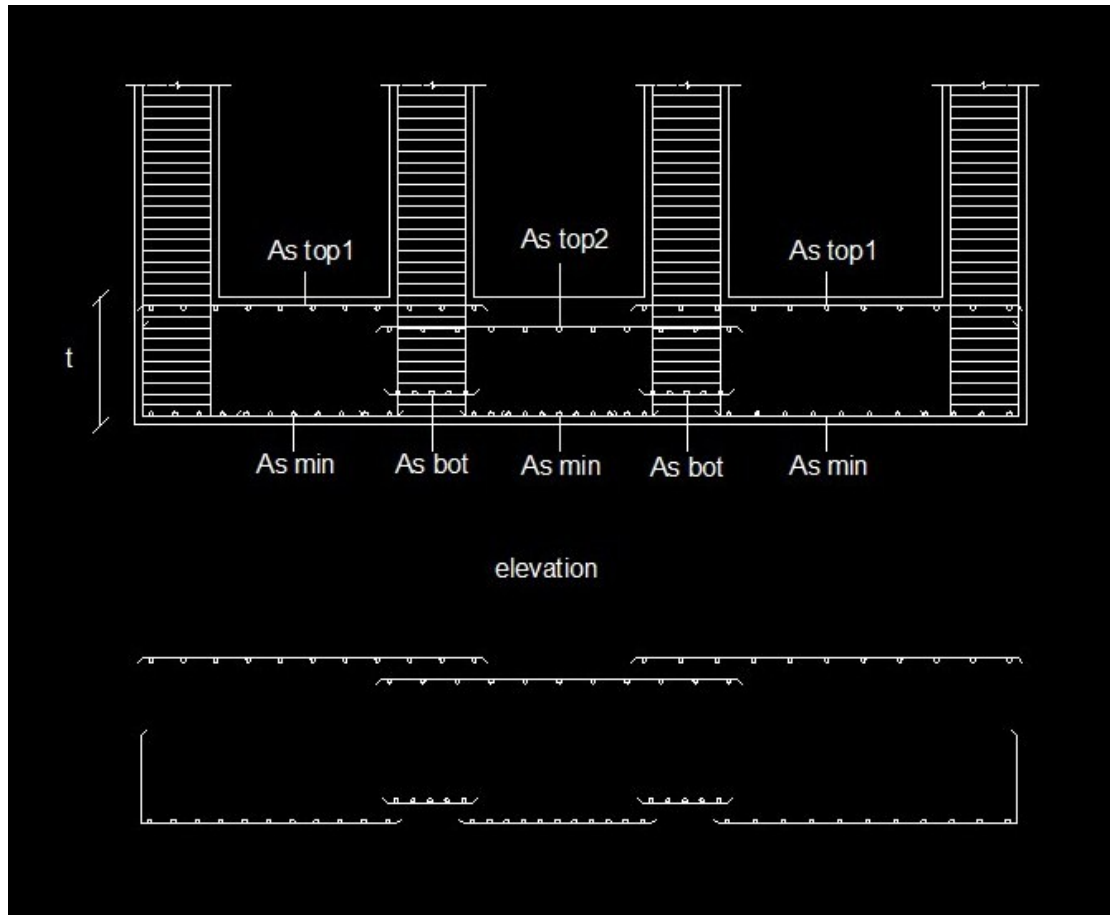
$$A_{s \text{ Bot}} = \frac{M_{\text{bot}}}{J*d*F_y} = \dots \text{ cm}^2 / B' = /m'$$

حيث أن:

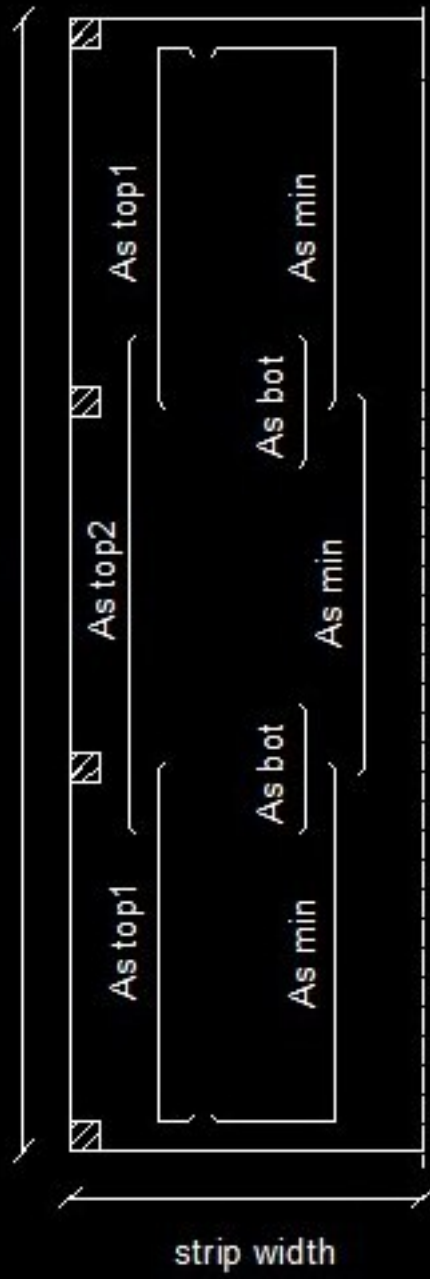
Mutop ← أعلي عزم علوي

Mubot ← أعلي عزم سفلي

Details of Reinforcement:



strip length



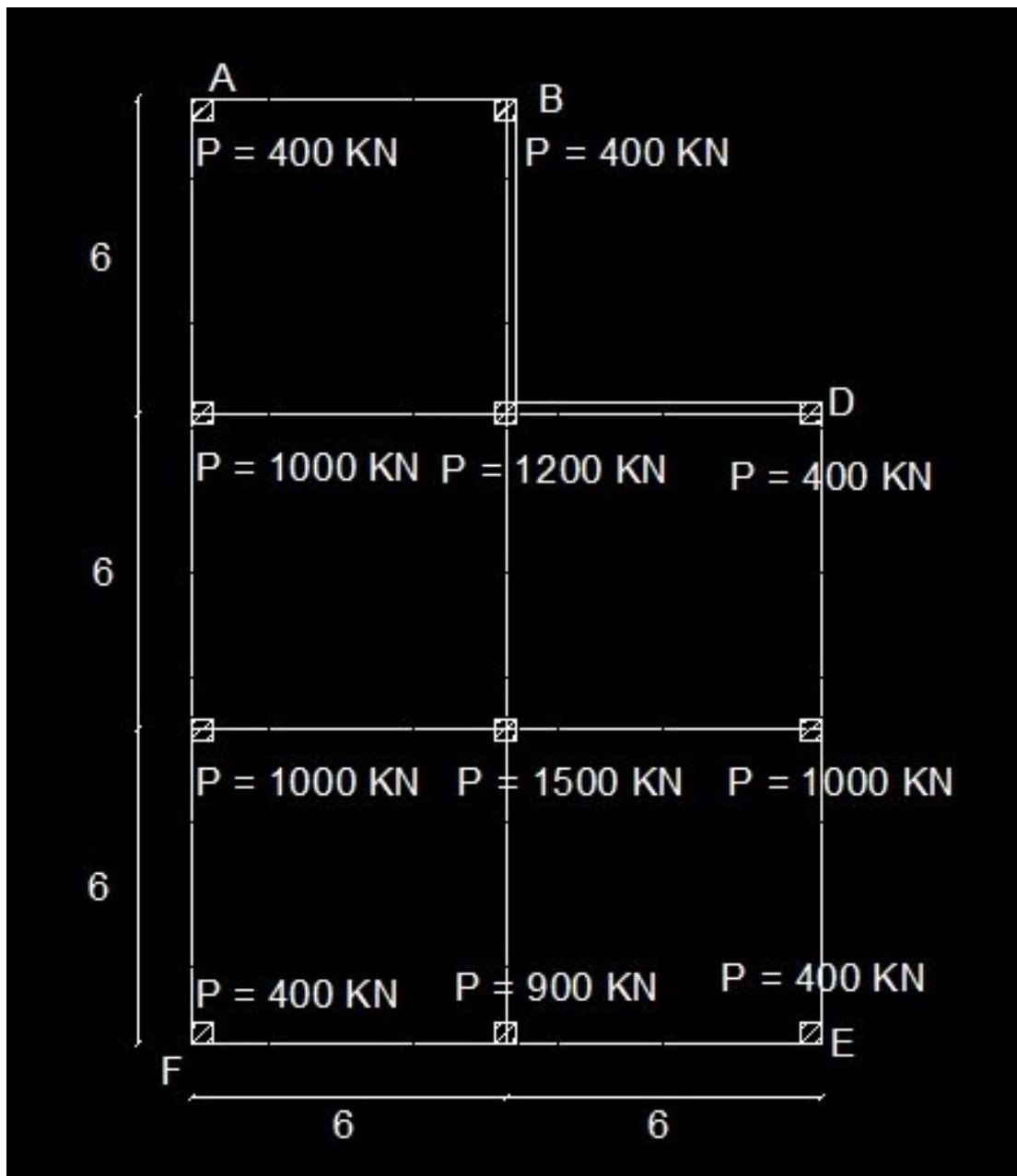
plan

Example: 1

The Raft footing shown in fig all columns 40 X 40 cm .

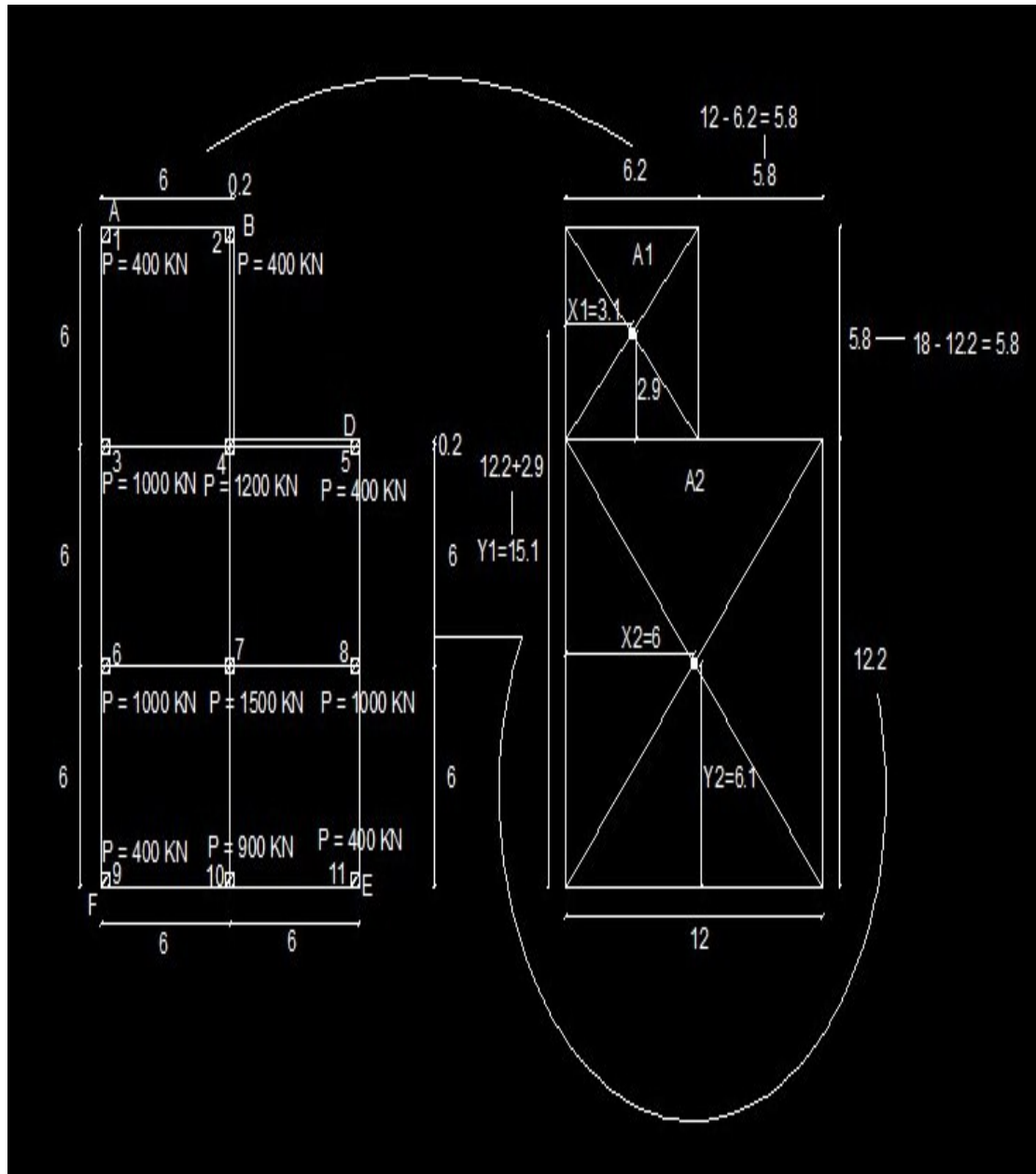
It is required to:

- 1) Determine the soil pressure under the corners of the given Raft.
- 2) Make Full design for strip AF take strip width=3m.
- 3) Determine the reinforcement steel of the Raft footing .
- 4) Draw net sketch showing dimensions of Raft footing and steel details.



Solution

Given: $f_{cu} = 250 \text{ kg/cm}^2$, $F_y = 3600 \text{ kg/cm}^2$



نلاحظ أن الشكل غير متماثل فيتم تقسيم الشكل

$$A_1 = 6.2 * 5.8 = 35.96 \text{ m}^2$$

$$A_2 = 12.2 * 12 = 146.4 \text{ m}^2$$

Area	X	Y	A*X	A*Y
35.96	3.1	15.1	111.5	543
146.40	6	6.1	878.4	893
182.36			989.9	1436
Σ Area			$\Sigma A*X$	$\Sigma A*Y$

1) Determination of C.G of Raft:

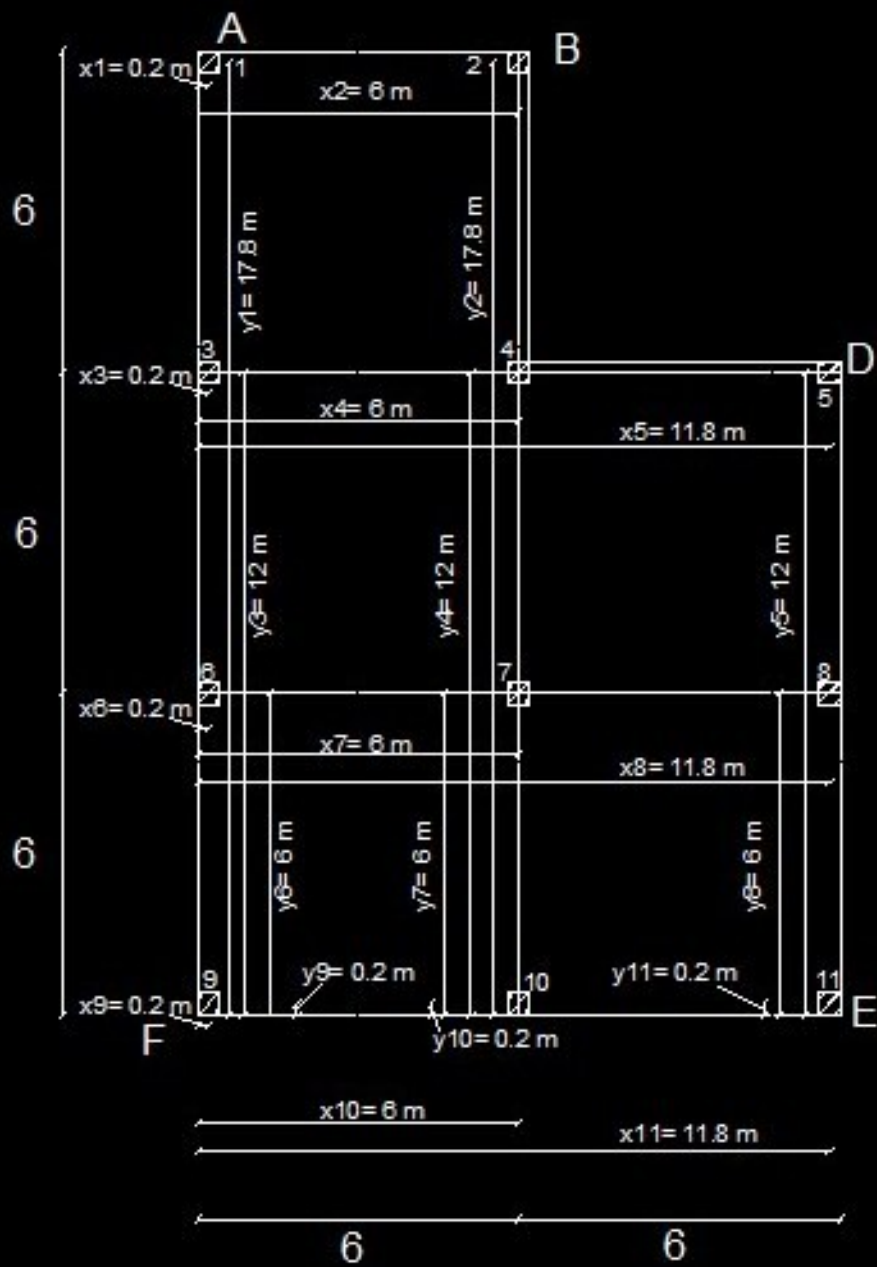
تحديد C.G للبشة.

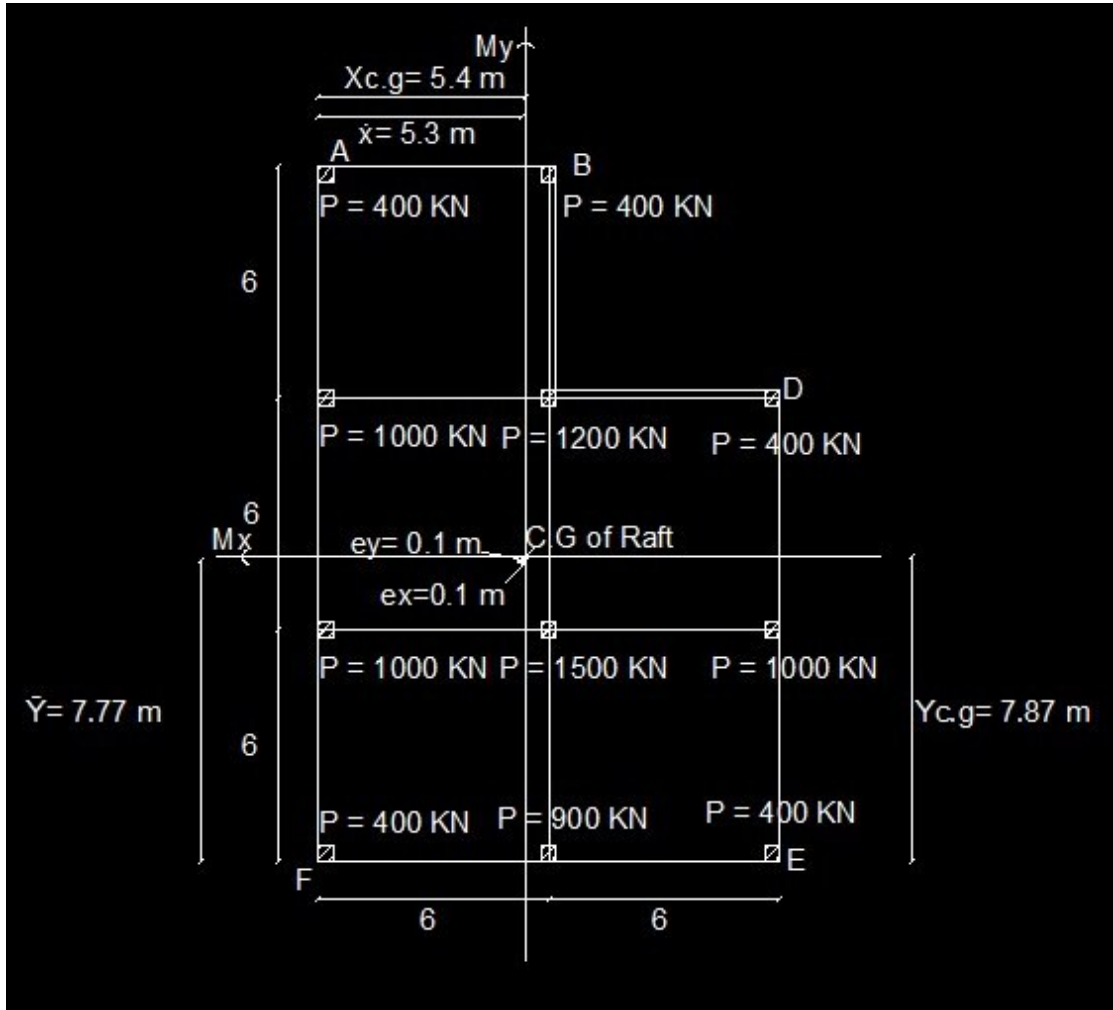
$$X_{C.G} = \frac{\Sigma A*X}{\Sigma Area} = \frac{989.9}{182.36} = 5.4 \text{ m}$$

$$Y_{C.G} = \frac{\Sigma A*Y}{\Sigma Area} = \frac{1436}{182.36} = 7.87 \text{ m}$$

2) Determination of Resultant Load and its point of application:

تحديد محصلة القوي (أحمال الأعمدة) ونقطة تأثيرها.





Col N.o	P (KN)	X	Y	P*X	P*y
1	400	0.2	17.8	80	7120
2	400	6	17.8	2400	7120
3	1000	0.2	12	200	12000
4	1200	6	12	7200	14400
5	400	11.8	12	4720	4800
6	1000	0.2	6	200	6000
7	1500	6	6	9000	9000
8	1000	11.8	6	11800	6000
9	400	0.2	0.2	80	80
10	900	6	0.2	5400	180
11	400	11.8	0.2	4720	80
	8600			45800	66780
	ΣP			$\Sigma P*X$	$\Sigma P*Y$

$$\bar{X} = \frac{\Sigma P*X}{\Sigma P} = \frac{45800}{8600} = 5.3 \text{ m}$$

$$\bar{Y} = \frac{\Sigma P*Y}{\Sigma P} = \frac{66780}{8600} = 7.77 \text{ m}$$

3) Determination the value and direction determined:

تحديد قيمة واتجاه العزم:

$$e_x = X_{C.G} - \bar{X} = 5.4 - 5.3 = 0.1 \text{ m}$$

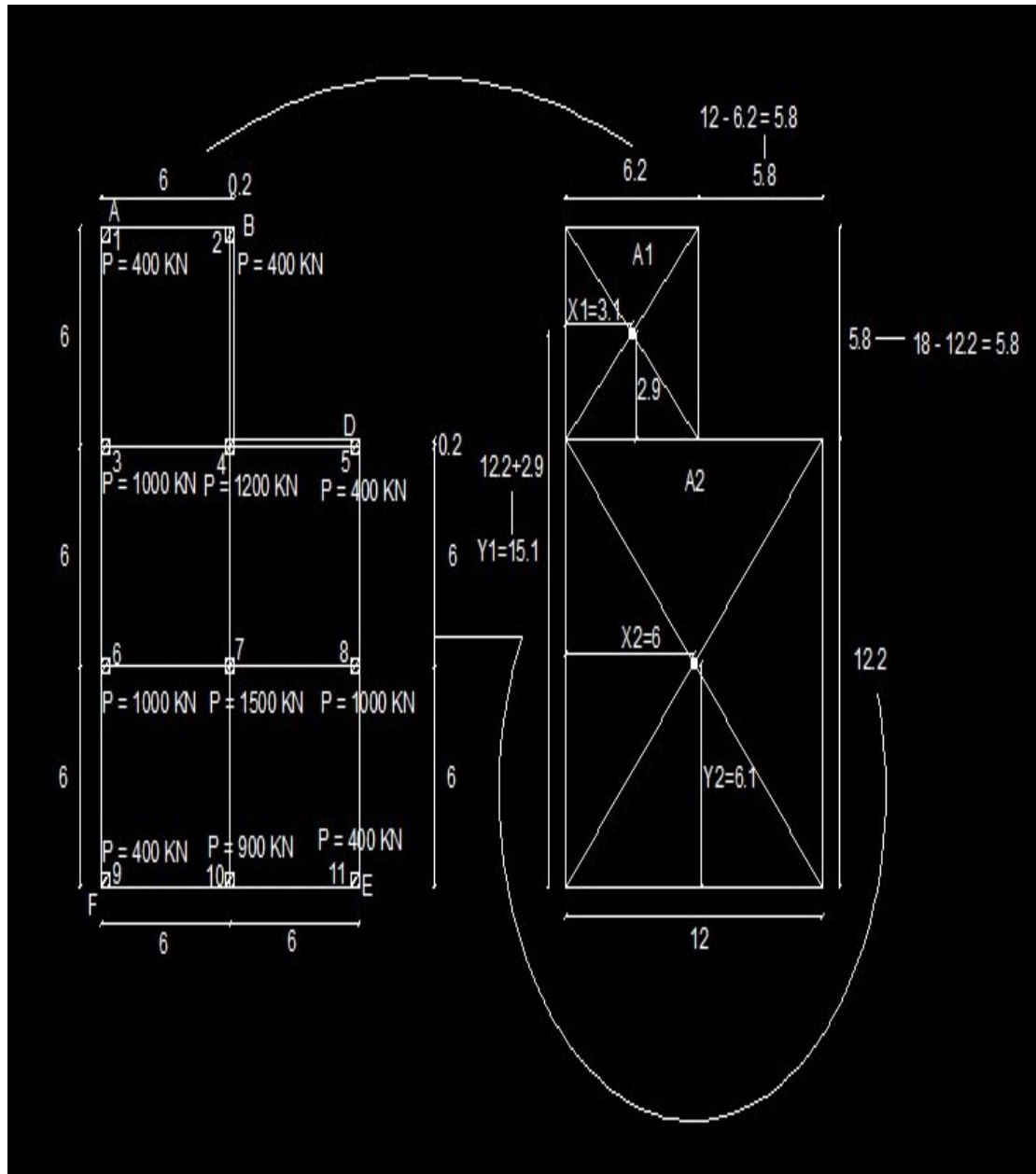
$$e_y = Y_{C.G} - \bar{Y} = 7.87 - 7.77 = 0.1 \text{ m}$$

$$M_x = \sum P * e_y = 8600 * 0.1 = 860 \text{ KN.m}$$

$$M_y = \sum P * e_x = 8600 * 0.1 = 860 \text{ KN.m}$$

4) Calculate the soil pressure at the points required:

$$\sigma = \frac{-N}{A} \pm \frac{M_x}{I_x} * y \pm \frac{M_y}{I_y} * x = \dots \text{ KN/m}^2$$



نلاحظ أن الشكل غير متماثل فيتم تقسيم الشكل

$$A_1 = 6.2 * 5.8 = 35.96 \text{ m}^2$$

$$A_2 = 12.2 * 12 = 146.4 \text{ m}^2$$

$$\text{Area of Raft (A)} = \sum \text{Area} = 182.36 \text{ m}^2$$

For A_1 :

$$A_1 = 6.2, B_1 = 5.8, Y_{C.GA1} = 15.1, Y_{C.G} = 7.87$$

For A_2 :

$$A_2 = 12, B_2 = 12.2, Y_{C.GA2} = 6.1, Y_{C.G} = 7.87$$

$$I_X = \left\{ \frac{A_1 \cdot (B_1)^3}{12} + A_1 \cdot (Y_{C.GA1} - Y_{C.G})^2 \right\} + \left\{ \frac{A_2 \cdot (B_2)^3}{12} + A_2 \cdot (Y_{C.GA2} - Y_{C.G})^2 \right\} = \dots \text{ m}^4$$

$$\begin{aligned} I_X &= \left\{ \frac{6.2 \cdot (5.8)^3}{12} + 35.96 \cdot (15.1 - 7.87)^2 \right\} + \left\{ \frac{12 \cdot (12.2)^3}{12} + 146.4 \cdot (6.1 - 7.87)^2 \right\} \\ &= (100.81 + 1879.73) + (1815.85 + 458.66) \\ &= 4255 \text{ m}^4 \end{aligned}$$

For A_1 :

$$A_1 = 5.8, B_1 = 6.2, X_{C.GA1} = 3.1, X_{C.G} = 5.4$$

For A_2 :

$$A_2 = 12.2, B_2 = 12, X_{C.GA2} = 6, X_{C.G} = 5.4$$

$$I_y = \left\{ \frac{A_1 \cdot (B_1)^3}{12} + A_1 \cdot (X_{C.GA1} - X_{C.G})^2 \right\} + \left\{ \frac{A_2 \cdot (B_2)^3}{12} + A_2 \cdot (X_{C.GA2} - X_{C.G})^2 \right\} = \dots \text{ m}^4$$

$$I_y = \left\{ \frac{5.8 \cdot (6.2)^3}{12} + 35.96 \cdot (3.1 - 5.4)^2 \right\} + \left\{ \frac{12.2 \cdot (12)^3}{12} + 146.4 \cdot (6 - 5.4)^2 \right\}$$

$$= (115.19 + 190.23) + (1756.8 + 52.7)$$

$$= 2115 \text{ m}^4$$

$$\sigma = \frac{-N}{A} \pm \frac{M_x}{I_x} \cdot y \pm \frac{M_y}{I_y} \cdot x = \dots \text{ KN/m}^2$$

$$\sigma_A = \frac{-8600}{182.36} + \frac{860}{4255} \cdot (18 - 7.87) - \frac{860}{2115} \cdot 5.4$$
$$= -47.3 \text{ KN/m}^2$$

$$\sigma_D = \frac{-8600}{182.36} + \frac{860}{4255} \cdot (12.2 - 7.87) + \frac{860}{2115} \cdot (12 - 5.4)$$
$$= -43.6 \text{ KN/m}^2$$

$$\sigma_F = \frac{-8600}{182.36} - \frac{860}{4255} \cdot (7.87) - \frac{860}{2115} \cdot (5.4)$$

$$= -51 \text{ KN/ m}^2$$

$$\begin{aligned}\sigma_E &= \frac{-8600}{182.36} - \frac{860}{4255} * (7.87) + \frac{860}{2115} * (12-5.4) \\ &= -46 \text{ KN/ m}^2\end{aligned}$$

6)Raft Foundation Design:

For strip AF

strip width=3m

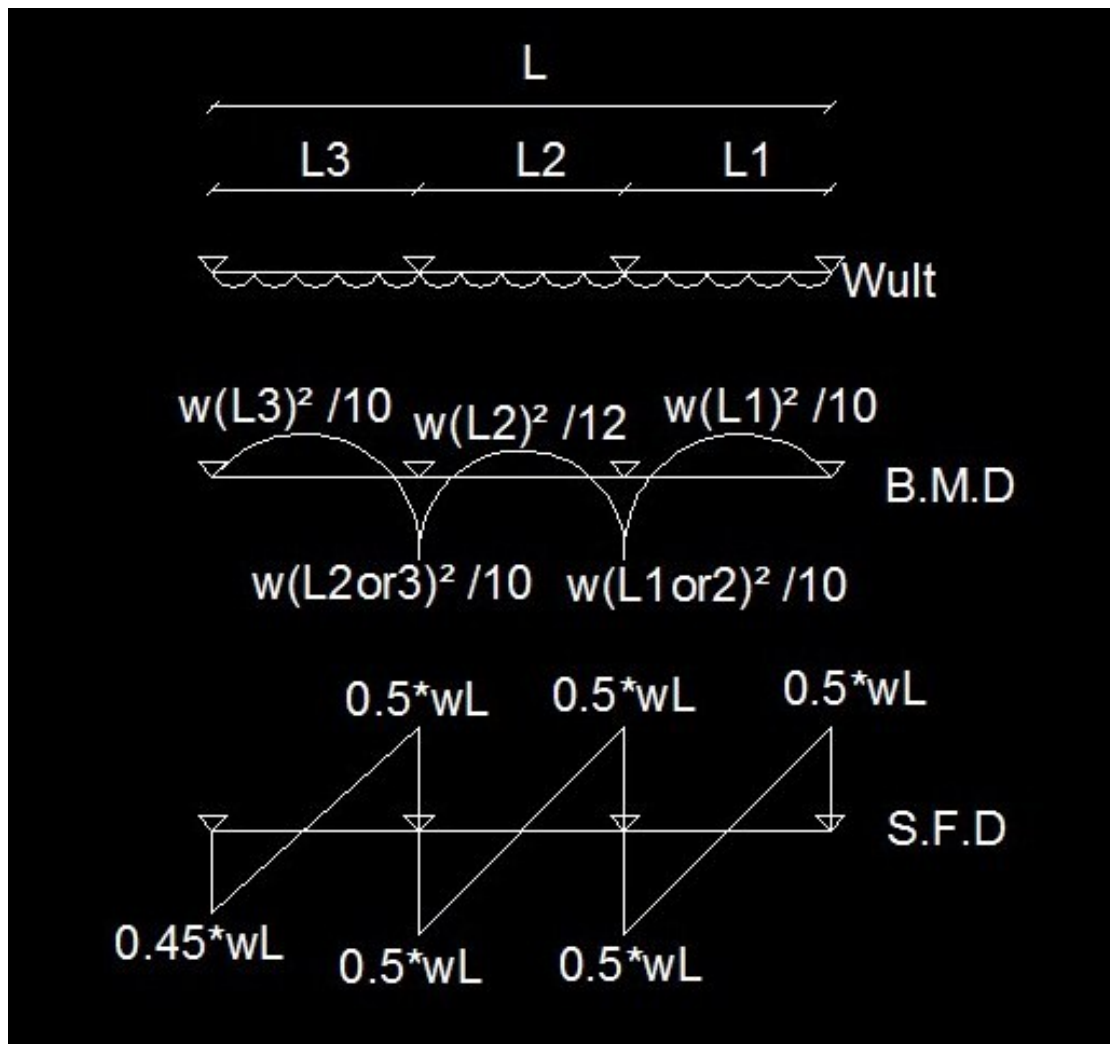
Method (2):

$$\sum P w = 400+1000+1000+400 = 2800 \text{ KN}$$

$$L = 3*6 = 18 \text{ m}$$

$$\begin{aligned}W &= \frac{\sum Pw}{L} = \frac{2800}{18} = 155.56 \text{ KN/B} \\ &= 15.56 \text{ t/B}\end{aligned}$$

$$W_U = W * 1.5 = 15.56 * 1.5 = 23.33 \text{ t/B}$$



$$M_{ult} = \frac{w(L)^2}{10} = \frac{23.33(6)^2}{10} = 84 \text{ mt}$$

$$M_{ult} = \frac{w(L)^2}{12} = \frac{23.33(6)^2}{12} = 70 \text{ mt}$$

$$M_{max} = 84 \text{ mt}$$

$$Q = 0.45 \cdot wL = 0.45 \cdot 23.33 \cdot 6 = 63 \text{ t}$$

$$Q = 0.5 \cdot wL = 0.5 \cdot 23.33 \cdot 6 = 70 \text{ t}$$

$$Q_{\max} = 70 \text{ t}$$

$$d = C_1 \sqrt{\frac{\text{Mult}}{F_{cu} * B}} = 5 \sqrt{\frac{84 * 10^5}{250 * 300}} = 53 \text{ cm} \cong 60 \text{ cm}$$

Check Shear:

$$Q_{sh} = Q_{\max} - \left(\frac{d}{2}\right) * w_{ult} = 70 - \left(\frac{0.6}{2}\right) * 23.33 = 63 \text{ ton}$$

$$q_{sh} = \frac{Q_{sh}}{B * d} = \frac{63 * 10^3}{300 * 60} = 3.5 \text{ kg/cm}^2$$

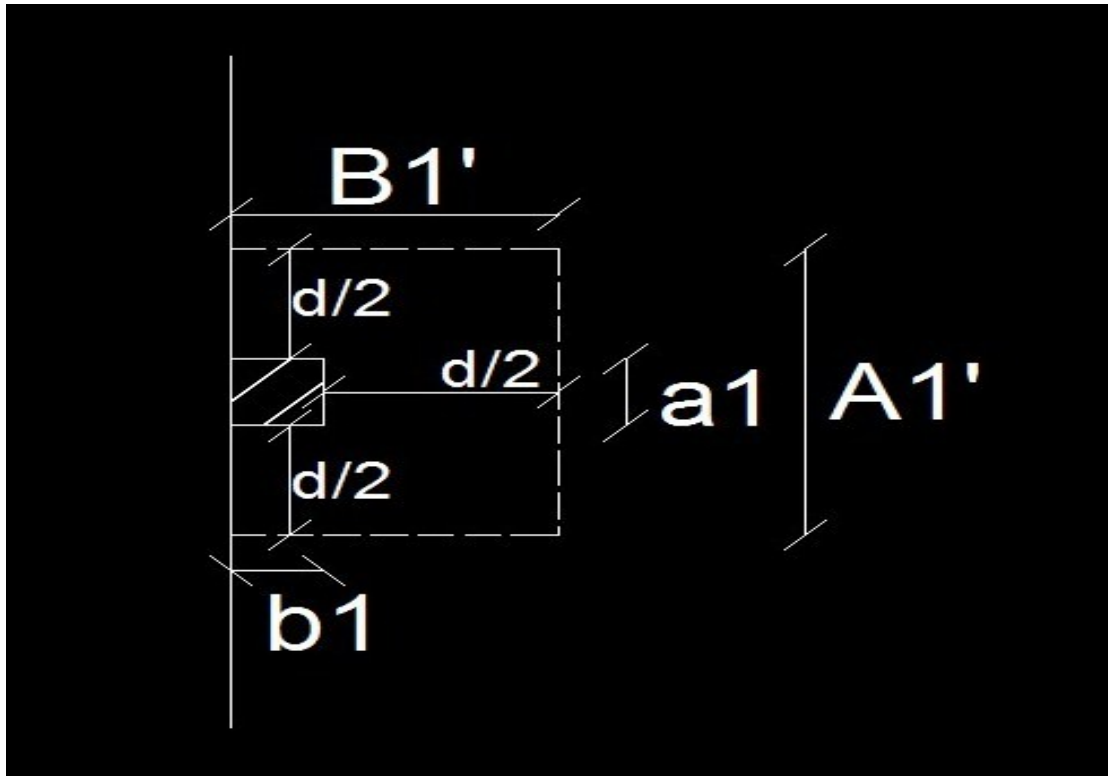
$$q_{cu} = 0.4 * \sqrt{F_{cu}} = 0.4 * \sqrt{250} = 6.3 \text{ kg/cm}^2$$

$$q_{cu} > q_{sh}$$

6.3 > 3.5 ok safe

$$t = d + \text{cover} = 60 + 10 = 70 \text{ cm}$$

Check Punching:



$$q_{un} = \frac{\sum P_{ult}}{\text{Area}} = \frac{8600}{182.36} = 47.2 \text{ KN/m}^2 \cong 4.72 \text{ t/m}^2$$

$$Q_p = P_u - q_u (A' * B') = \dots \text{ Ton}$$

$$A' = (a_1 + d) = 0.4 + 0.6 = 1 \text{ m}$$

$$B' = (b_1 + \frac{d}{2}) = (0.4 + \frac{0.6}{2}) = 0.7 \text{ m}$$

$$Q_p = 100 - 4.72 (1 * 0.7) = 96.7 \text{ Ton}$$

$$q_p = \frac{Q_p}{2 * (A' + B') * d} = \frac{96.7 * 10^3}{2 * (100 + 70) * 60} = 4.74 \text{ kg/cm}^2$$

$$q_{pcu} = (0.5 + \frac{b}{a}) \sqrt{\frac{F_{cu}}{\lambda c}} = (0.5 + \frac{0.4}{0.4}) \sqrt{\frac{250}{1.5}}$$

$$=19.36 \text{ kg/cm}^2$$

$$q_{pcu} > q_p$$

$$19.36 > 4.74 \text{ ok safe}$$

$$t = d + \text{cover} = 60 + 10 = 70 \text{ cm}$$

Reinforcement of the footing:

$$\begin{aligned} A_{s \text{ Top1}} &= \frac{M_{\text{top}}}{J \cdot d \cdot F_y} = \dots \text{ cm}^2 / B' = /m' \\ &= \frac{84 \cdot 10^5}{0.826 \cdot 60 \cdot 3600} = 47 \text{ cm}^2 / 3 = 15.6 \text{ cm}^2 / m' \end{aligned}$$

Use 8Y 16 /m'

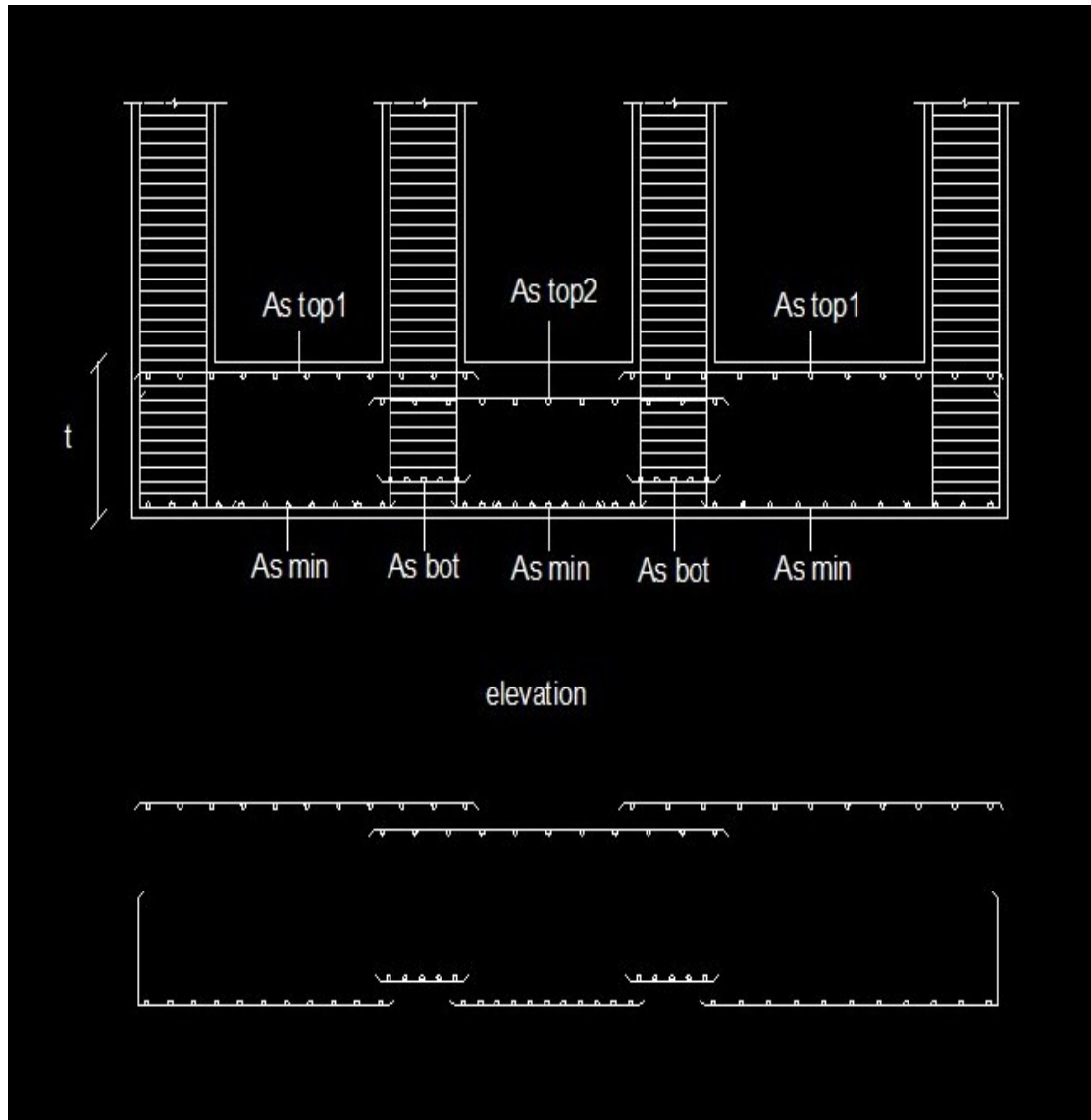
$$\begin{aligned} A_{s \text{ Top2}} &= \frac{M_{\text{top}}}{J \cdot d \cdot F_y} = \dots \text{ cm}^2 / B' = \text{ cm}^2 / m' \\ &= \frac{70 \cdot 10^5}{0.826 \cdot 60 \cdot 3600} = 39 \text{ cm}^2 / 3 = 13 \text{ cm}^2 / m' \end{aligned}$$

Use 7Y 16 /m'

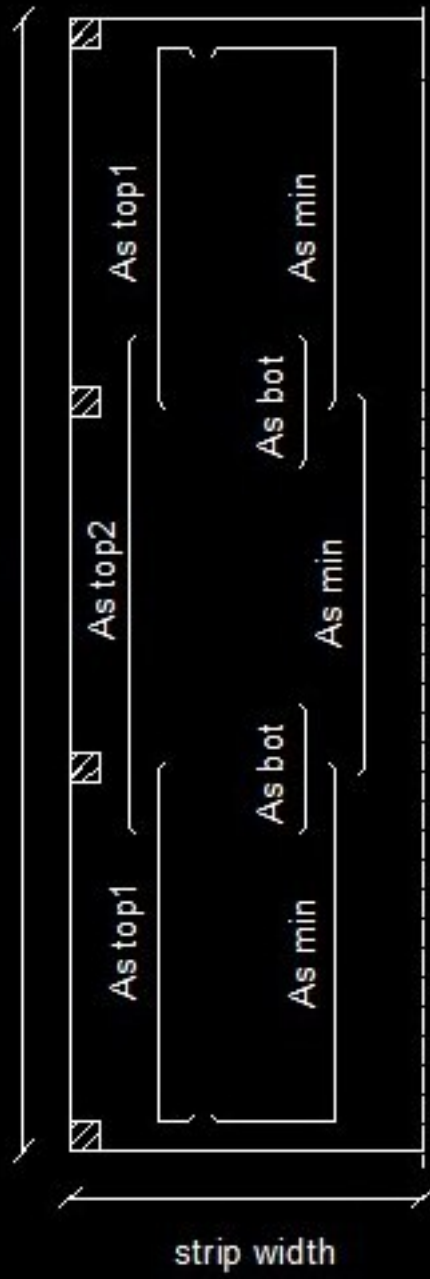
$$\begin{aligned} A_{s \text{ Bot}} &= \frac{M_{\text{bot}}}{J \cdot d \cdot F_y} = \dots \text{ cm}^2 / B' = \text{ cm}^2 / m' \\ &= \frac{84 \cdot 10^5}{0.826 \cdot 60 \cdot 3600} = 47 \text{ cm}^2 / 3 = 15.6 \text{ cm}^2 / m' \end{aligned}$$

Use 8Y 16 /m'

Details of Reinforcement:



strip length



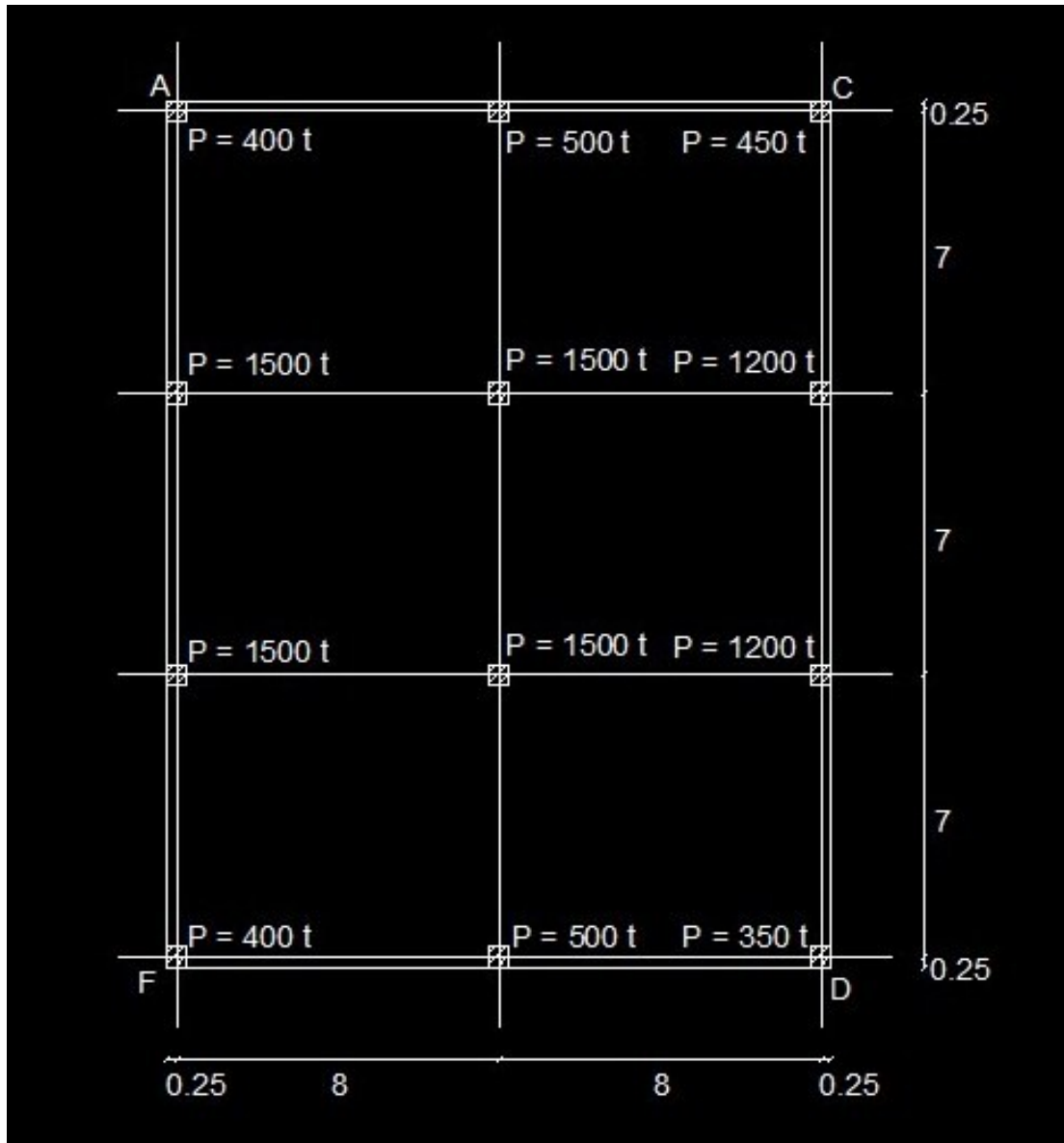
plan

Example: 2

The Raft footing shown in fig all columns 50 X 50 cm .

It is required to:

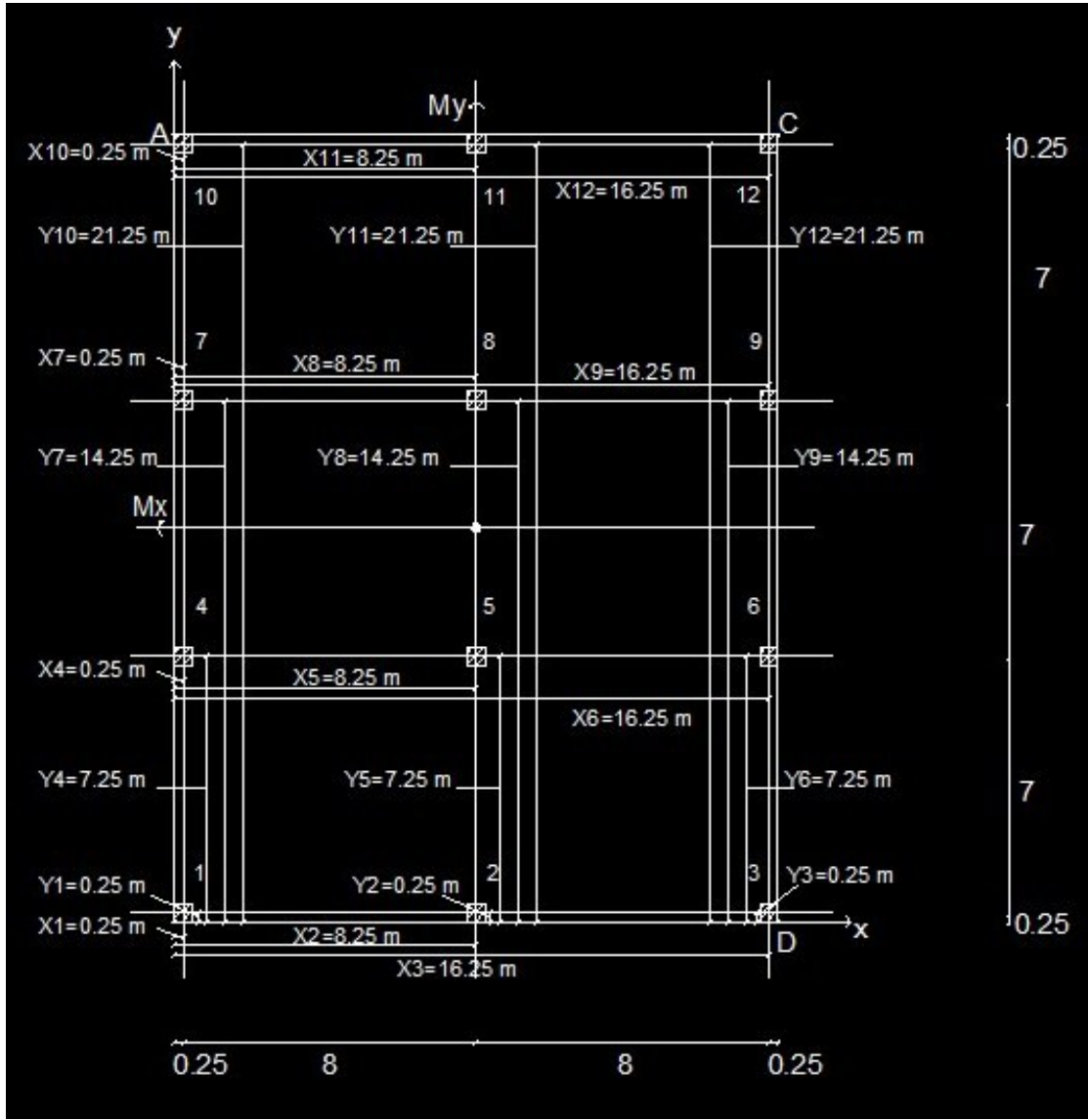
- 1) Determine the soil pressure under the corners of the given Raft.
- 2) Make Full design for strip width=3m.
- 3) Determine the reinforcement steel of the Raft footing .
- 4) Draw net sketch showing dimensions of Raft footing and steel details.

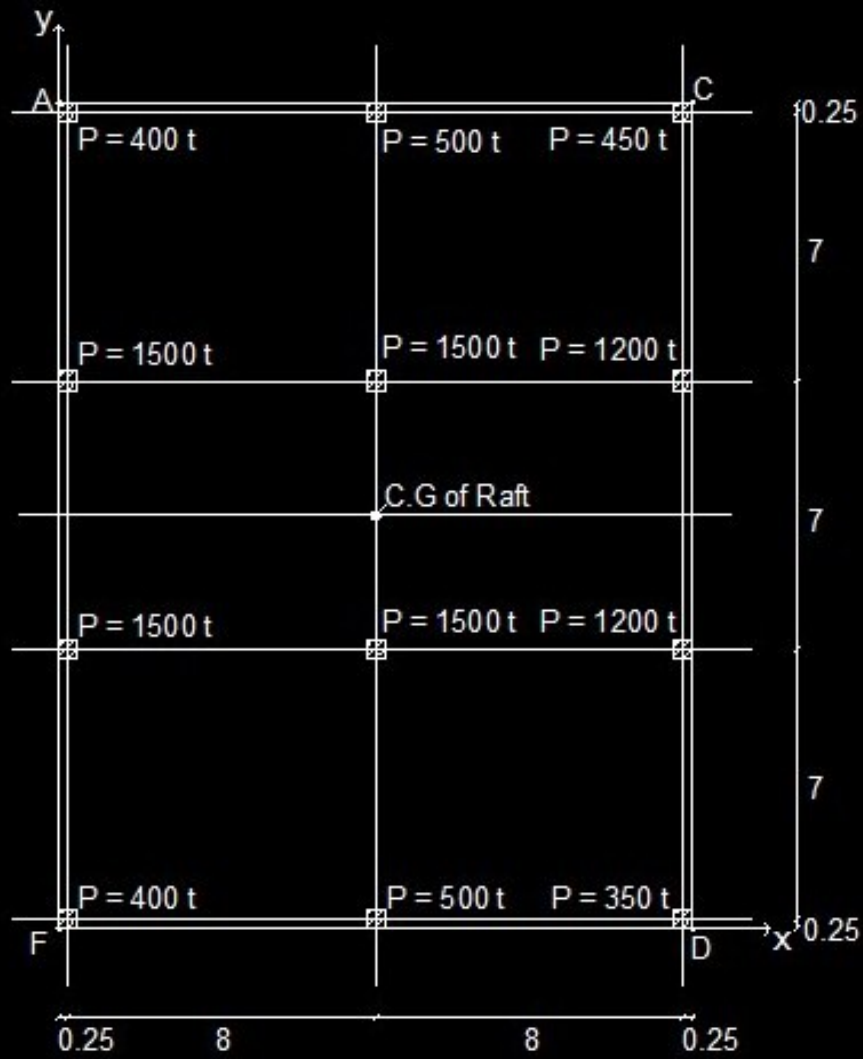


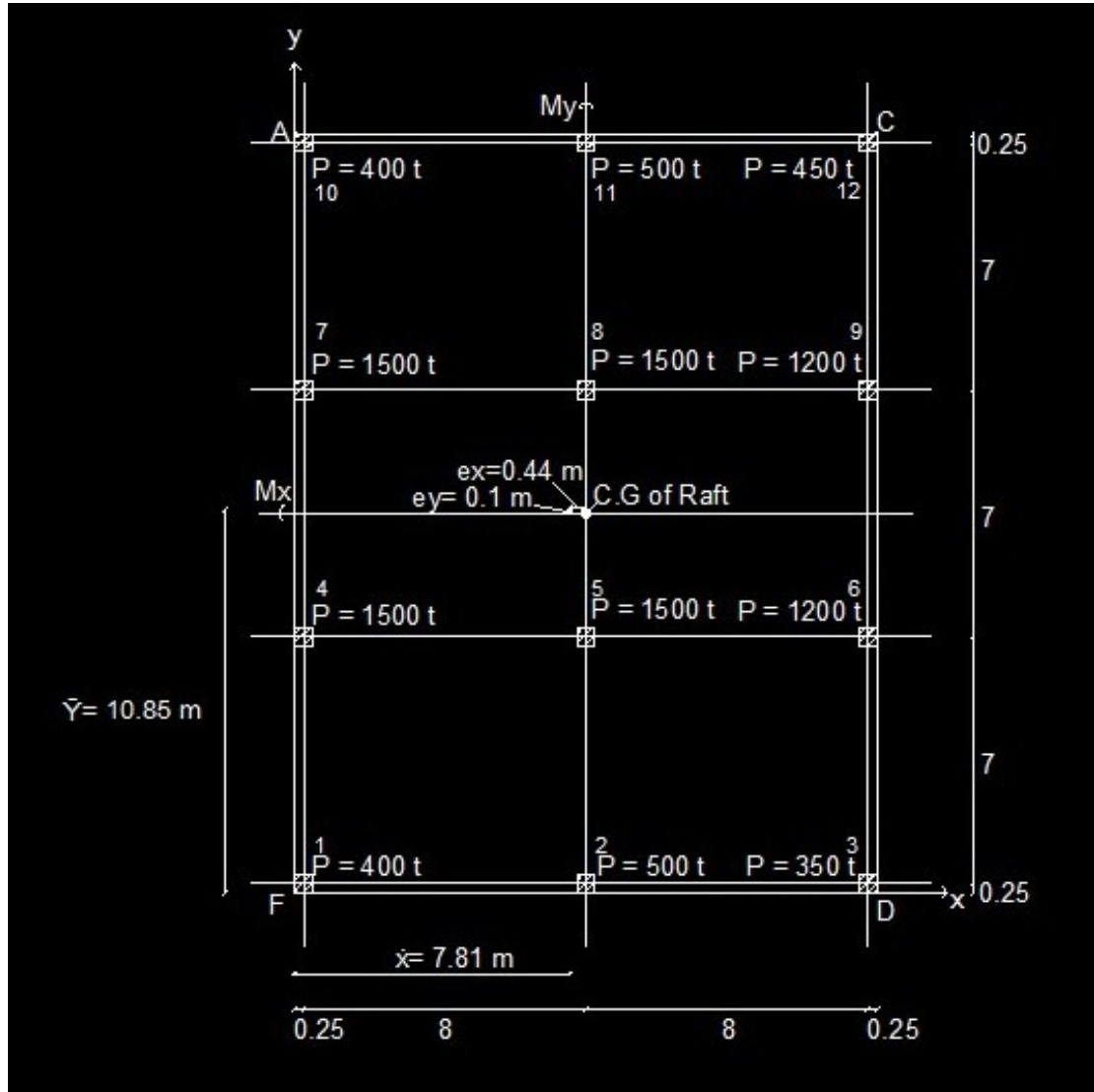
Solution

Given: $f_{cu} = 250 \text{ kg/cm}^2$, $F_y = 3600 \text{ kg/cm}^2$

, $q_{all} = 60 \text{ KN/m}^2$







1) Determination of C.G of Raft:

تحديد C.G للبشة.

2) Determination of Resultant Load and its point of application:

تحديد محصلة القوي (أحمال الأعمدة) ونقطة تأثيرها.

Col N.o	P (KN)	X	Y	P*X	P*y
1	400	0.25	0.25	100	100
2	500	8.25	0.25	4125	125
3	350	16.25	0.25	5687.5	87.5
4	1500	0.25	7.25	375	10875
5	1500	8.25	7.25	12375	10875
6	1200	16.25	7.25	19500	8700
7	1500	0.25	14.25	375	21375
8	1500	8.25	14.25	12375	21375
9	1200	16.25	14.25	19500	17100
10	400	0.25	21.25	100	8500
11	500	8.25	21.25	4125	10625
12	450	16.25	21.25	7312.5	9562.5
	11000			85950	119300
	ΣP			$\Sigma P*X$	$\Sigma P*Y$

$$\bar{X} = \frac{\sum P * X}{\sum P} = \frac{85950}{11000} = 7.81 \text{ m}$$

$$\bar{Y} = \frac{\sum P * Y}{\sum P} = \frac{110300}{11000} = 10.85 \text{ m}$$

3) Determination the value and direction determined:

تحديد قيمة واتجاه العزم:

$$e_x = \frac{A}{2} - \bar{X} = \frac{16.5}{2} - 7.81 = 0.44 \text{ m}$$

$$e_y = \frac{B}{2} - \bar{Y} = \frac{21.5}{2} - 10.85 = 0.1 \text{ m}$$

$$M_x = \sum P * e_y = 11000 * 0.1 = 1100 \text{ KN.m}$$

$$M_y = \sum P * e_x = 11000 * 0.44 = 4840 \text{ KN.m}$$

4) Calculate the soil pressure at the points required:

$$\sigma = \frac{-N}{A} \pm \frac{M_x}{I_x} * y \pm \frac{M_y}{I_y} * x = \dots \text{ KN/m}^2$$

$$\text{Area of Raft (A)} = (A*B)=16.5*21.5= 354.75 \text{ m}^2$$

$$I_x = \frac{A*(B)^3}{12} = \frac{16.5*(21.5)^3}{12} = 13665 \text{ m}^4$$

$$I_y = \frac{B*(A)^3}{12} = \frac{21.5*(16.5)^3}{12} = 8048 \text{ m}^4$$

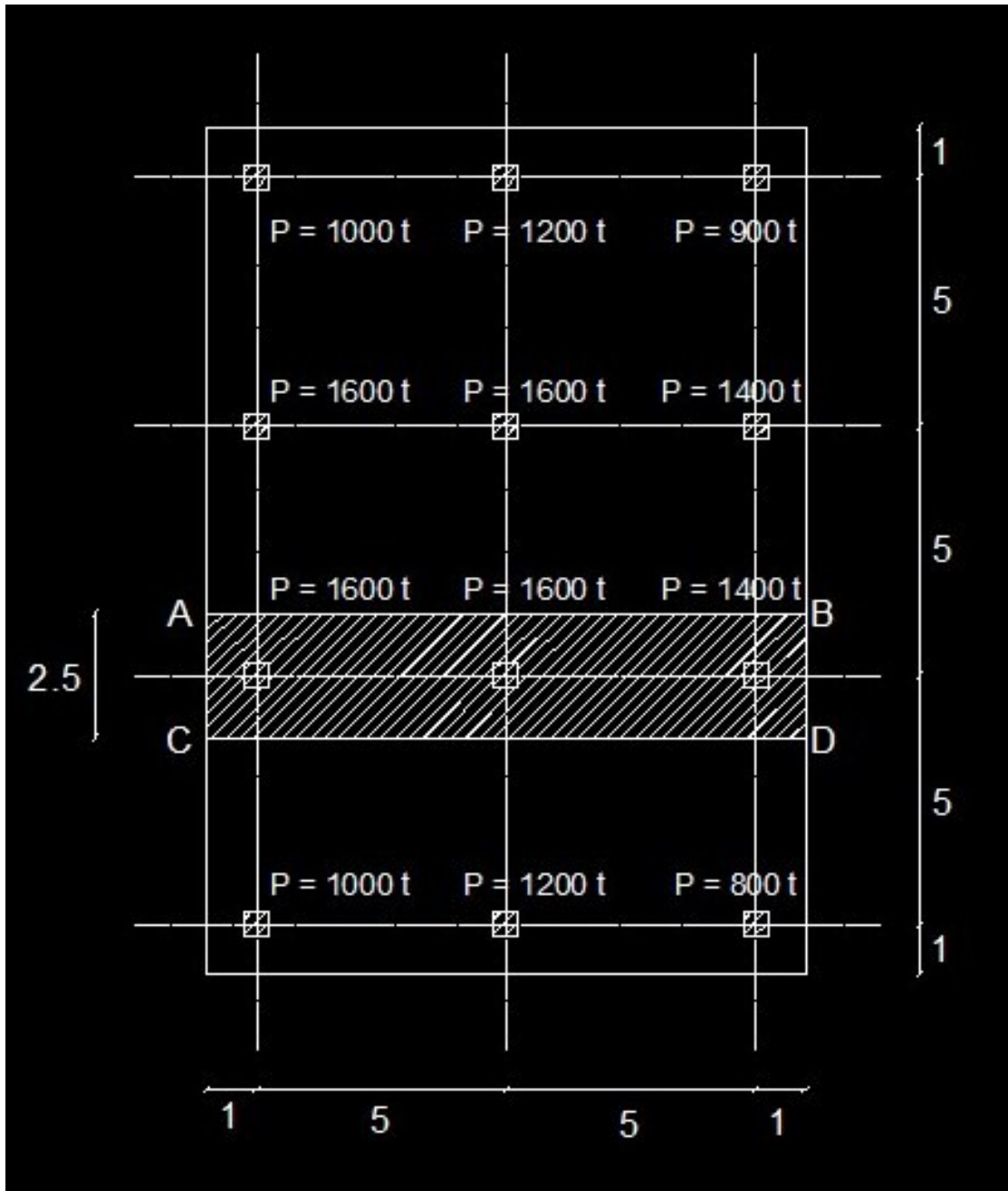
الباقي نفس الشيء

Example: 3

The Raft footing shown in fig all columns 50 X 50 cm .

It is required to:

- 1) Determine the soil pressure under the corners of the given Raft.
- 2) Make Full design for strip ABDC strip width=2.5m.
- 3) Determine the reinforcement steel of the Raft footing .
- 4) Draw net sketch showing dimensions of Raft footing and steel details.



Solution

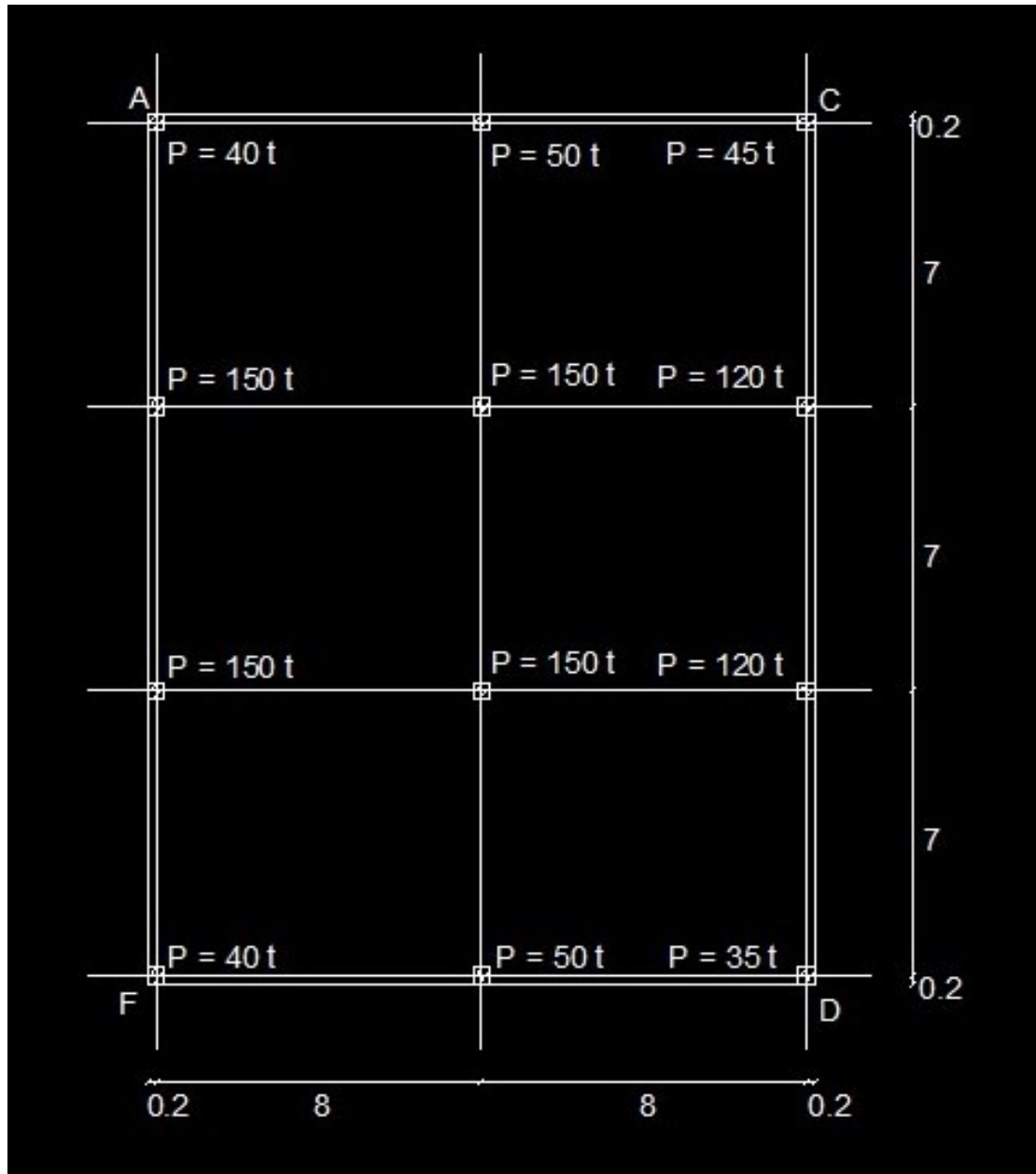
Given: $f_{cu} = 250 \text{ kg/cm}^2$, $F_y = 3600 \text{ kg/cm}^2$

Example: 4

The Raft footing shown in fig all columns 40 X 40 cm .

It is required to:

- 1) Determine the soil pressure under the corners of the given Raft.
- 2) Make Full design for strip width=2.5m.
- 3) Determine the reinforcement steel of the Raft footing .
- 4) Draw net sketch showing dimensions of Raft footing and steel details.



Solution

Given: $f_{cu} = 250 \text{ kg/cm}^2$, $F_y = 3600 \text{ kg/cm}^2$

Piles:

1) Design of piles:

2) Bearing Capacity of piles:

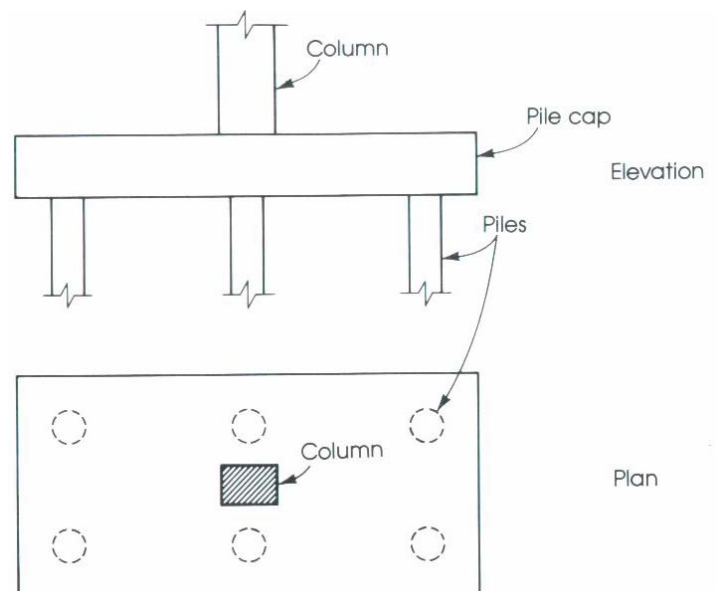
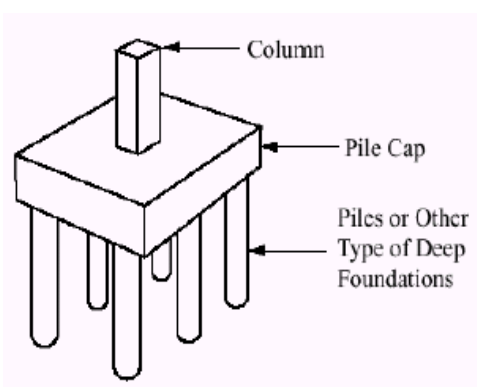
3) Determination settlement:

4) Short and Long pile:

5) Design of piles cap:

6) Design of steel sheet piles:

Piles:



Main reasons For use piles:

1) In case of the top layers are as weak that they could not bear the structure , the piles transfer loads to a good layer at reasonable depth.

عندما تكون الطبقات السطحية ضعيفة بحيث لا تستطيع تحمل أحمال المنشأ تقوم الخوازيق بنقل الحمل إلى الطبقات العميقة الأقوى.

2) In order to resist uplift pressure.

3) In case of structure in water.

في حالات المنشآت المائية.

4) In order to densify the soil as in case of short stone piles.

Types of piles:

1)With respect to the method of transform loads:

A) End Bearing piles.

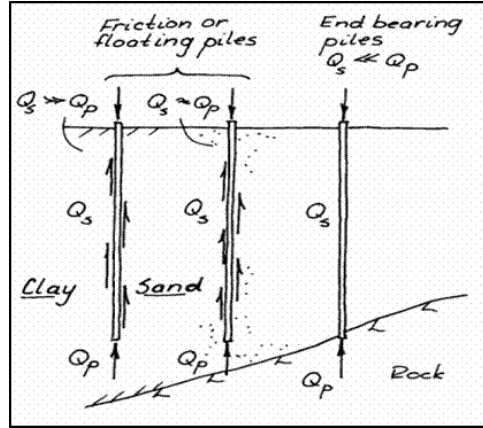
خوازيق ارتكاز: وهذا النوع ينقل الحمل إلى التربة بالمقاومة المتولدة عند نقطة ارتكازه أو قاعدته (Qb).

B) Friction piles.

خوازيق احتكاك: وهذا النوع ينقل الحمل أساسا بمقاومة الاحتكاك على سطحه (Q_s).

C) End Bearing + Friction piles.

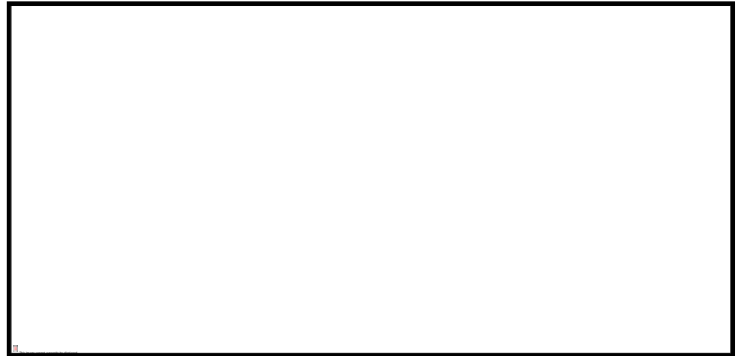
وهذا النوع ينقل الحمل جزئيا بواسطة الاحتكاك على سطحه وجزئيا بمقاومة الارتكاز عند قاعدته (Q_b+Q_s).



End bearing piles

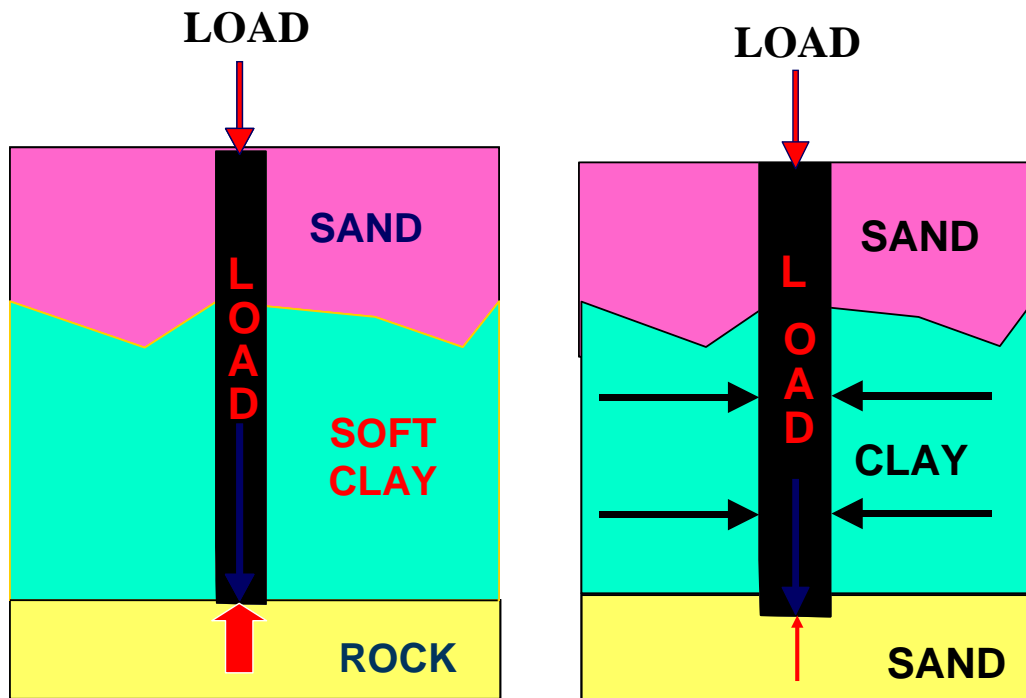


Friction piles



END BEARING PILE

FRICITION PILE

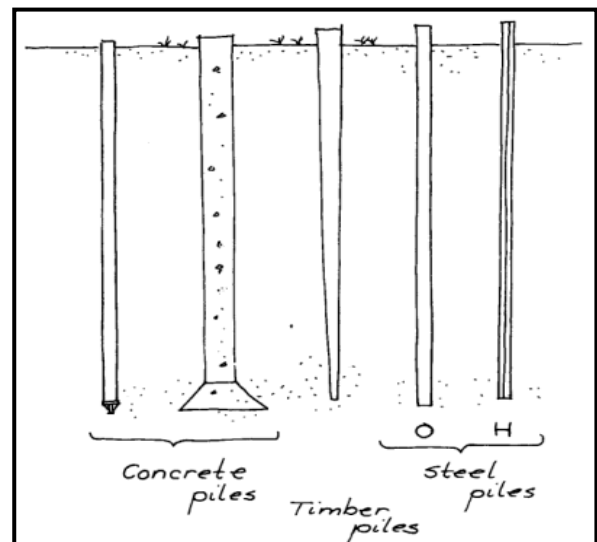
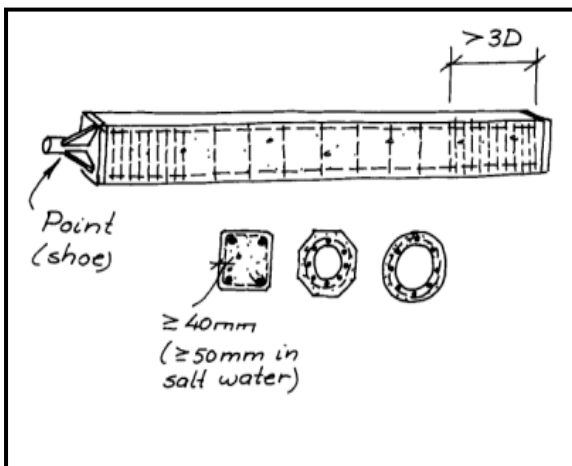


End bearing - Friction

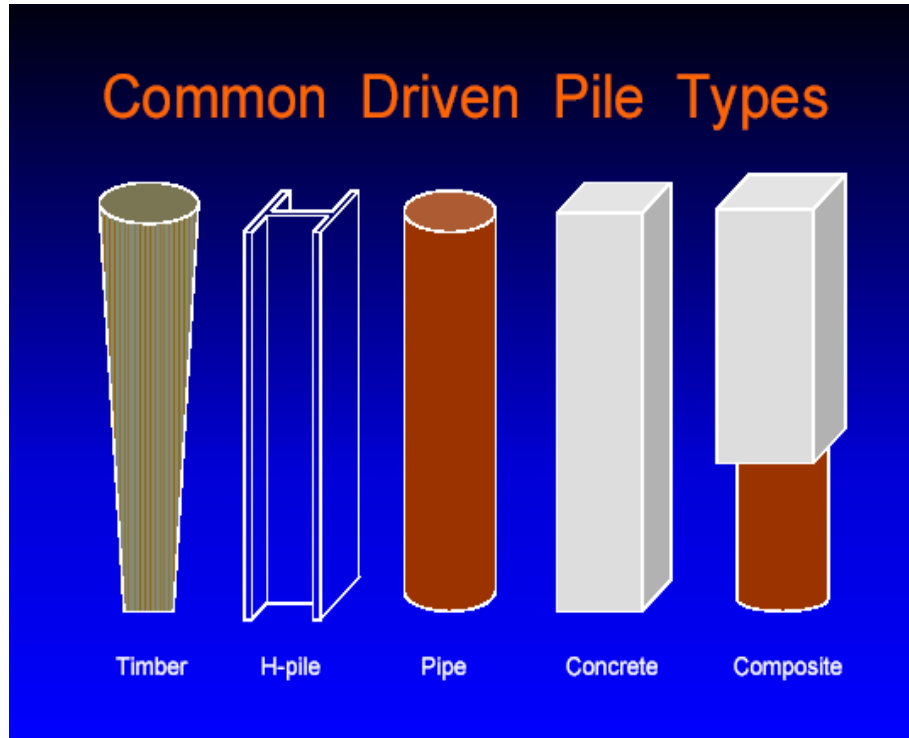
2) With respect to Material:

تصنع الخوازيق من الخرسانة أو الحديد أو الخشب أو أكثر من مادة من هذه المواد.

The main types of materials used for piles are wood, steel and concrete.



Materials used for piles



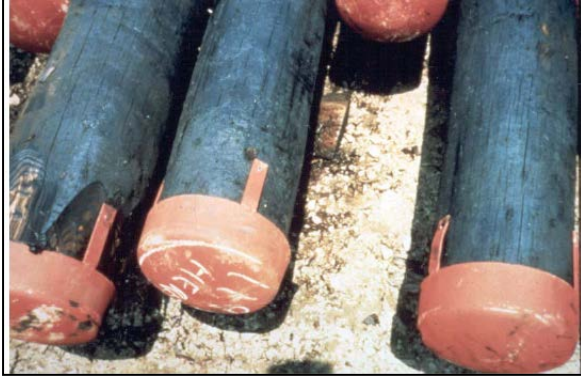
A) Timber piles:

خوازيق خشب:

تستخدم في الأعمال المؤقتة.

Use in temporary works.





Length: 9 → 15 m

Max load: 45 Ton

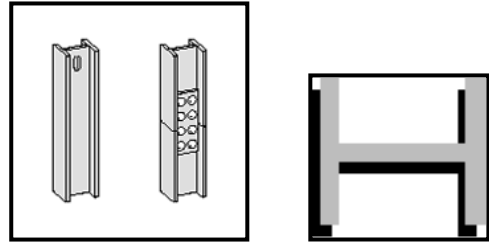
B) Steel piles:

خوازيق حديد:

تستخدم عندما يخترق الخازوق طبقات قوية.

Use when the pile cross hard layers.





Steel Pile – H piles:



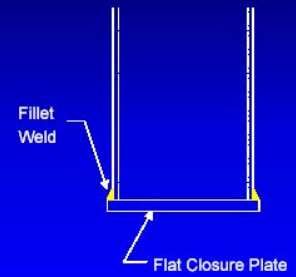
Steel Pipe Pile (Tube piles)



Steel Pipe Pile




Typical Pipe Pile Closure Plate




Steel Pipe Pile


Environmentally friendly techniques
in driving steel pipe piles



NS ECO pile



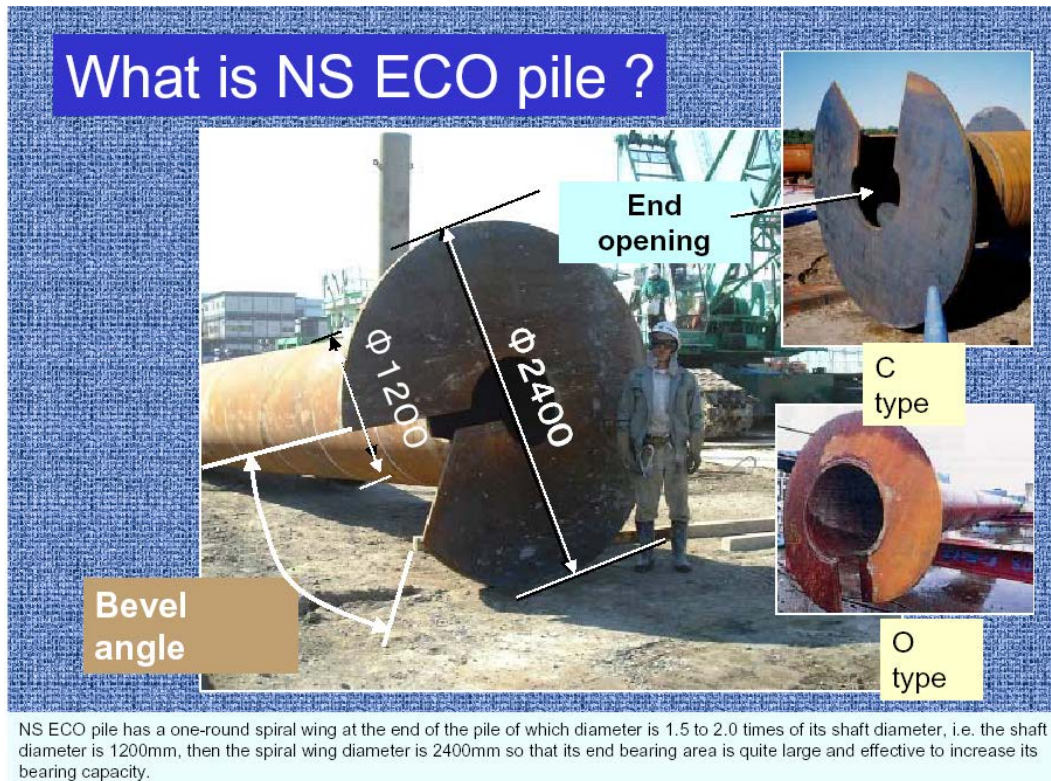
Wing pile



Drill pile

The image displays three different types of steel pipe piles. The "NS ECO pile" is a large, dark, curved pile with a central opening. The "Wing pile" is a pipe with a large, flat, wing-like protrusion on one side. The "Drill pile" is a long, dark pipe with a series of horizontal ridges or grooves along its length.

Steel Pipe Pile



Length: 12 → 50 m

Max load: 35 → 100 Ton

C) Concrete piles:

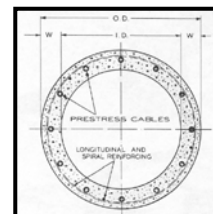
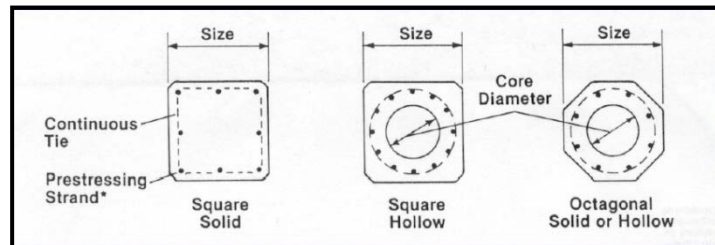
خوازيق خرسانة:

C-1) Pre cast: Driven

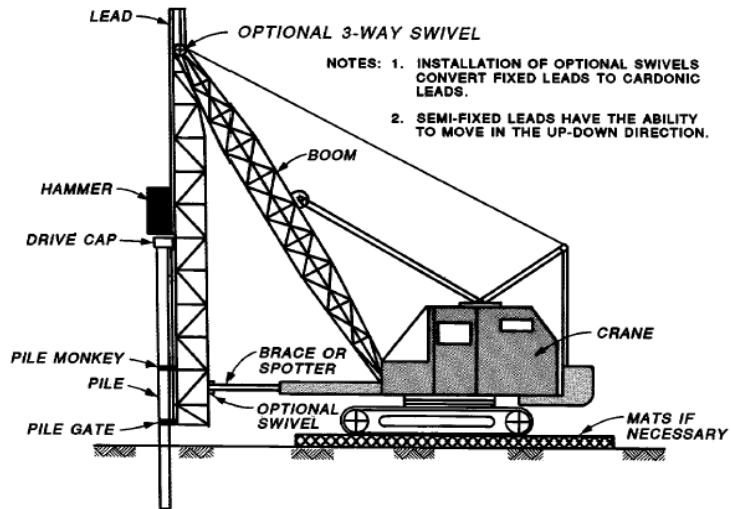
سابقة الصب: بالدق

C-2) Cast in place: Driven , Bored

مصبوب في الموقع :بالحفر والصب

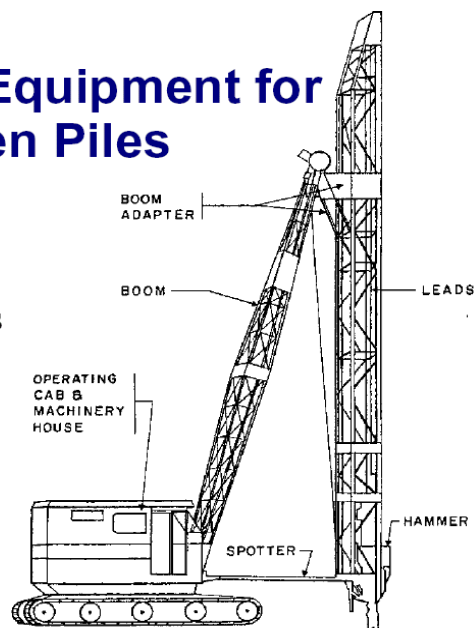






Installation Equipment for Driven Piles

- Pile Driving Rigs
- Pile Hammers
- Hammer Accessories
 - Leaders
 - Cushion Material
- Predrilling, Jetting and Spudding



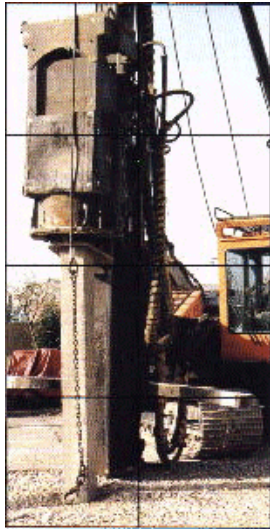
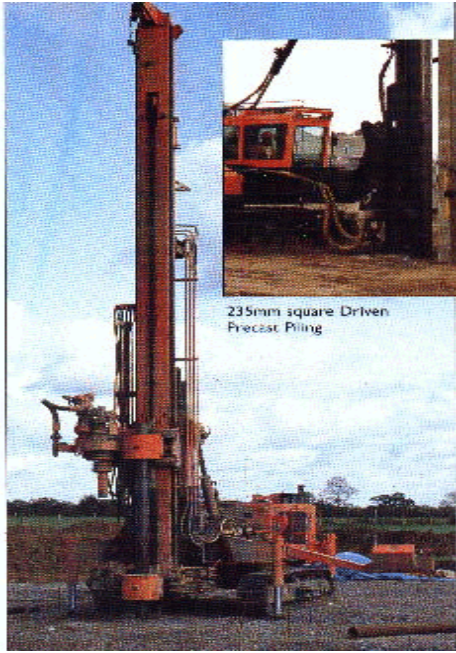
Hammer & Cushion

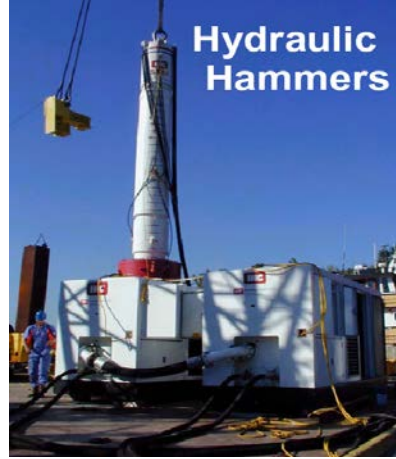
Leads

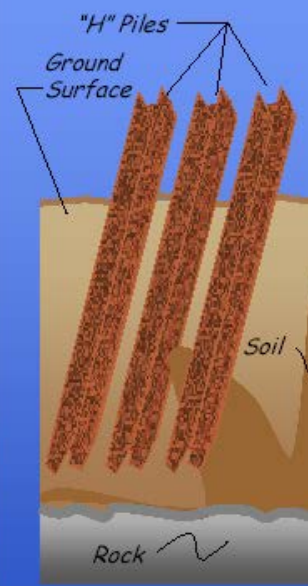
Pile & Cushion

Template









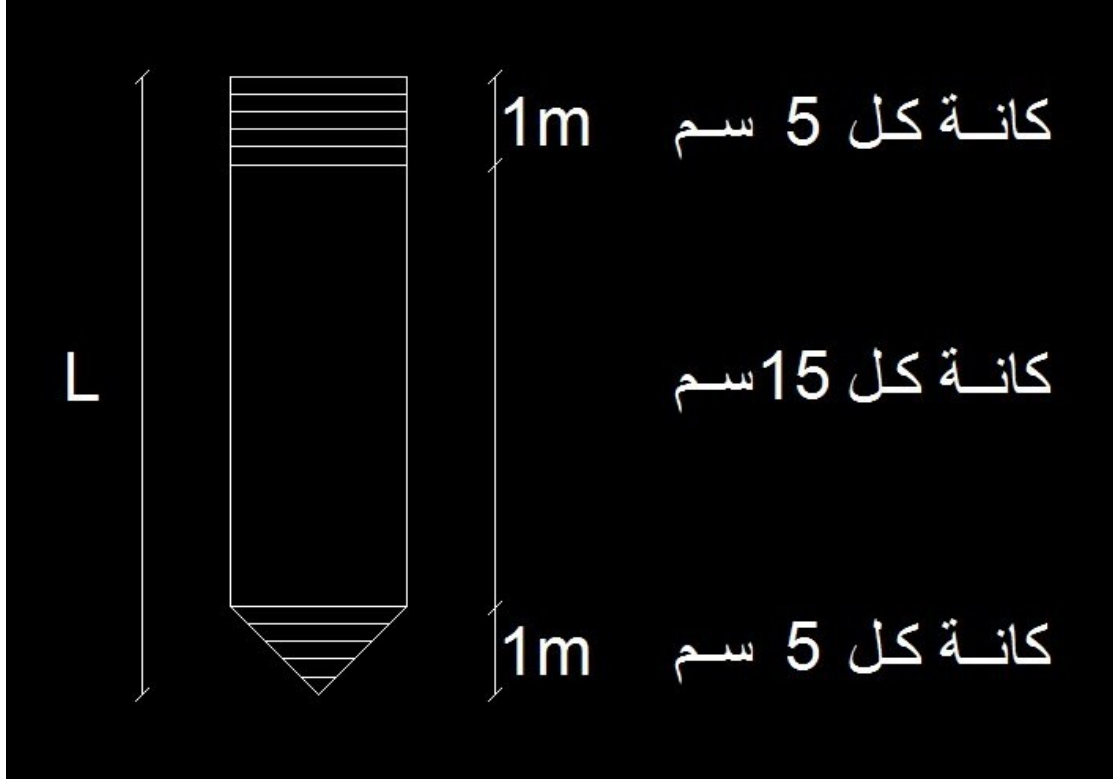
Driven Pile Foundation

Driven Pile Foundation Construction

C-1) Pre cast:

يتطلب تسليح الأجهادات الناتجة عن المناولة والنقل.

Handling stresses.



$$\text{If } \frac{L}{D} \leq 30 \rightarrow A_s = 1.25 \% A_c$$

$$\text{If } 30 < \frac{L}{D} < 40 \rightarrow A_s = 1.5 \% A_c$$

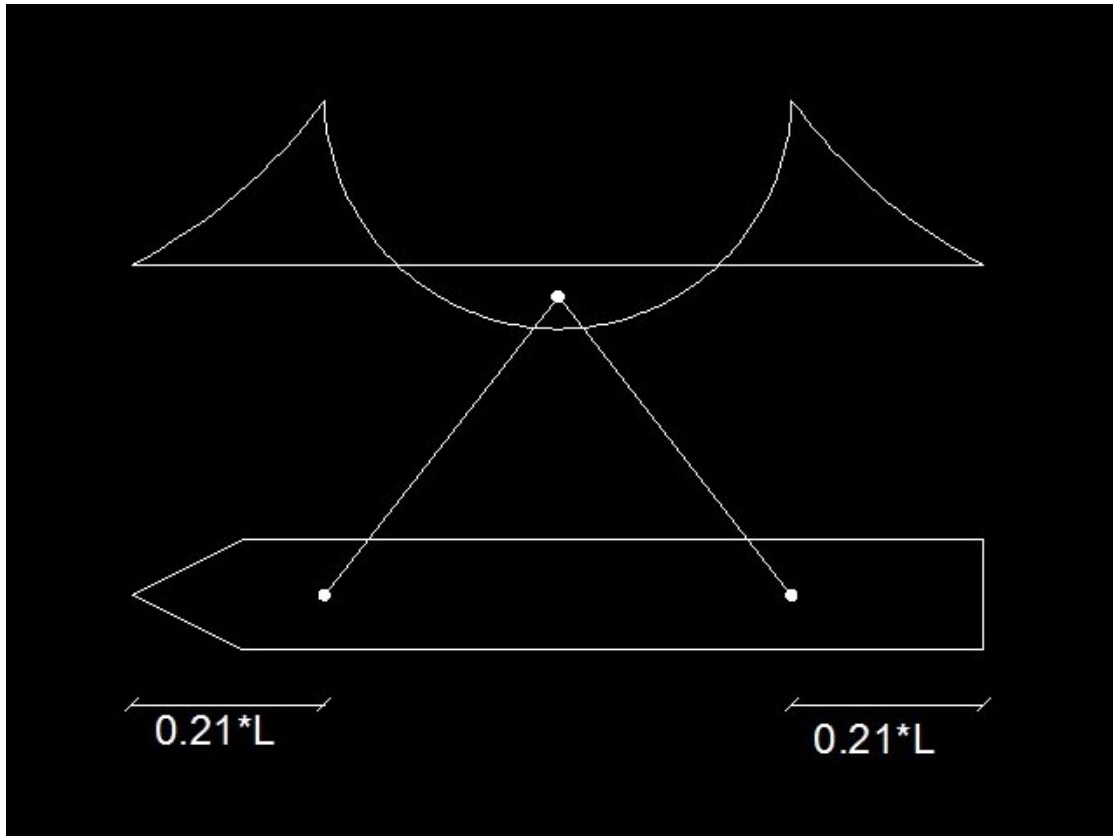
$$\text{If } \frac{L}{D} > 40 \rightarrow A_s = 2 \% A_c$$

حيث أن:

L → طول الخازوق

D → قطر الخازوق

عملية رفع الخازوق:



C-2) Cast in place:

Types of Cast in place pile:

C-2-1) Simplex piles. , C-2-2) Frankie piles.

C-2-3) Vibro piles. , C-2-4) Raymod piles.

C-2-5) Strausse piles.

1) Design of piles:

هناك طريقتين:

1- استخدام اختبار الاختراق القياسي:

Use standard penetration test (S.P.T):

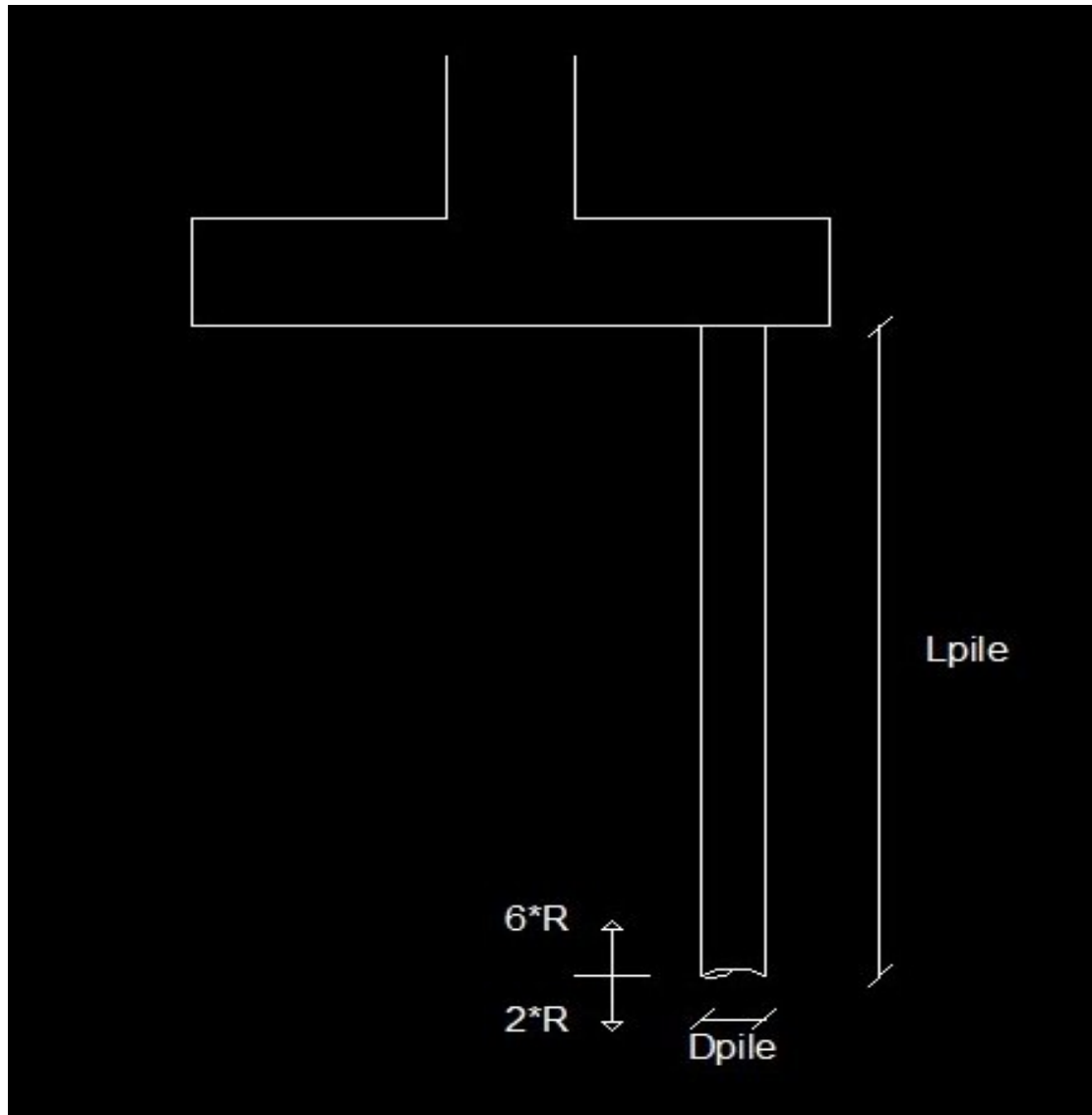
2- استخدام اختبار المخروط الإستاتيكي:

Use cone penetration test (C.P.T):

سيتم دراسة الطريقة الأولى فقط

3- استخدام اختبار الاختراق القياسي:

Use standard penetration test (S.P.T):



Assume:

$$D_{pile} = \dots \text{ cm}$$

$$L_{pile} = \dots \text{ m}$$

$$Q_{all} = 45 \cdot N \cdot \frac{\pi(D_{pile})^2}{4} + \frac{\bar{N}}{3} \cdot \pi \cdot D_{pile} \cdot L_{pile} = \dots \text{ KN}$$

حيث أن:

$Q_{all} \rightarrow$ حمل تشغل الخازوق.

$N \rightarrow$ number of average blows from S.P.T.
tests through depth of 3D above and below
pile tip.

القيمة المتوسطة لعدد الدقات في تجربة الاختراق القياسي في
طبقة التربة المؤثرة علي حمل الارتكاز و الممتدة لمسافة
(2R) أسفل قاعدة الخازوق و (6R) أعلا نقطة الارتكاز.

$\bar{N} \rightarrow$ average number of blows from S.P.T.
tests throughout the pile length subjected to
shear.

متوسط عدد الدقات في تجربة الاختراق القياسي علي طول
الخازوق داخل الطبقة أو الطبقات غير متماسكة الحبيبات.

$D_{pile} \rightarrow$ pile diameter.

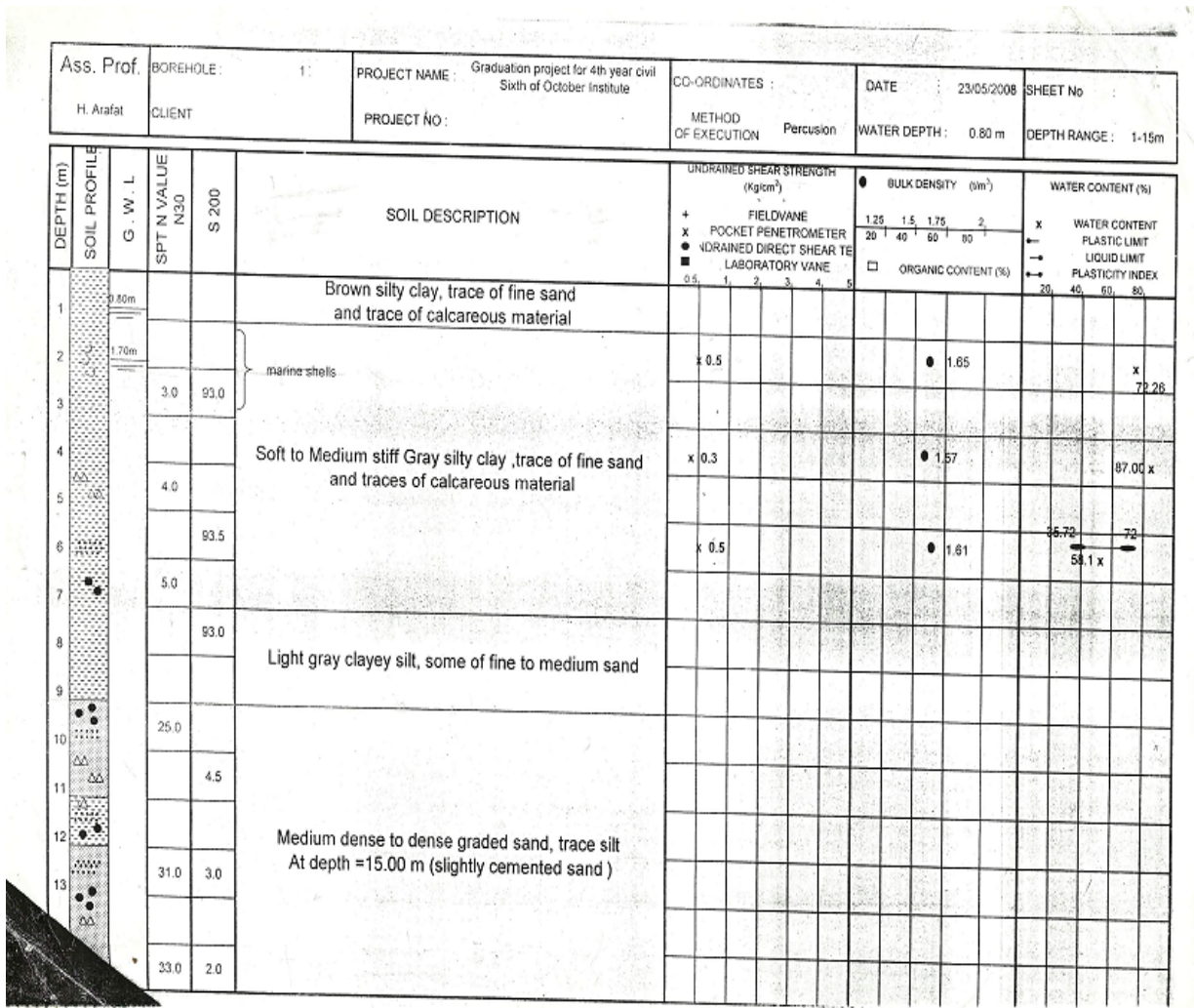
قطر الخازوق.

$L_{pile} \rightarrow$ pile length.

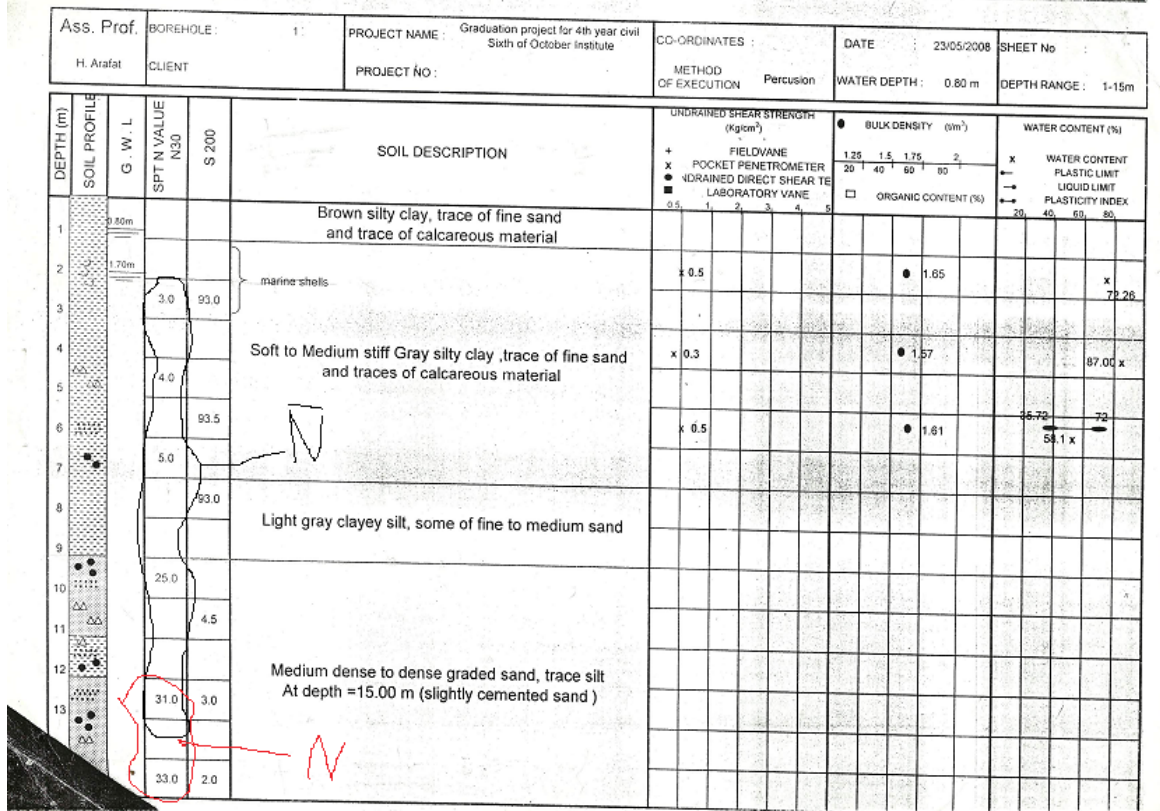
طول الخازوق.

Example: 1

For the inspection of soil Design of piles
Use standard penetration test (S.P.T)



Solution



Assume:

$$D_{\text{pile}} = 40 \text{ cm}$$

$$L_{\text{pile}} = 12 \text{ m}$$

$$Q_{\text{all}} = 45 * N * \frac{\pi(D_{\text{pile}})^2}{4} + \frac{\bar{N}}{3} * \pi * D_{\text{pile}} * L_{\text{pile}}$$

$$N = \frac{31+33}{2} = 32$$

$$\bar{N} = \frac{3+4+5+25+31}{5} = 13.6$$

$$Q_{\text{all}} = 45 * 32 * \frac{\pi(0.4)^2}{4} + \frac{13.6}{3} * \pi * 0.4 * 12 = 249.4 \text{ KN}$$

$$Q_{\text{all}} = 25 \text{ T}$$

2) Bearing Capacity of piles:

Methods of Calculation Bearing Capacity of piles:

- 1) Static formula.
- 2) Dynamic formula.
- 3) Field tests.
- 4) Pile loading test.

سيتم دراسة الطريقة الأولى فقط.

1) Static formula:

For pure clay:

1) Compression:

الخوازيق المعرضة لأحمال ضغط:

$$Q_{ult} = C * N_c * \frac{\pi(D)^2}{4} + C_a * \pi * d * L$$

$$Q_{all} = \frac{Q_{ult}}{F.O.S}$$

$$\text{End Bearing} = C * N_c * \frac{\pi(D)^2}{4}$$

$$\text{Friction} = C_a * \pi * d * L$$

حيث أن:

$Q_{ult} \rightarrow$

قدرة تحمل الخازوق.

$Q_{all} \rightarrow$

حمل الأمان للخازوق.

$C \rightarrow$ Cohesion of soil at pile tip.

متوسط تماسك التربة حول الطرف السفلي للخازوق.

$d \rightarrow$ pile diameter.

قطر الخازوق.

$L \rightarrow$ pile length.

طول الخازوق.

F.O.S \rightarrow Factor of Safety.

معامل الأمان.

F.O.S = 3 if (D.L+L.L)

F.O.S = 2.5 if (D.L+L.L+WIND+EAETHQUAKE)

$N_c \rightarrow$ Bearing capacity factor (6 \rightarrow 9)

معامل قدرة التحميل.

$$N_c = 6 \text{ if } d > 100 \text{ cm}$$

$$N_c = 7 \text{ if } 50 < d < 100 \text{ cm}$$

$$N_c = 9 \text{ if } d < 50 \text{ cm}$$

$C_a \rightarrow$ adhesion

متوسط إلتصاق التربة علي سطح الخازوق.

$$C_a = \frac{2}{3} * C$$

OR

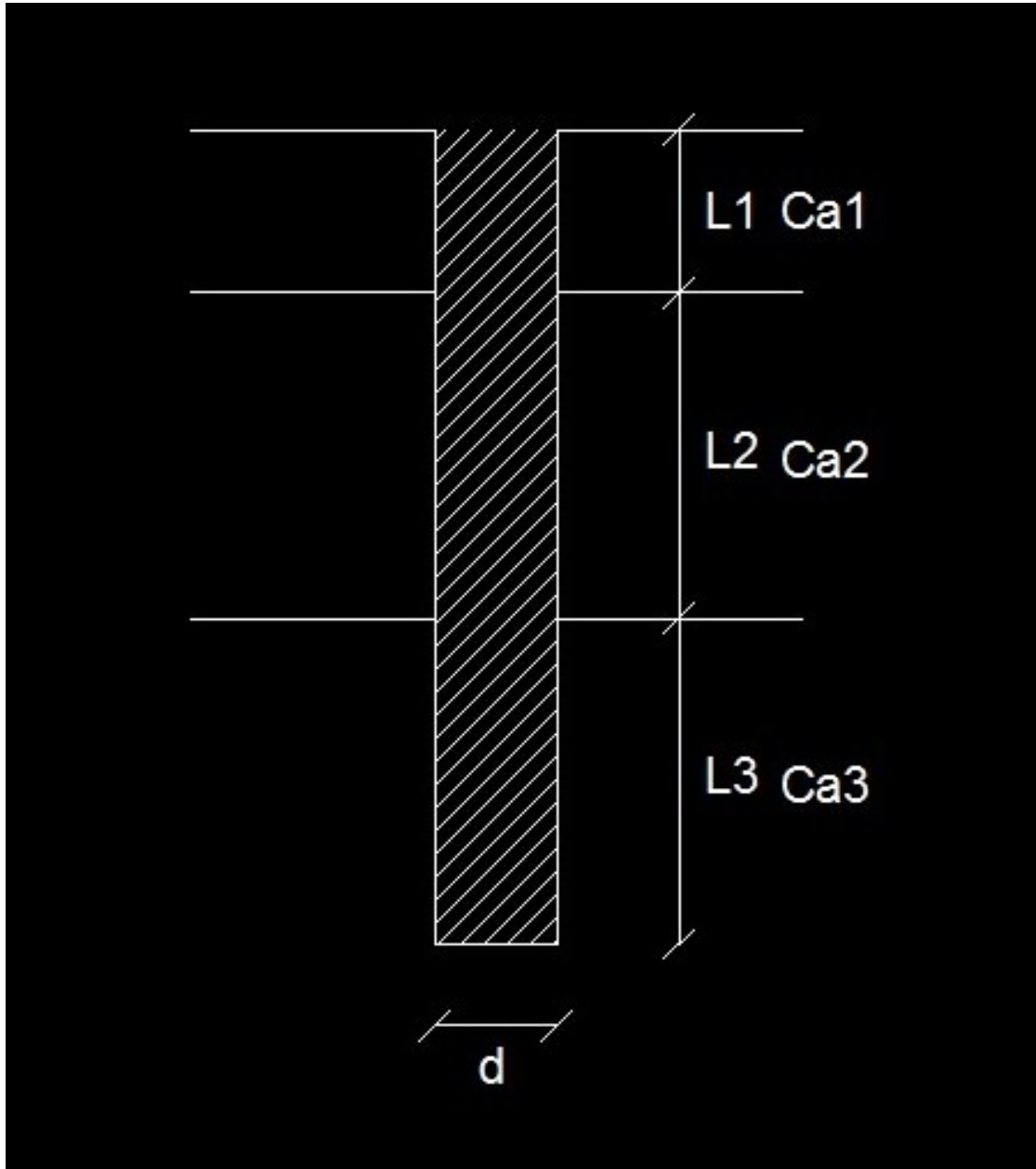
$C_a = 0.3 - 0.4 (C_u)$ $C_u \leq 100 \text{ kPa}$ For bored piles.

$C_a = 0.6 - 0.8 (C_u)$ For driven piles.

OR

For driven Piles C_a could be directly taken as mentioned in the following table:

Pile Type	Cohesion C_u (kN/m²)	Adhesion C_a (kN/m²)
Timber or concrete	0-12.5	0-12.5
	12.5-25	12.5-24
	25-50	24-37.5
	50-100	37.5-47.5
	100-200	47.5-65
Steel	0-12.5	0-12.5
	12.5-25	12.5-23
	25-50	23-35
	50-100	35-36



في حالة وجود عدد من الطبقات نضرب C_a لكل طبقة *
 طول الخازوق في هذه الطبقة:

$$C_{a1} * L_1 + C_{a2} * L_2 + C_{a3} * L_3$$

2) Tension:

الخوازيق المعرضة لأحمال الشد:

$$T_{ult} = C_a * \pi * d * L + W_p$$

$$T_{all} = \frac{t_{ult}}{F.O.S}$$

حيث أن:

$$T_{ult} \rightarrow$$

أقصى حمل شد يتحمله الخازوق.

$$T_{all} \rightarrow$$

حمل الشد الآمان الذي يتحمله للخازوق.

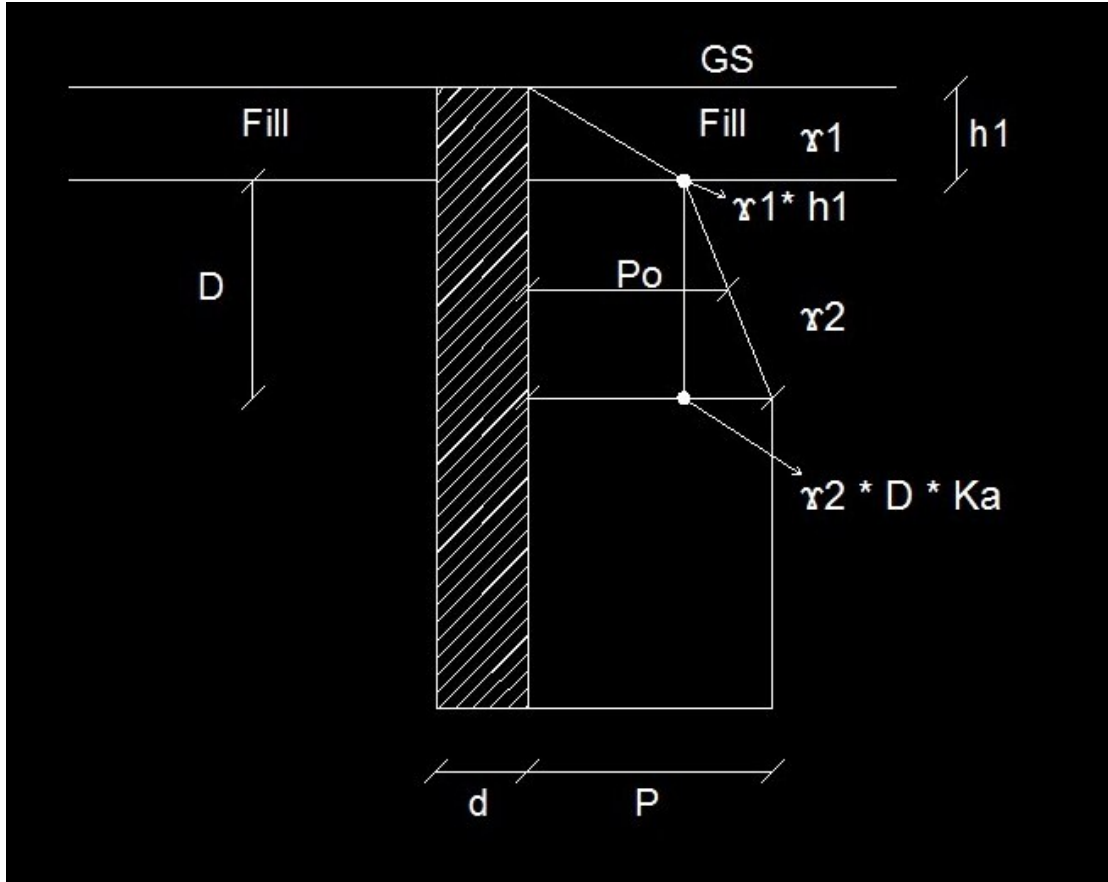
$$W_p \rightarrow \text{Weight of pile.}$$

وزن الخازوق.

$$W_p = \frac{\pi * (d^2)}{4} * L * \gamma_c$$

$$\gamma_c = 2.5$$

For Cohesion Less Soil (Sand):



1) Compression:

الخوازيق المعرضة لأحمال ضغط:

$$Q_{ult} = P * N_q * \frac{\pi * (d^2)}{4} + K_{HC} * P_o * \tan \delta * \pi * d * L$$

$$Q_{all} = \frac{Q_{ult}}{F.O.S}$$

$$\text{End Bearing} = P * N_q * \frac{\pi * (d^2)}{4}$$

$$\text{Friction} = K_{HC} * P_o * \tan \delta * \pi * d * L$$

حيث أن:

$$D = 20*d$$

العمق الذي يظل بعده الضغط الجانبي ثابت ولا يزيد.

$$P = \gamma_1 * h_1 + \gamma_2 * h_2$$

P →

الضغط الجانبي علي عمق D من سطح طبقة الرمل.

$$K_a = \frac{1 - \sin \phi}{1 + \sin \phi}$$

N_q → Bearing capacity factor function of ν

معامل قدرة التحميل.

To get N_q from table:

ν	25	30	35	40	
Displacement pile	15	30	75	150	Nq
Bored pile	7	15	37	75	

If $\nu = 0$, $N_q = 0$

$$\nu^* = \nu - 3^{\circ} \text{ (For bored piles)}$$

$$\nu^* = \frac{\nu + 40^{\circ}}{2} \text{ (For driven piles)}$$

K_{HC} → Coefficient of lateral pressure.

$K_{HC} = 0.7 \rightarrow 1.5$ (For bored piles) Take = 1

$K_{HC} = 1 \rightarrow 1.5$ (For driven piles) Take = 1.5

قيم المعاملات (K_{HC}) & (K_{Ht}) طبقا للكود المصرى :

K_{Ht}	K_{HC}	نوع الخازوق
0.50 – 0.30	1.0 - 0.50	خازوق ذو قطاع H
1.0 – 0.6	1.5 - 1.0	خازوق إزاحة
1.3 – 1.0	2.0 – 1.5	خازوق إزاحة متغير القطاع
0.6 – 0.3	0.9 – 0.4	خازوق إزاحة باستخدام النفثات
1.0 – 0.4	1.5 – 0.7	خازوق تنقيب اعتيادي (قطر أقل من 0.60 متر)

$P_o \rightarrow$

متوسط قيمة الضغط الجانبي خلال الطول.

$\delta \rightarrow$ Pile-Soil friction angle

زاوية الاحتكاك بين الخازوق و التربة.

$\delta = \frac{3}{4} * \nu$ (for concrete and timber pile).

$\delta = 20^\circ$ (for steel pile).

2) Tension:

الخوازيق المعرضة لأحمال الشد:

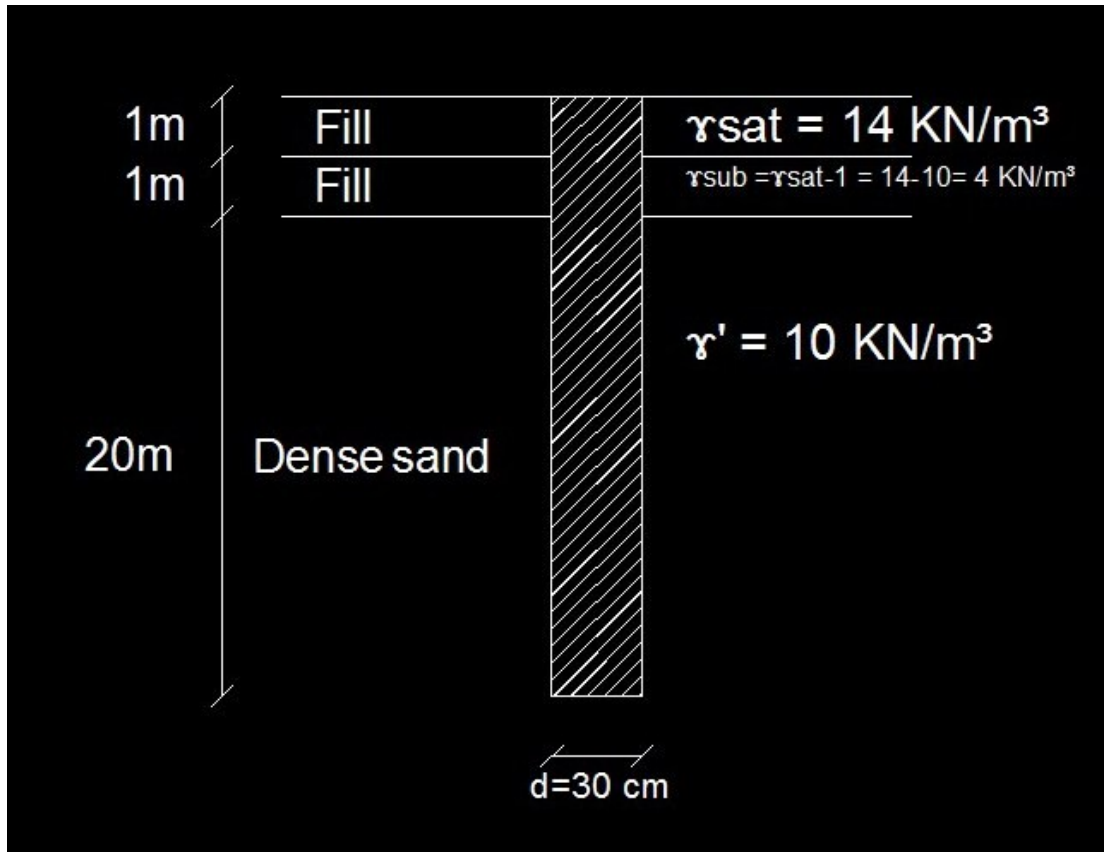
$$T_{ult} = K_{Ht} * P_o * \tan \delta * \pi * d + W_p$$

$$T_{all} = \frac{t_{ult}}{F.O.S}$$

Example: 2

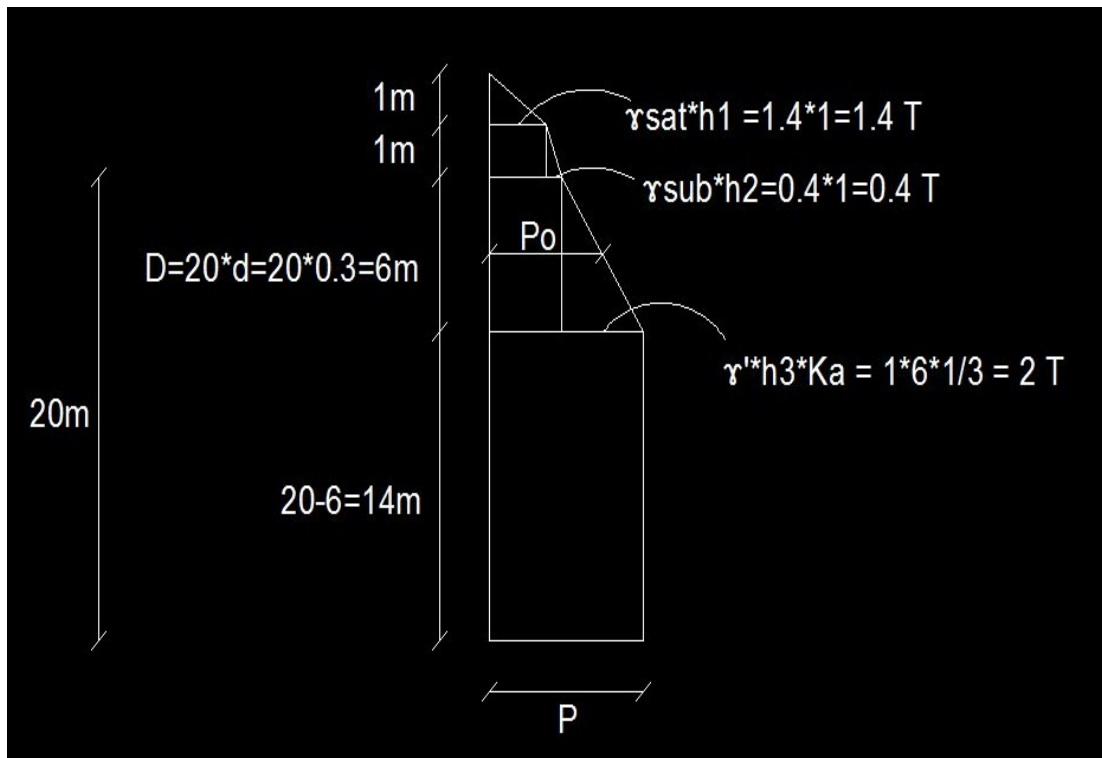
Given : $\nu = 30^\circ$, $d = 30 \text{ cm}$, $K_{Ht} = 1$, $K_{Hc} = 1.5$, F.O.S = 3

Req : Determine the allowable Max Load for Driven pile shown in case of Compression & Tension .



Solution

$$100 \text{ kN} / \text{m}^2 = 10 \text{ t} / \text{m}^2 = 1 \text{ kg} / \text{cm}^2$$



For Cohesion Less Soil (Sand):

$$D = L \cdot d = 20 \cdot 0.3 = 6 \text{ m}$$

1) Compression:

$$Q_{\text{ult}} = P \cdot N_q \cdot \frac{\pi \cdot (d^2)}{4} + K_{\text{HC}} \cdot P_o \cdot \tan \delta \cdot \pi \cdot d \cdot L$$

$$K_a = \frac{1 - \sin \phi}{1 + \sin \phi} = \frac{1 - \sin 30}{1 + \sin 30} = 0.33$$

$$\delta = \frac{3}{4} \cdot \nu = \frac{3}{4} \cdot 30 = 22.5$$

$$\nu = 30^\circ \rightarrow N_q = 30 \text{ from table}$$

$$P = 1.4 + 0.4 + 2 = 3.8 \text{ T}$$

$$P_{o1} = \left(\frac{1.4 + 0.4 + 3.8}{2} \right) * 6 = 16.8 \text{ T}$$

$$P_{o2} = 3.8 * 14 = 47.6 \text{ T}$$

$$P_{T0} = 47.6 + 16.8 = 64.4 \text{ T}$$

تم ضرب قيمة ال P_o في الطول L لكل جزء فلا يتم وضع قيمة الطول L في المعادلة.

$$Q_{ult} = 3.8 * 30 * \frac{\pi * (0.3)^2}{4} + 1.5 * 64.4 * \tan 22.5 * \pi * 0.3$$

$$= 45.77 \text{ Ton}$$

$$Q_{all} = \frac{Q_{ult}}{F.O.S} = \frac{45.77}{3} = 15.26 \text{ Ton}$$

2) Tension:

$$T_{ult} = K_{Ht} * P_o * \tan \delta * \pi * d + W_p$$

$$= 1 * 64.4 * \tan 22.5 * \pi * 0.3 + 3.89 = 29 \text{ Ton}$$

$$K_{Ht} = 1, L = 22$$

$$W_p = \frac{\pi * (d^2)}{4} * L * \gamma_c$$

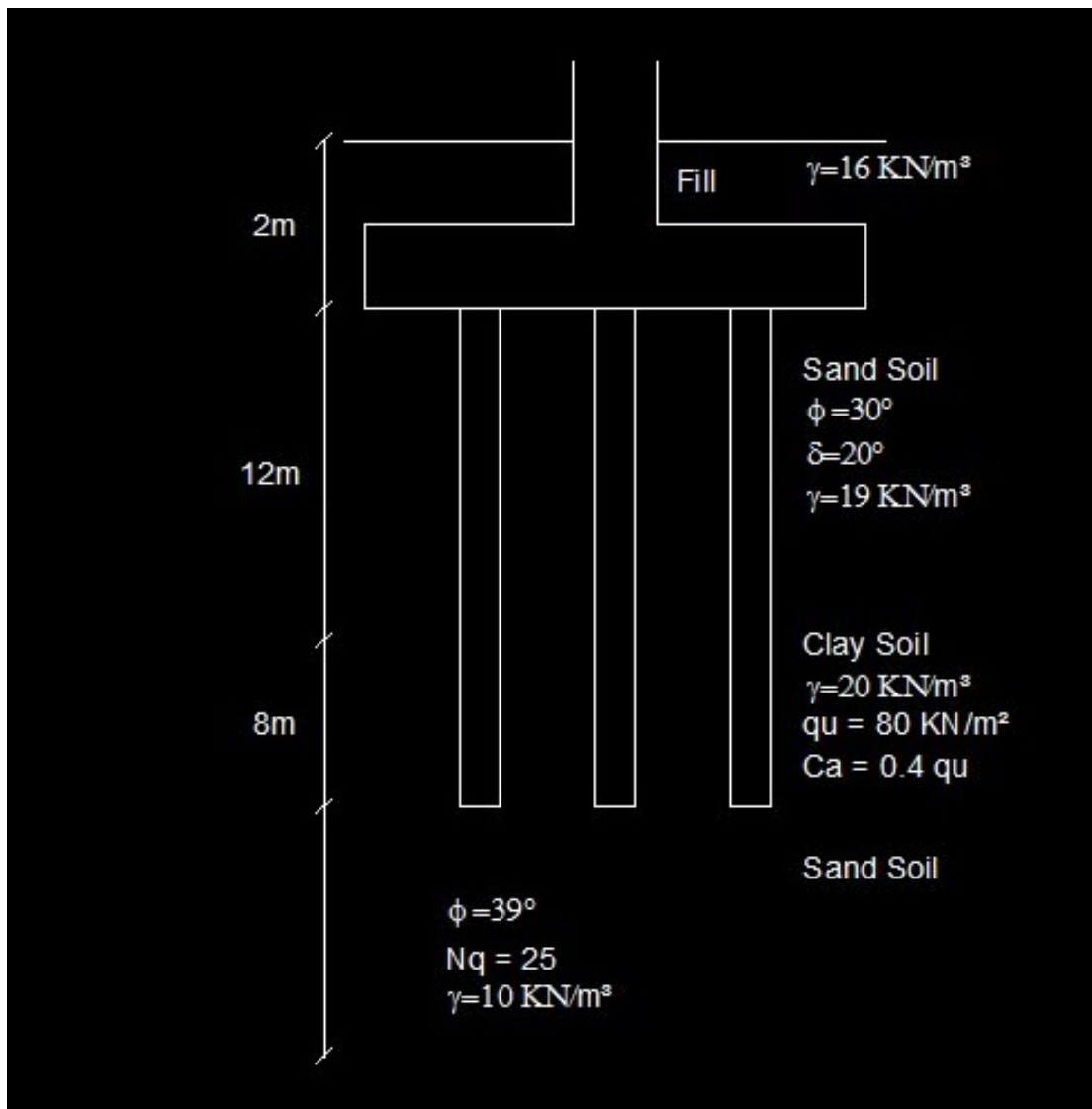
$$W_p = \frac{\pi * (0.3)^2}{4} * 22 * 2.5 = 3.89$$

$$T_{all} = \frac{t_{ult}}{F.O.S} = \frac{29}{3} = 9.67 \text{ Ton}$$

Example: 3

Given : $d = 40 \text{ cm}$, $K_{Ht} = 1$, $K_{Hc} = 1$, F.O.S = 3 , No. of piles = 12

Req : Determine the safe Load capacity of the pile group.



Solution

For Clay Soil:

∴ Pile Rested on Sand Soil:

∴ end Bearing = 0

$$Q_{ult(1)} = C_a * \pi * d * L$$

$$C_a = 0.4 * q_u = 0.4 * 80 = 32 \text{ KN/m}^2$$

$$Q_{ult(1)} = 32 * \pi * 0.4 * 8 = 321.7 \text{ KN}$$

For Sand Soil:

Sand (1):

طبقة الرمل العلوية:

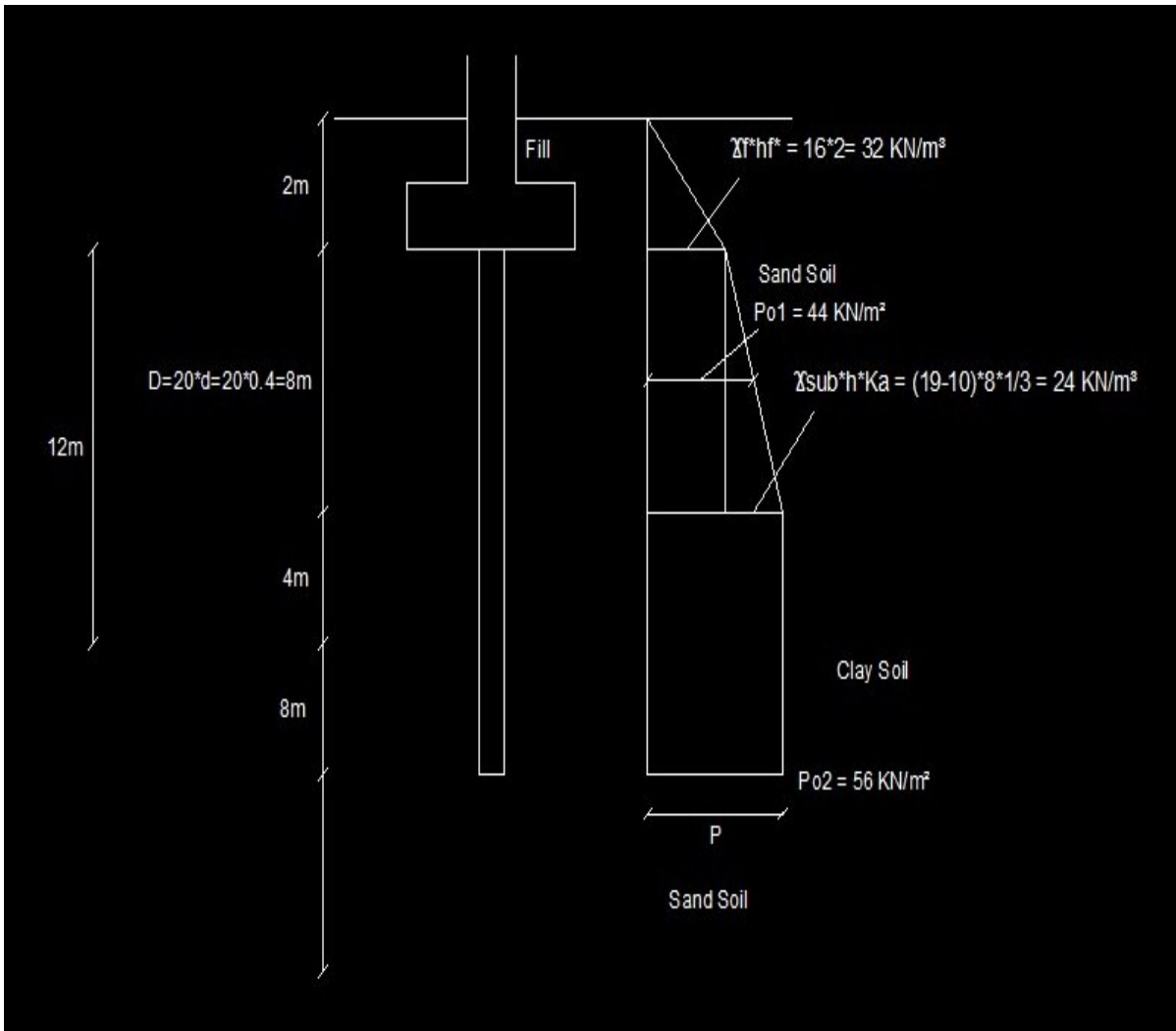
Friction only:

$$D = L * d = 20 * 0.4 = 8 \text{ m}$$

$$Q_{ult} = K_{HC} * P_o * \tan \delta * \pi * d * L$$

$$K_a = \frac{1 - \sin \phi}{1 + \sin \phi} = \frac{1 - \sin 30}{1 + \sin 30} = 0.33 = 1/3$$

$$\gamma_{sub} = \gamma - \gamma_w = 19 - 10 = 9 \text{ KN/m}^3$$



$$P_{o1} = \frac{32 + 56}{2} = 44\text{ KN/m}^2$$

$$P_{o2} = 56\text{ KN/m}^2$$

$$Q_{ult(2)} = 1 \times \{(8 \times 44) + (4 \times 56)\} \times \tan 20^\circ \times \pi \times 0.4$$

$$= 263.45\text{ KN}$$

Sand (2):

طبقة الرمل السفلية:

End Bearing only:

$$Q_{ult(3)} = P * N_q * \frac{\pi * (d^2)}{4}$$

$$Q_{ult(3)} = 56 * 25 * \frac{\pi * (0.4)^2}{4} = 176 \text{ KN}$$

$$Q_{ult(TOTAL)} = Q_{ult(1)} + Q_{ult(2)} + Q_{ult(3)}$$

$$= 321.7 + 263.45 + 176 = 761.15 \text{ KN}$$

$$Q_{all} = \frac{Q_{ult}}{F.O.S} = \frac{761.15}{3} = 253.72 \text{ KN}$$

$$Q_{all(group)} = \text{No. of piles} * Q_{all} = 12 * 253.72$$

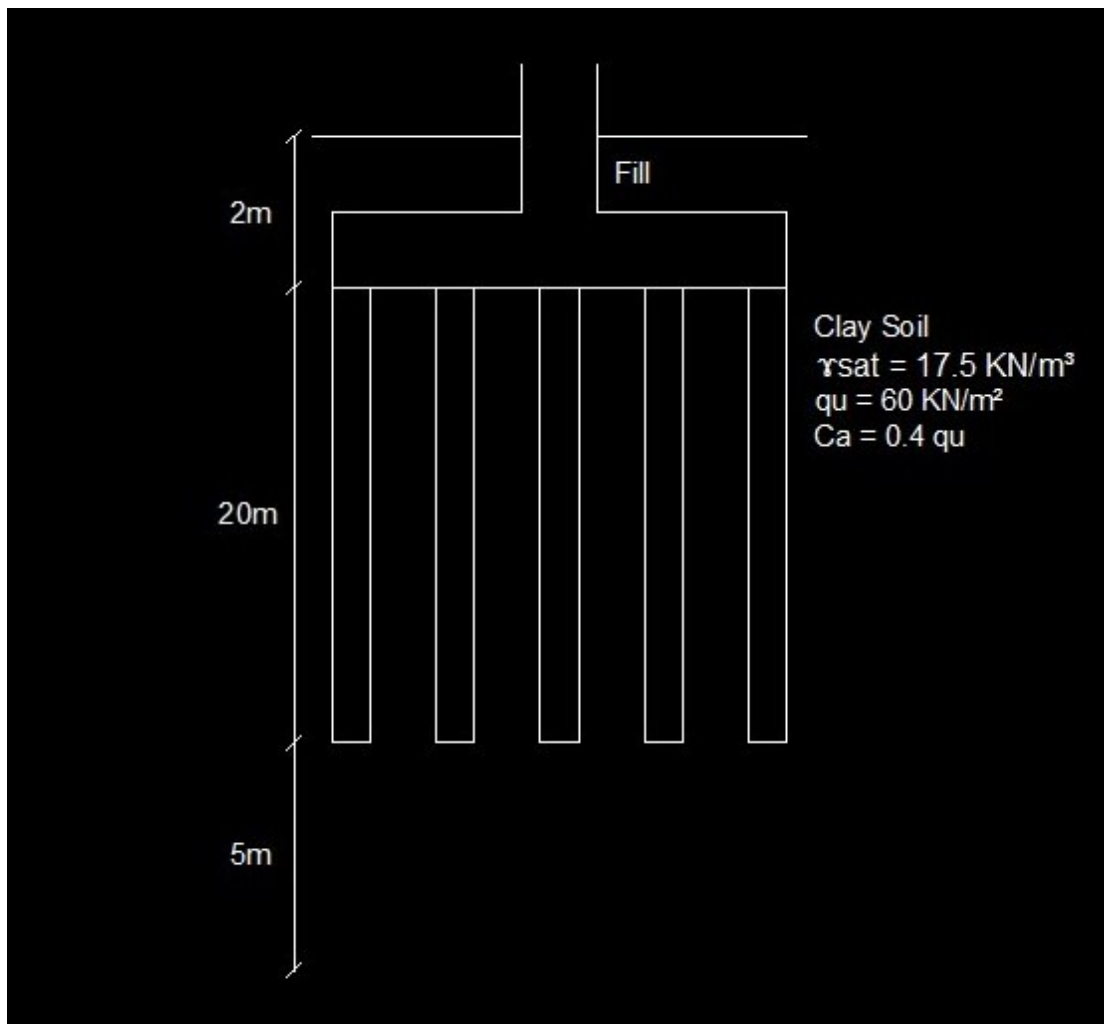
$$= 3044.64 \text{ KN} = 304.46 \text{ Ton}$$

Example: 4

Given : $d = 40 \text{ cm}$, F.O.S = 3 , No. of piles = 16 ,

Friction pile.

Req : Determine the safe Load capacity of the pile group.



Solution

For Clay Soil:

∴ Pile Friction:

∴ end Bearing = 0

$$Q_{ult(F)} = C_a * \pi * d * L$$

$$C_a = 0.4 * q_u = 0.4 * 60 = 24 \text{ KN/m}^2$$

$$Q_{ult(F)} = 24 * \pi * 0.4 * 20 = 603.2 \text{ KN} = 60.3 \text{ Ton}$$

$$Q_{all} = \frac{Q_{ult}}{F.O.S} = \frac{603.2}{3} = 201.1 \text{ KN}$$

$$Q_{all(\text{group})} = \text{No. of piles} * Q_{all} = 16 * 201.1 \\ = 3217.1 \text{ KN} = 321.7 \text{ Ton}$$

3) Determination piles settlement:

For settlement of a single pile is considered to be the sum of three components:

هبوط الخازوق المفرد: يتم حسابه باعتبار هبوط الخازوق عند طرفة العلوي هو حاصل جمع ثلاثة مقادير هي:

1.The elastic compression of pile shaft (S_s):

الهبوط نتيجة لانفعال جذع الخازوق تحت إجهادات التحميل:

2.The settlement caused by load transferred at the pile tip (S_{pp}):

الهبوط نتيجة لإنتقال حمل الارتكاز Q_b إلي التربة S_{pp} .

3.The settlement caused by load transferred along the pile shaft (S_{ps}):

هبوط الخازوق نتيجة لإنتقال حمل الاحتكاك Q_f من جذع الخازوق إلي التربة S_{ps} .

The total settlement is then equal to:

$$S_o = S_s + S_{pp} + S_{ps}$$

1.The elastic compression of pile shaft (S_s) :

$$S_s = (Q_b + \alpha_f * Q_f) * \frac{L}{A * E_p}$$

In which:

حيث أن:

Q_b → Bearing load at pile tip.

حمل الإرتكاز المنقول للتربة عند طرف الخازوق السفلي.

Q_f → Friction load transmitted by pile shaft.

حمل الإحتكاك المنقول للتربة عن طريقة جهود الإحتكاك
علي سطح جذع الخازوق.

L → Pile length.

طول الخازوق.

A → Pile cross-sectional area.

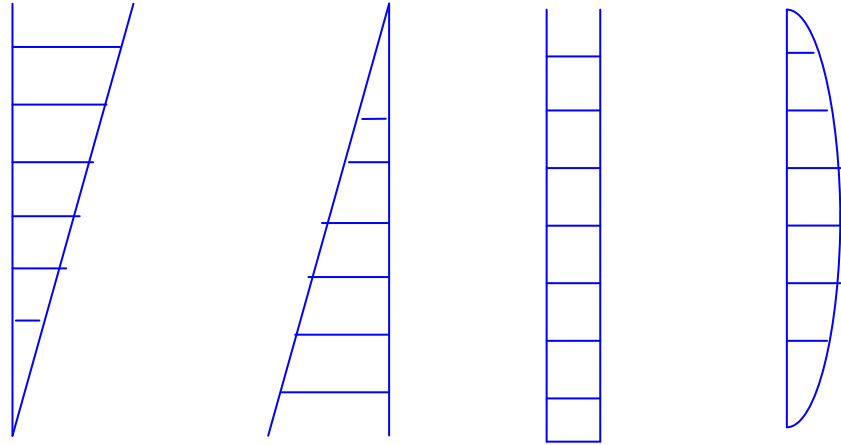
مساحة مقطع الخازوق.

E_p → Elastic modulus for pile material.

معامل المرونة لمادة الخازوق.

α_f → Skin friction distribution coefficient.

معامل يتوقف علي منحنى توزيع جهود الإحتكاك علي إمتداد
طول الخازوق.



$$\alpha_f = 0.33$$

$$\alpha_f = 0.67$$

$$\alpha_f = 0.5$$

$$\alpha_f = 0.5$$

Skin friction distribution Coefficient (α_f)

2- Settlement caused by load transferred at the pile tip (S_{pp}):

$$S_{pp} = \frac{C_b Q_b}{d \cdot q}$$

In which:

C_b → Factor according to table 9.1.

معامل يعتمد علي نوعية التربة وعلي أسلوب تنفيذ الخازوق.

Q_b → Bearing load at pile tip.

حمل الإرتكاز المنقول للتربة عند طرف الخازوق السفلي.

$d \rightarrow$ pile diameter.

قطر الخازوق.

$q \rightarrow$ Ultimate end bearing capacity.

الجهد الأقصى لسعة التحميل عند نهاية الخازوق.

Bearing stratum under pile tip assumed to extend at least 10 pile diameters below tip and soil below tip is of comparable or higher stiffness.

ويشترط أن تكون طبقة ارتكاز الخازوق ممتدة تحت طرف الخازوق لمسافة تساوي عشرة أمثال قطره على الأقل وأن تكون الطبقات التي تليها ذات مقاومة تتساوى مع أو تزيد عن مقاومة الطبقات المنشأة بها الخوازيق.

Table 9.1 Values of C_b :

Soil Type	Driven piles	Bored Piles
Loose to dense sand	0.02-0.04	0.09-0.18
Soft to stiff clay	0.02-0.03	0.03-0.06
Loose to dense silt	0.03-0.05	0.09-0.12

3- Settlement caused by load transferred along the pile shaft (S_{ps}):

$$S_{ps} = \frac{C_s Q_f}{L_o \cdot q}$$

In which:

حيث أن:

C_s → Factor from the following relation:

معامل.

$$C_s = (0.93 + 0.16 \sqrt{\frac{L_o}{d}}) \cdot C_b$$

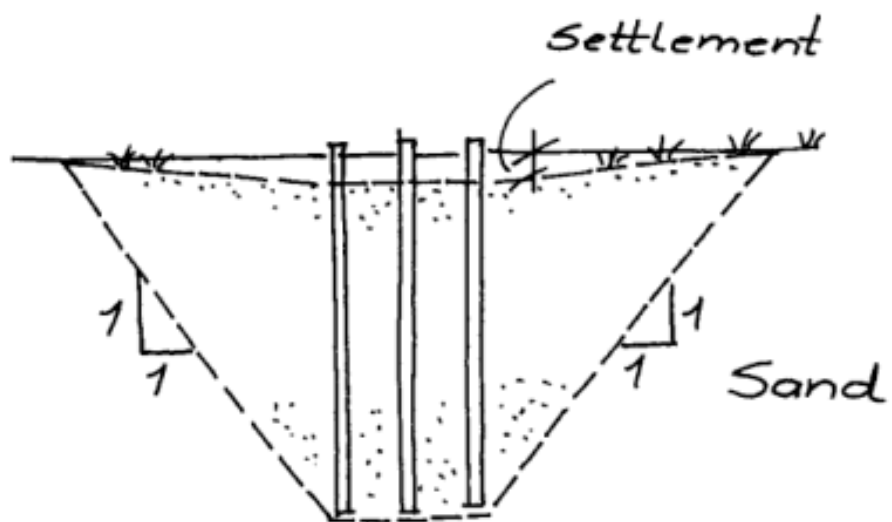
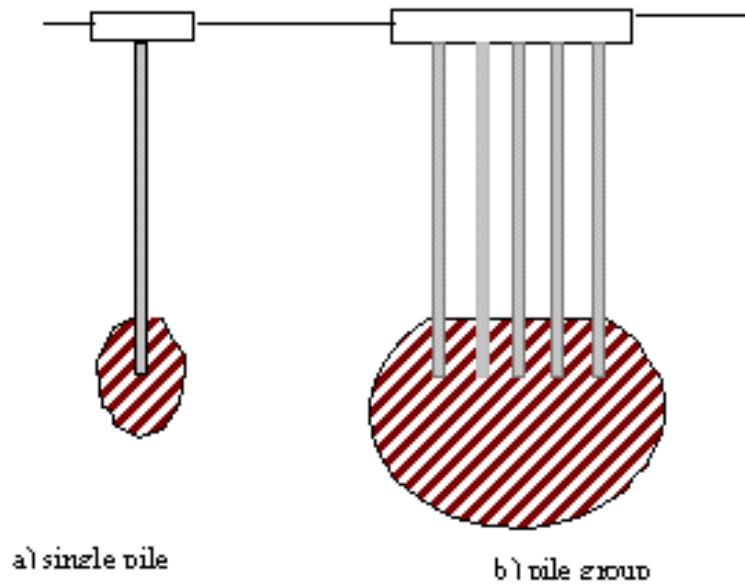
L_o → Embedded pile length.

طول جذع الخازوق المدفون بالتربة.

q → Ultimate end bearing capacity.

الجهد الأقصى لسعة التحميل عند نهاية الخازوق.

Settlement of pile groups:



Settlement of pile groups according to Egyptian code:

$$S_g = S_o * \sqrt{\frac{b}{d}}$$

In which:

حيث أن:

b → pile group width.

المقياس الأدنى (الطول الأصغر) لمجموعة الخوازيق
بالمسقط الأفقي.

d → pile diameter.

قطر الخازوق.

So → Single pile settlement estimated or determined from load tests.

مقدار هبوط الخازوق المفرد مقدر من الصيغة السابق ذكرها
أو المحددة من تجارب التحميل.

Example: 5

Given : $d = 80 \text{ cm}$, $L = 25 \text{ m}$, $Q_{all} = 200 \text{ Ton}$,

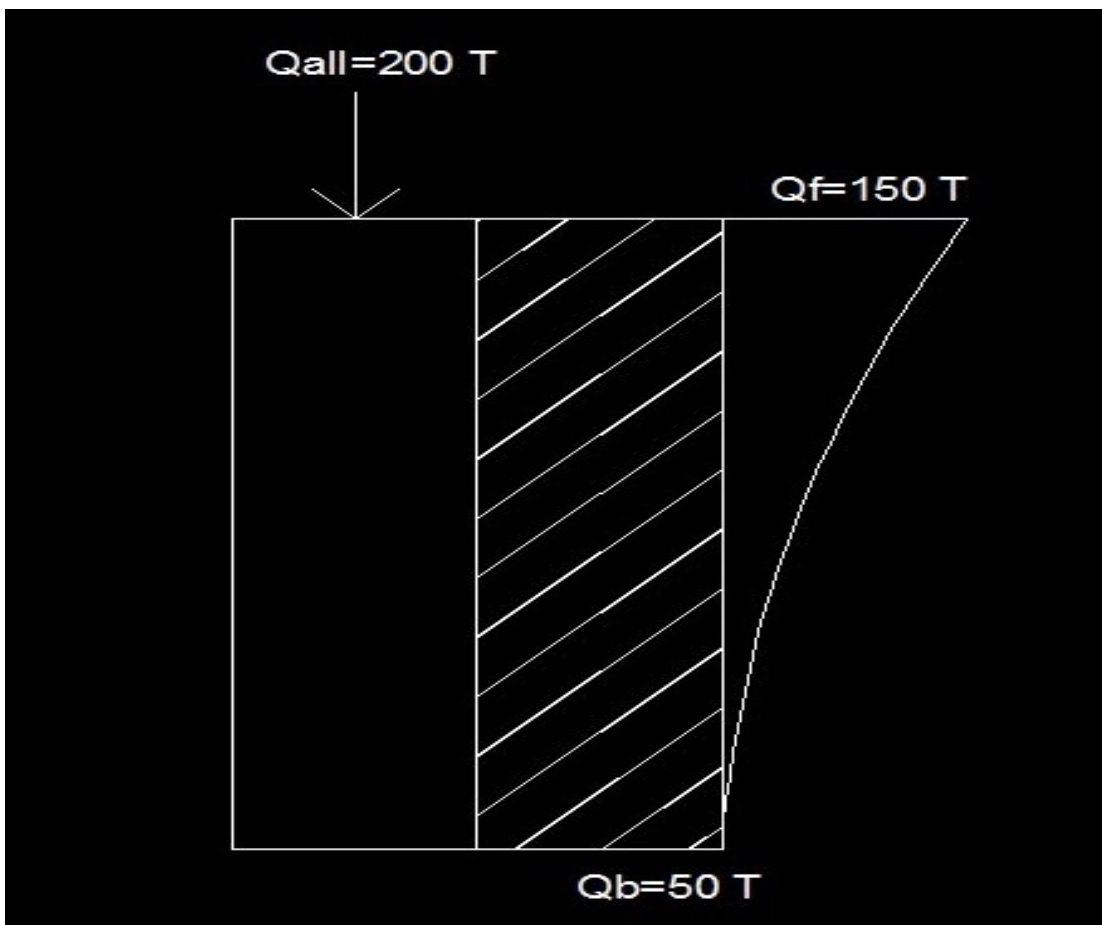
$E_p = 2000000 \text{ t/m}^2$, $b = 5.6 \text{ m}$, Soil Type is Loose to dense sand , Bored Piles

Req : Determine the settlement of a single pile & the Settlement of pile groups.

Solution

For settlement of a single pile:

$$S_o = S_s + S_{pp} + S_{ps}$$



$$S_s = (Q_b + \alpha_f * Q_f) * \frac{L}{A * E_p}$$

$$A = \frac{\pi * (d)^2}{4} = \frac{\pi * (0.8)^2}{4} = 0.5 \text{ m}$$

$\alpha_f = 0.5$ from chart

$$S_s = (50 + 0.5 * 150) * \frac{25}{0.5 * 2000000} = 0.00313 \text{ m}$$

$$S_{pp} = \frac{C_b * Q_b}{d * q}$$

$d = 0.8 \text{ m}$, $Q_b = 0 \text{ T}$

$C_b = 0.09$ From table

$$q = \frac{Q_b}{A} = \frac{0}{0.5} = 0$$

$$S_{pp} = \frac{0.09 * 0}{0.8 * 0} = 0$$

$$S_{ps} = \frac{C_s * Q_f}{L_o * q}$$

$$C_s = (0.93 + 0.16 \sqrt{\frac{L_o}{d}}) * C_b$$

$L_o = 18 \text{ m}$, $d = 0.8$, $C_b = 0.09$, $q = 300$

$$C_s = (0.93 + 0.16 * \sqrt{\frac{18}{0.8}}) * 0.09 = 0.15$$

$$S_{ps} = \frac{0.15 * 150}{18 * 300} = 0.0042 \text{ m}$$

$$S_o = S_s + S_{pp} + S_{ps}$$

$$= 0.00313 + 0 + 0.0042 = 0.0073 \text{ m}$$

For Settlement of pile groups:

$$S_G = S_o \sqrt{\frac{b}{d}} = 0.0073 * \sqrt{\frac{5.6}{0.8}} = 0.02 \text{ m}$$

4) Short and Long pile:

Elastic versus rigid behavior:

$$T = \sqrt[5]{\frac{E \cdot I}{\eta}}$$

حيث أن:

T → relative stiffness factor

E → modulus of elasticity of pile

I → pile inertia

$$I = \frac{\pi \cdot (D)^4}{64}$$

η for clayey or silty soil:

$q_{un} \text{ (KN/m}^2\text{)}$	25	50	100
$\eta \text{ (KN/m}^3\text{)}$	600	1600	3700

η for sand soil:

Relative Density (Dr)	35	65	85	100
$\eta \text{ (KN/m}^3\text{)}$	4300	12300	18000	22200

For submerged soil " η " is reduced to half the above values. Besides, " η " must be reduced to 0.25 the above values if pile spacing in the direction of loading is three times the pile diameter (3D), no reduced if spacing = 8D, values for another spacing values shall be calculated by interpolation.

If $\frac{L}{T} < 2 \rightarrow$ the pile is considered short rigid pile

If $\frac{L}{T} > 4 \rightarrow$ the pile is considered long flexible pile

حيث أن:

L \rightarrow pile length (embedded length)

For Short Rigid Piles:

1) Fixed headed piles:

1.1.) Piles in sandy soil:

$$P_u = 1.5 * \gamma * L^2 * D * K_p$$

حيث أن:

γ → effective unit weight

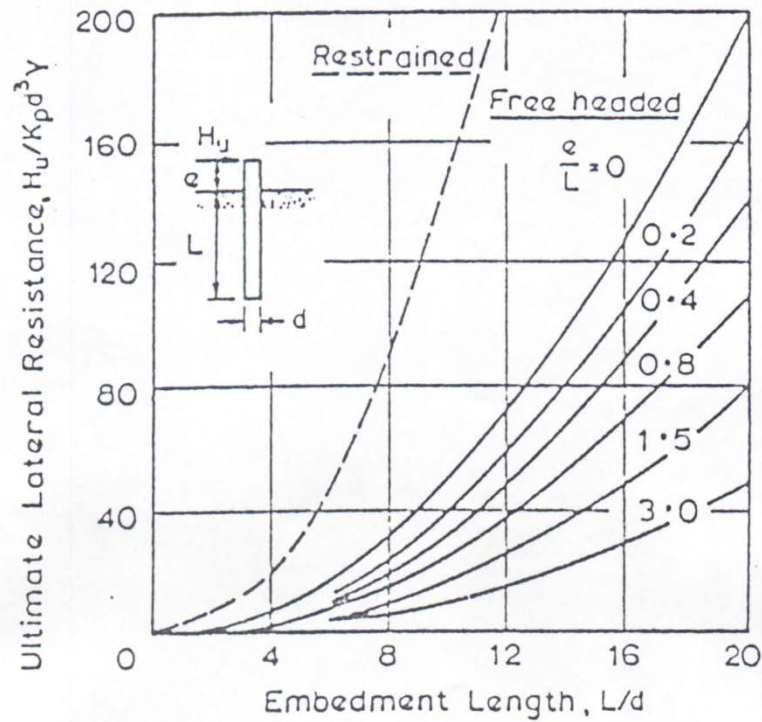
$\gamma = \gamma_{sub}$ under water

L → pile length

D → pile diameter

K_p → passive coefficient

To get K_p from chart



(a)

Fig. (2-a) Ultimate lateral resistance of short piles in cohesionless soils (after Broms, 1964)

1.2.) piles in clay soil:

$$P_u = 9 * c_u * D * (L - 1.5 * D)$$

حيث أن:

$c_u \rightarrow$ undrained shear strength of soil

2) Free headed piles:

2.1.) Piles in sandy soil:

$$P_u = \frac{0.5 * D * (L)^3 * K_p * \alpha}{H + L}$$

حيث أن:

L → is the embedded length of pile

H →

سمك الردم

Take H=2m

2.2.) piles in clay soil:

$$P_u = \frac{(L_o)^2 - 2 * L' * L_o + (0.5 * (L')^2)}{L + H + (1.5 * D)} * 9 * C_u * D$$

حيث أن:

$$L' = L - 1.5 * D$$

$$L_o = \frac{(H + \frac{2}{3} * L)}{2 * H + L} * L$$

For Long Flexible Pile

1) Fixed headed piles:

1.1.) Piles in sandy soil:

$$P_u = \frac{2 * \text{Mult resisting}}{H + \left\{ 0.54 * \left(\frac{P_u}{(\alpha' * D * K_p)} \right) \right\}}$$

حيث أن:

$M_{ult} \rightarrow$ is the moment of resisting of the pile section including its reinforcement.

1.2.) piles in cohesive soil:

$$P_u = \frac{2 * \text{Mult resisting}}{H + \left\{ 1.5 * \left(\frac{P_u}{(9 * C_u * D)} \right) \right\}}$$

The maximum induced ultimate moment in pile = $0.85 * P_u * \eta$

The maximum deflection at pile top

$$= 0.88 * P_{\text{service}} * \frac{(T)^3}{E * I}$$

2) Free headed piles:

2.1.) Piles in sandy soil:

$$P_u = \frac{\text{Mult resisting}}{H + \left\{ 0.54 * \left(\frac{P_u}{(\lambda' * D * K_p)} \right) \right\}}$$

حيث أن:

M_{ult} → is the moment of resisting of the pile section including its reinforcement.

2.2.) piles in cohesive soil:

$$P_u = \frac{\text{Mult resisting}}{H + \left\{ 1.5 * \left(\frac{P_u}{(9 * C_u * D)} \right) \right\}}$$

The maximum induced ultimate moment in pile = $0.77 * (P_u * \eta + M_{OU})$

The maximum deflection at pile top

$$= 2.4 * \frac{P_{\text{service}} * (\eta)^3}{E * I} + \frac{1.55 * M_o * (\eta)^2}{E * I}$$

حيث أن:

M_o → is any induced acting moment on the free pile head

$$P_u = \frac{\text{Rection}}{\text{no.of pile}}$$

$$\text{Reaction} = \sqrt{(F_x)^2 + (F_y)^2}$$

From INTERACTION Diagrams:

$$K = \frac{M_u}{F_{cu} * (R)^3}$$

Get ρ

$$A_s = \rho * (f_{cu} * 10^{-4}) * \pi * (R)^2$$

حيث أن:

R →

نصف قطر الخازوق

Example: 5

Given : $D = 80 \text{ cm}$, $L = 25 \text{ m}$, $E_p = 2000000 \text{ t/m}^2$, piles in clay soil , $q_{un} = 50 \text{ KN/m}^2$, $C_u = 5 \text{ t/m}^2$, $F_x = 327.7$,

$F_y = 73.34$, No. of piles = 11 ,

$F_{cu} = 30 \text{ N/mm}^2$, Pile Rested in cohesive soil

Req : Determine the pile is Short or Long pile.

Solution

$$T = \frac{5 \sqrt{E \cdot I}}{\eta}$$

$$I = \frac{\pi \cdot (D)^4}{64} = \frac{\pi \cdot (0.8)^4}{64} = 0.02 \text{ m}^4$$

for clayey soil:

$$\eta = 1600 = 1600 / 2 = 800 \text{ KN/m}^3 = 80 \text{ t/m}^3$$

$$T = \frac{5 \sqrt{2000000 \cdot 0.02}}{80} = 3.47 \text{ m}$$

$$L = 25 - 2 = 23 \text{ m}$$

$$\frac{L}{T} = \frac{23}{3.47} = 6.63 > 4$$

∴ the pile is considered long flexible pile

For long flexible pile (Fixed headed)

$$P_u = \frac{2 * \text{Mult resisting}}{H + \left\{ 1.5 * \left(\frac{P_u}{(9 * C_u * D)} \right) \right\}}$$

Take $H = 3$

$$C_u = 5 \text{ t/m}^2$$

$$P_u = \frac{\text{Rection}}{\text{no.of pile}}$$

$$\begin{aligned} \text{Reaction} &= \sqrt{(Fx)^2 + (Fy)^2} \\ &= \sqrt{(327.7)^2 + (73.34)^2} = 336 \text{ T} \end{aligned}$$

$$P_u = \frac{336}{11} = 30.55 \text{ T}$$

$$30.55 = \frac{2 * \text{Mult}}{3 + \left\{ 1.5 * \left(\frac{30.55}{(9 * 5 * 0.8)} \right) \right\}}$$

$$2M_{\text{ult}} = 130.54$$

$$M_{\text{ult}} = 65.27 \text{ m.t}$$

From INTERACTION Diagrams:

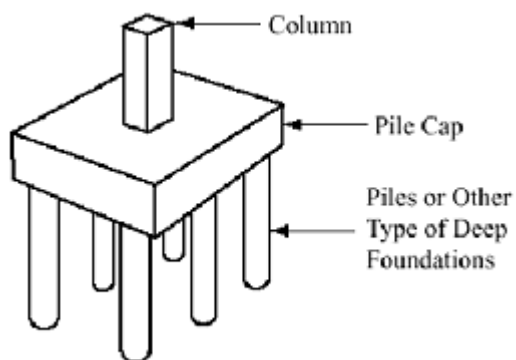
$$K = \frac{M_u}{F_{cu} * (R)^3} = \frac{65.27 * 10^7}{30 * (400)^3} = 0.34$$

$$\rho = 4$$

$$\begin{aligned} A_s &= \rho * (f_{cu} * 10^{-4}) * \pi * (R)^2 \\ &= 4 * (30 * 10^{-4}) * \pi * (40)^2 \\ &= 60.32 \text{ cm} \end{aligned}$$

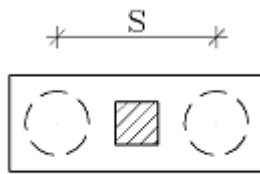
Use 20 y 25

5) Design of piles cap:

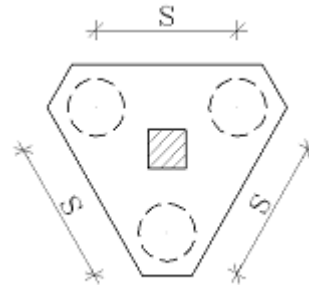


Pile caps are thick slabs used to tie a group of piles together to support and transmit column loads to the piles.

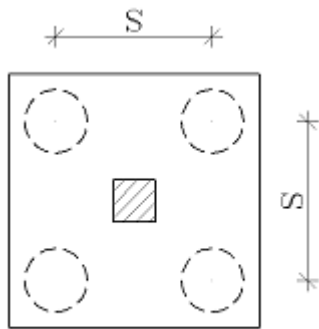
Typical Arrangement of Piles:



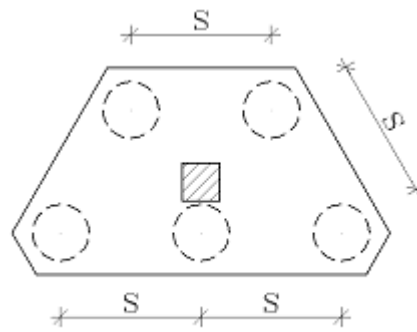
2 Piles



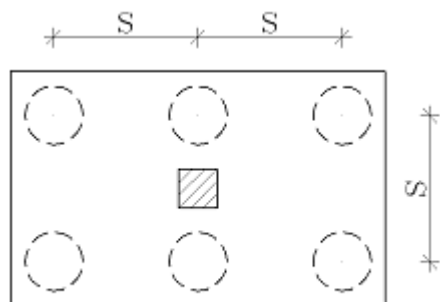
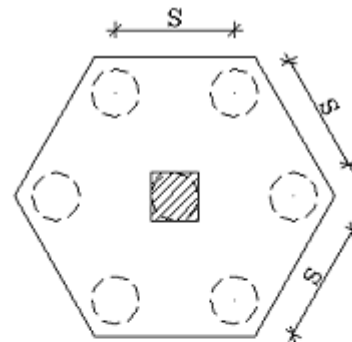
3 Piles



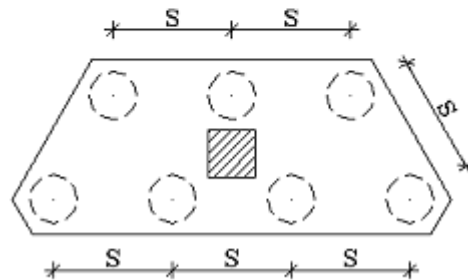
4 Piles



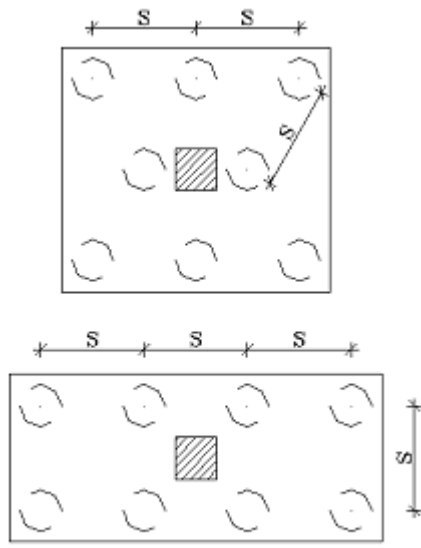
5 Piles



6 Piles

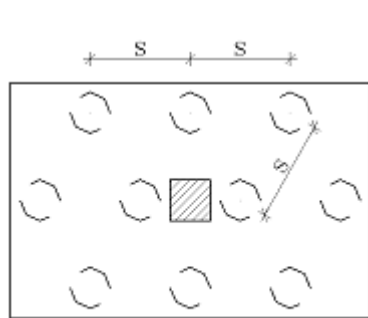


7 Piles

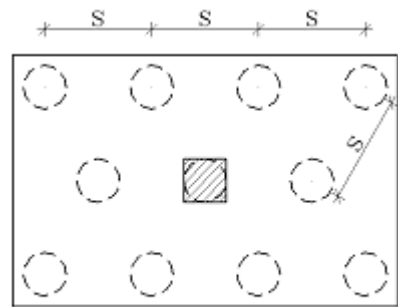


8 Piles

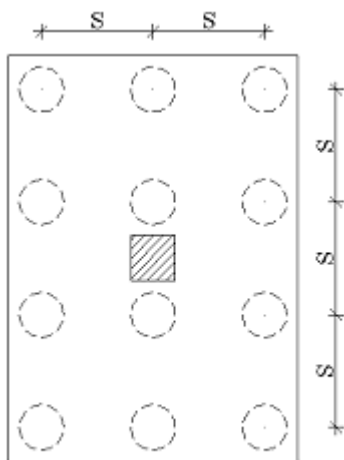
9 Piles



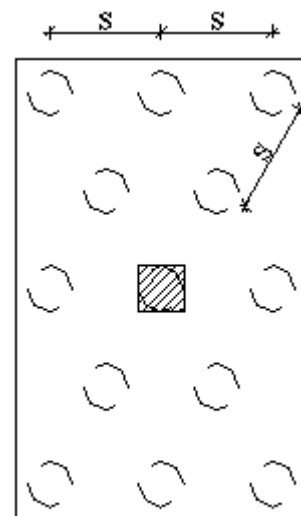
10 Piles



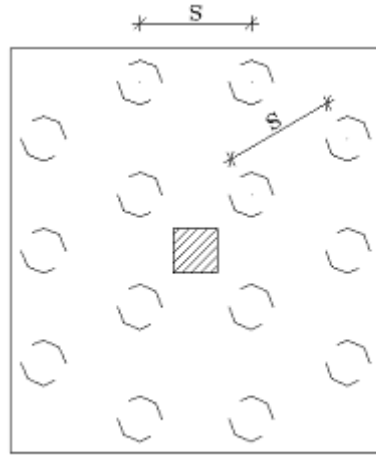
11 Piles



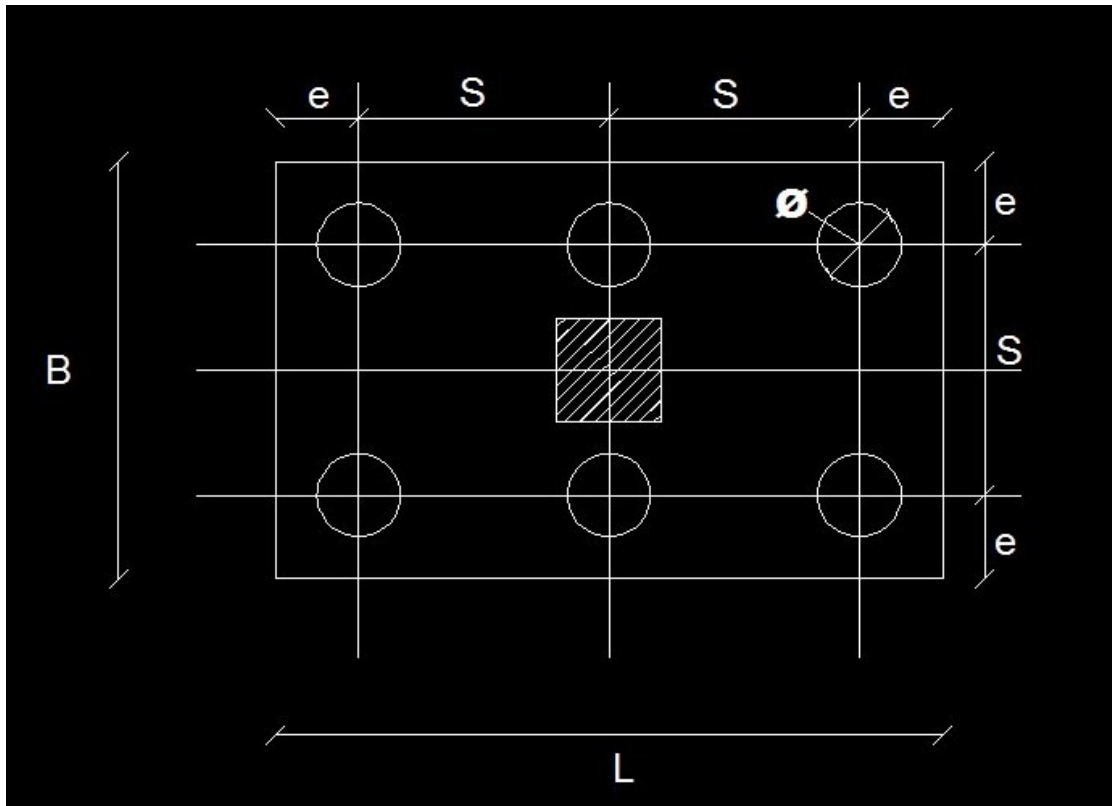
12 Piles



13 Piles



14 Piles



يراعي أن يكون العمود في C.G of pile cap
حتى تكون القاعدة مرتكزة علي العمود

Steps of Design:

$$1) \text{ No.of.pile} = \frac{1.15 \cdot p}{Q_{all}} + (1 \rightarrow 2)$$

approximated to the nearest bigger no \rightarrow
min 2 piles

2) Draw pile cap and get Dimention:

Thickness of PC = 10 cm

$$S_{min} = 3 \cdot v \rightarrow \text{for friction piles}$$

$$S_{min} = 2.5 \cdot v \rightarrow \text{for bearing piles}$$

$$S_{max} = 6 \cdot v$$

$$e = (1 \rightarrow 1.5) \cdot v$$

$$P_{pile} = \frac{1.1P}{\text{no.of piles}}$$

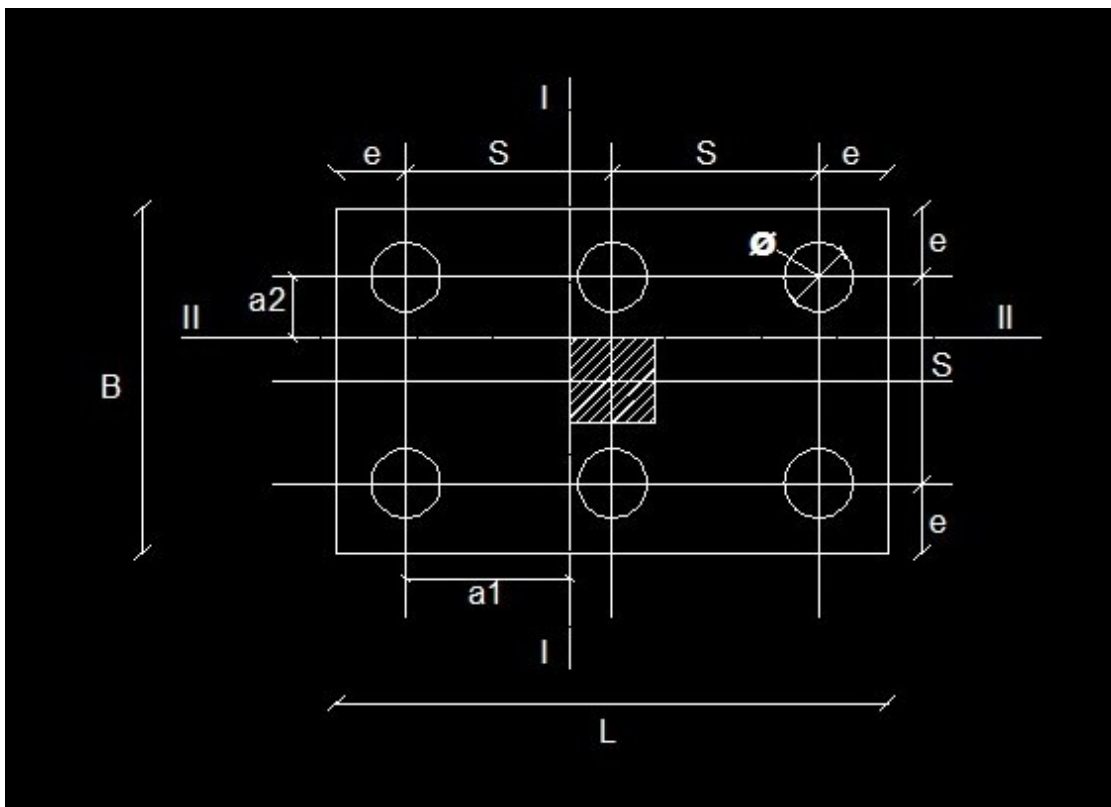
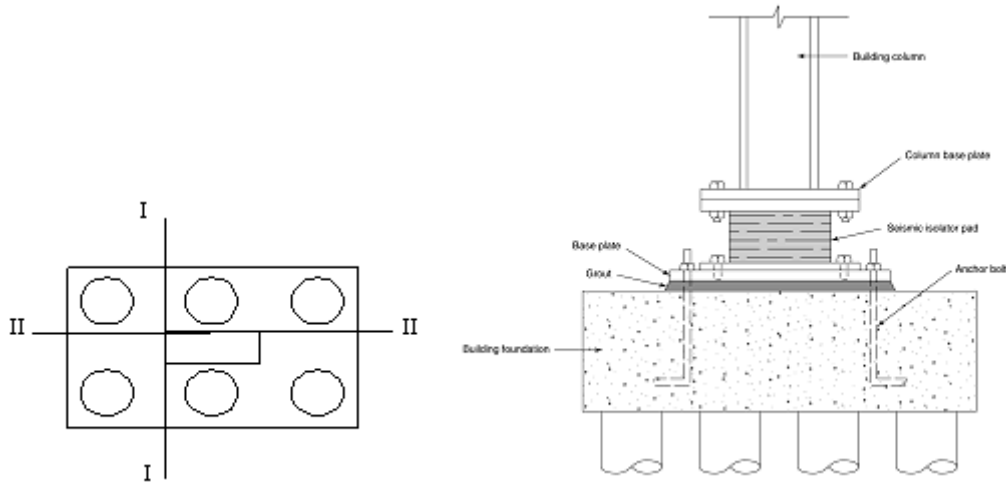
$$P_u = 1.5 \cdot P_{pile}$$

حيث أن:

$v \rightarrow$ pile diameter

3) Design for moment:

The critical section for moment is taken at the column face.



$$M_l = \text{no. of pile} * P_u * a_1$$

No. of piles →

عدد الخوازيق المقابل لل I

$$M_{II} = \text{no. of pile} * P_u * a_2$$

No. of piles →

عدد الخوازيق المقابل لل II

$$d_I = C_1 \sqrt{\frac{MuI}{F_{cu} * B}}$$

$$d_{II} = C_1 \sqrt{\frac{MuII}{F_{cu} * L}}$$

حيث أن:

$$C_1 = 5$$

Take the bigger of d_I , d_{II}

$$d_{\min} = \{(1.5 * v) + 10\text{cm}\}$$

حيث أن:

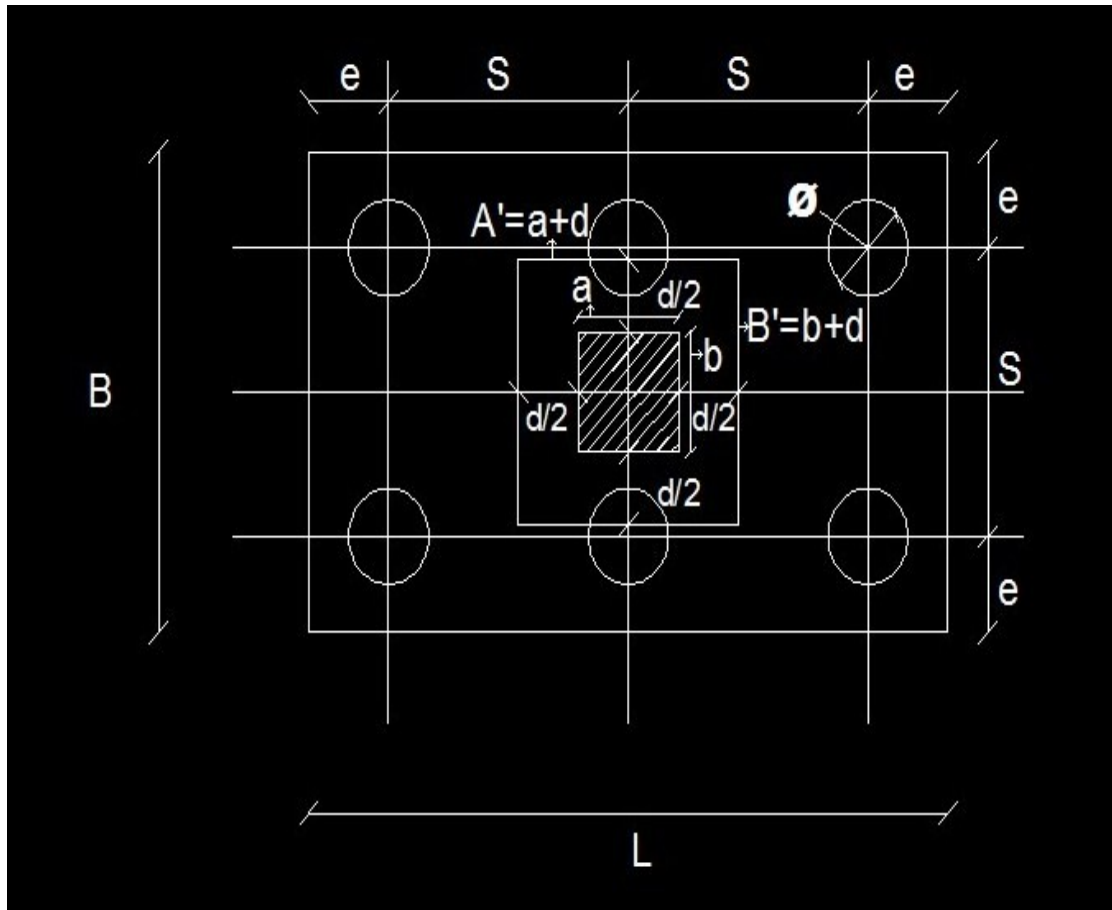
v → pile diameter

d_I , d_{II} , d_{\min} → depth of pile cap

$$t = d + \text{cover}$$

$$\text{cover} = (10 \text{ to } 15 \text{ cm})$$

Check Punching:



$$Q_p = p_u - p_{upile}$$

$$A' = (a + d) = \dots \text{ m}$$

$$B' = (b + d) = \dots \text{ m}$$

حيث أن:

$a \rightarrow$ عرض العمود , $b \rightarrow$ طول العمود

$d \rightarrow$ depth of pile cap

$p_{upile} \rightarrow$ parts of the piles inside the column, critical section at $d/2$ from the column as in shallow footing

$$\chi_c = 1.5$$

$$q_p = \frac{Q_p}{2 * (A' + B') * d} = \dots \text{ kg/cm}^2$$

$$q_{pcu} = \sqrt{\frac{F_{cu}}{\chi_c}} = \dots \text{ kg/cm}^2$$

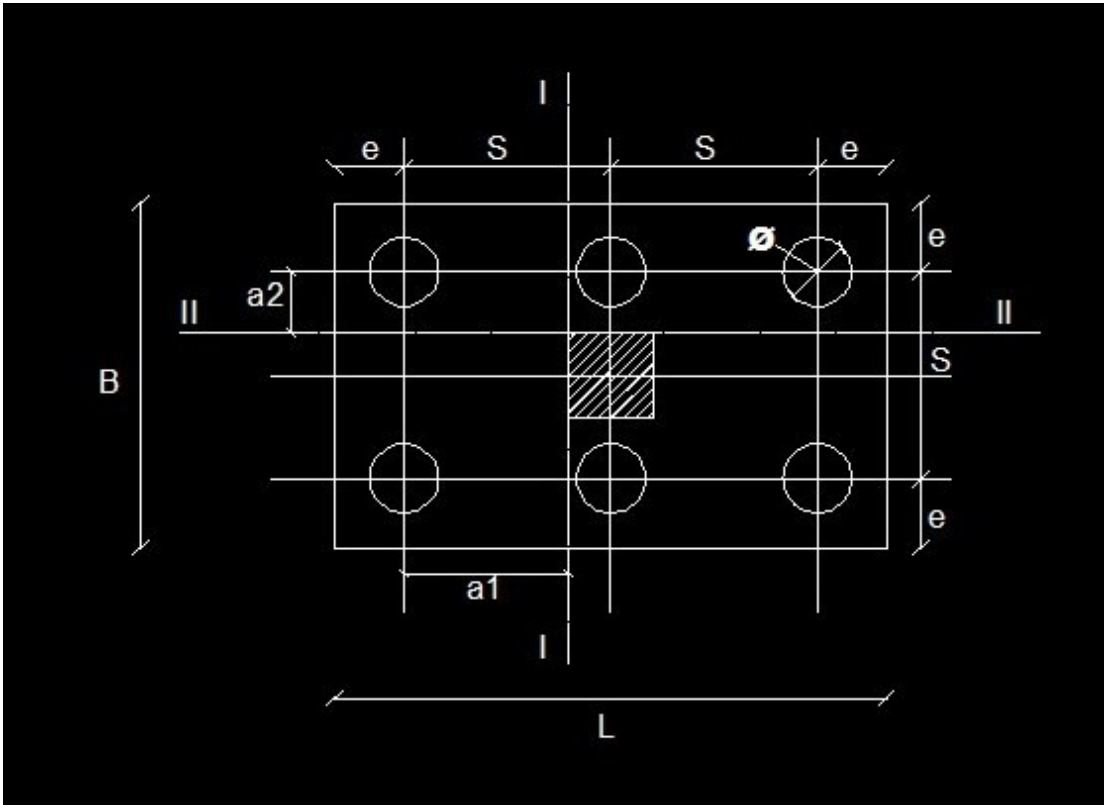
If $q_{pcu} > q_p$ ok safe

If $q_{pcu} < q_p$ un safe \rightarrow increase depth

$$t = d + \text{cover}$$

$$\text{cover} = (10 \text{ to } 15 \text{ cm})$$

Check Shear:



Q_{sh1} = sum no. of piles

No. of piles \rightarrow

مجموع حمل الخوازيق المقابل لل ا

$$q_{sh1} = \frac{Q_{sh1}}{B*d}$$

$$q_{cu} = 0.4 * \sqrt{F_{cu}}$$

if $q_{sh} < q_{cu}$ ok safe

if $q_{sh} > q_{cu}$ not safe increase depth

$$d = Q_{sh1} / (q_{cu} * B)$$

$$t = d + \text{cover}$$

$$\text{cover} = (10 \text{ to } 15 \text{ cm})$$

$$Q_{sh2} = \text{sum no. of piles}$$

No. of piles \rightarrow

مجموع حمل الخوازيق المقابل لل ||

$$q_{sh2} = \frac{Q_{sh1}}{L * d}$$

$$q_{cu} = 0.4 * \sqrt{F_{cu}}$$

if $q_{sh} < q_{cu}$ ok safe

if $q_{sh} > q_{cu}$ not safe increase depth

$$d = Q_{sh1} / (q_{cu} * L)$$

$$t = d + \text{cover}$$

$$\text{cover} = (10 \text{ to } 15 \text{ cm})$$

Reinforcement of the Cap Pile:

$$A_{s1} = M_{ultI} / J * d_I * f_y / B \text{ -----(1)}$$

$$A_{s2} = M_{ultII} / J * d_{II} * f_y / L \text{ -----(1)}$$

$$A_{s \min} = (0.15 / 100) * B * d \text{ -----(2)}$$

نأخذ القيمة الأكبر في القيم 1,2

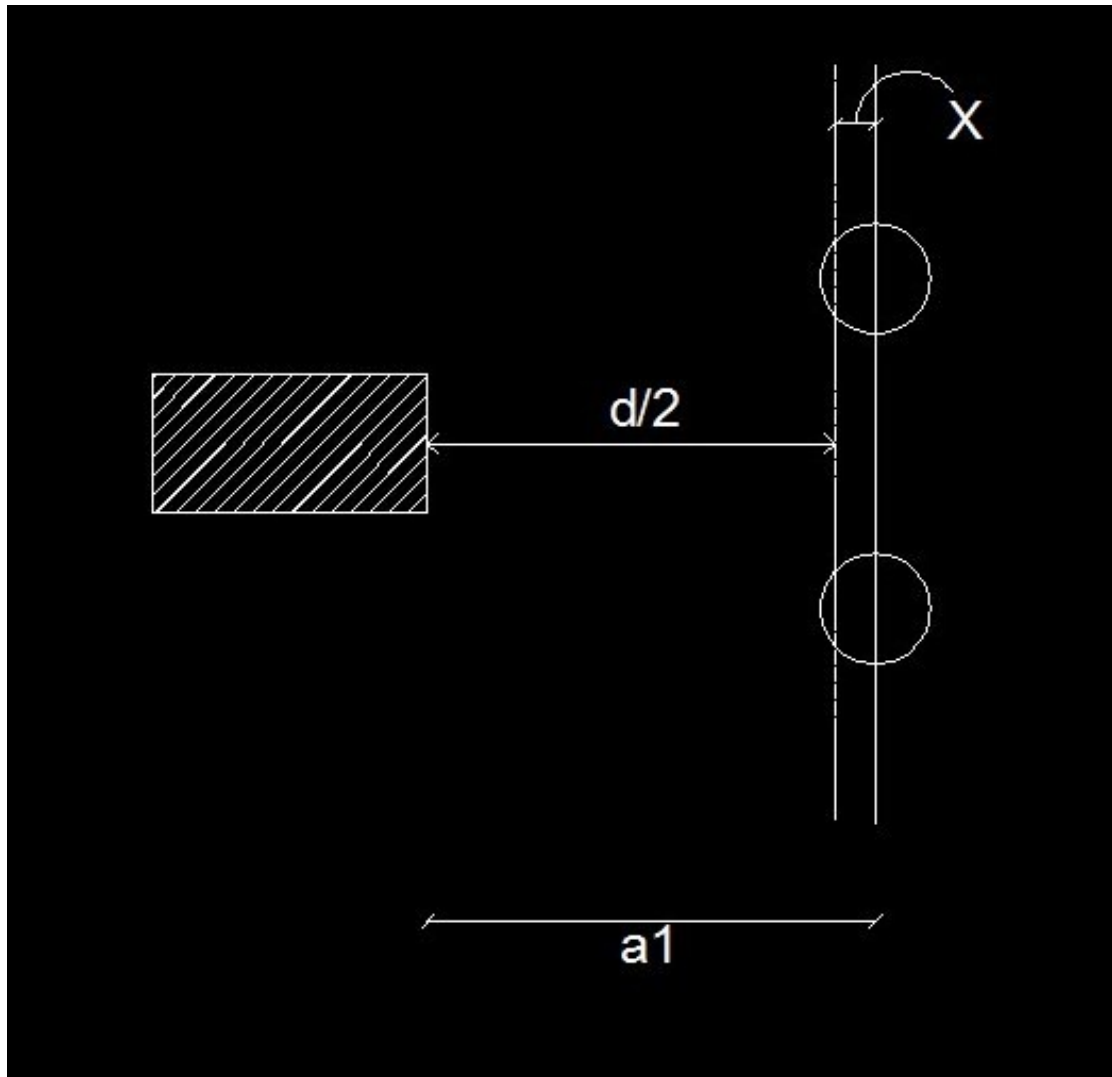
If $A_s \geq A_{s \min} \rightarrow ok$

If $A_s < A_{s \min} \rightarrow take A_s = A_{s \min}$

في حالة تساوي $B=L$ أبعاد القاعدة والشكل يكون متماثل:

Check Punching:

$$Q_p = \frac{Pu * (X + \frac{v}{2})}{v}$$



حيث أن:

$v \rightarrow$ pile diameter

$$A' = (a + d) = \dots \text{ m}$$

$$B' = (b + d) = \dots \text{ m}$$

حيث أن:

$a \rightarrow$ عرض العمود , $b \rightarrow$ طول العمود

$d \rightarrow$ depth of pile cap

$$\chi_c = 1.5$$

$$q_p = \frac{Q_p}{2 * (A' + B') * d} = \dots \text{ kg/cm}^2$$

$$q_{pcu} = \sqrt{\frac{F_{cu}}{\chi_c}} = \dots \text{ kg/cm}^2$$

If $q_{pcu} > q_p$ ok safe

If $q_{pcu} < q_p$ un safe \rightarrow increase depth

$$t = d + \text{cover}$$

$$\text{cover} = (10 \text{ to } 15 \text{ cm})$$

Check Shear:

$$Q_{sh} = Q_p * \text{No. of piles}$$

No. of piles \rightarrow

عدد الخوازيق المقابل لل || أو |

$$q_{sh} = \frac{Q_{sh}}{B * d}$$

$$q_{cu} = 0.4 * \sqrt{F_{cu}}$$

if $q_{sh} < q_{cu}$ ok safe

if $q_{sh} > q_{cu}$ not safe increase depth

$$d = Q_{sh} / (q_{cu} * B)$$

$$t = d + \text{cover}$$

cover = (10 to 15 cm)

Reinforcement of the Cap Pile:

$$A_s = M_{ult} / J * d * f_y \text{ -----(1)}$$

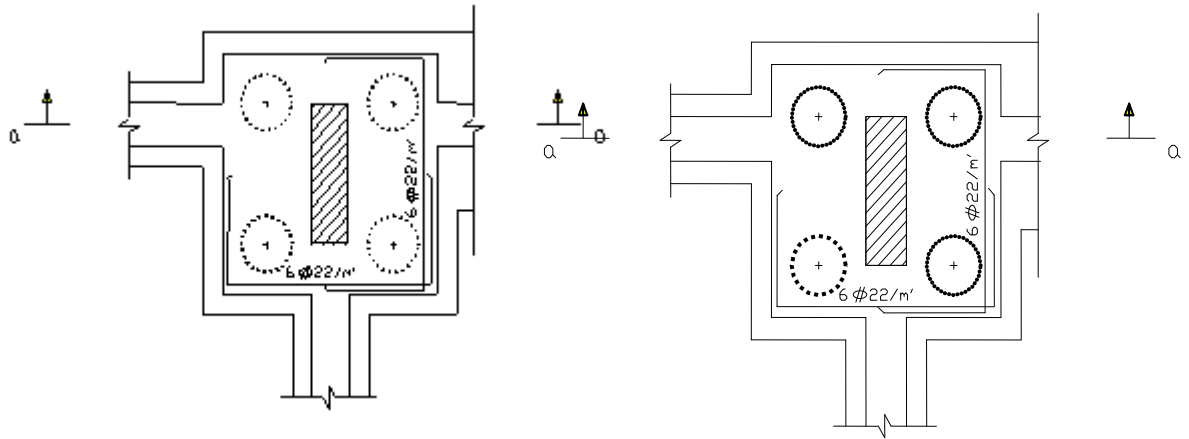
$$A_{s \min} = (0.15 / 100) * B * d \text{ -----(2)}$$

نأخذ القيمة الأكبر في القيم 1,2

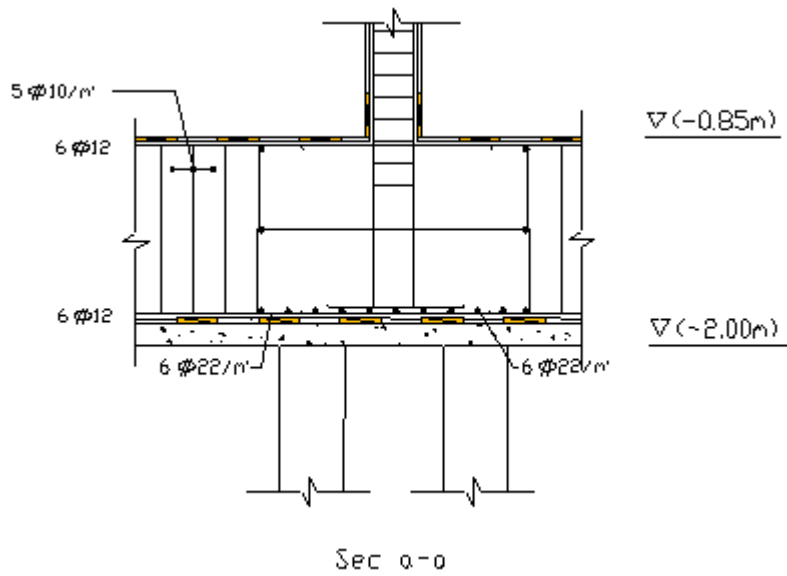
If $A_s \geq A_{s \min} \rightarrow$ ok

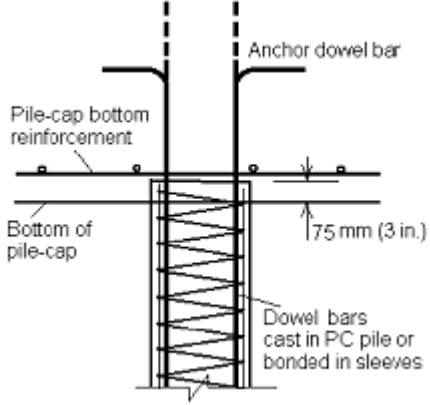
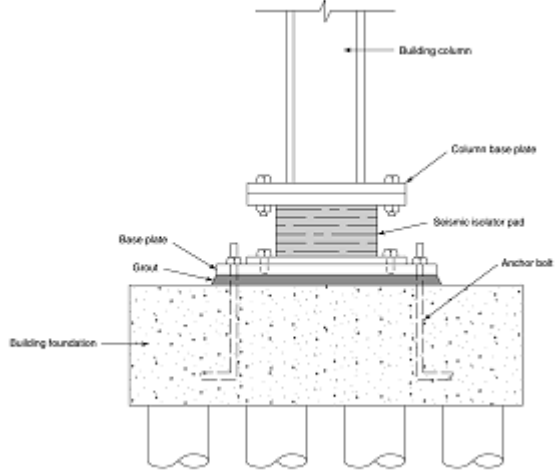
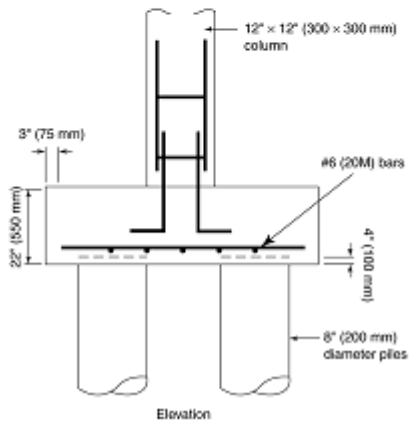
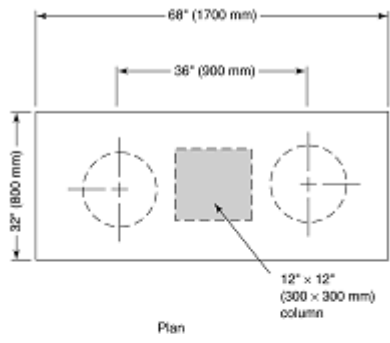
If $A_s < A_{s \min} \rightarrow$ take $A_s = A_{s \min}$

Details of reinforcement:



Plane





Example: 6

Given : Pile Diameter = 40 cm , $Q_{all} = 50 \text{ T}$,

$F_{cu} = 200 \text{ Kg/cm}^2$, $F_y = 3600 \text{ Kg/cm}^2$,

Column Caring = 200 T , Column Dimension = 60x60 cm

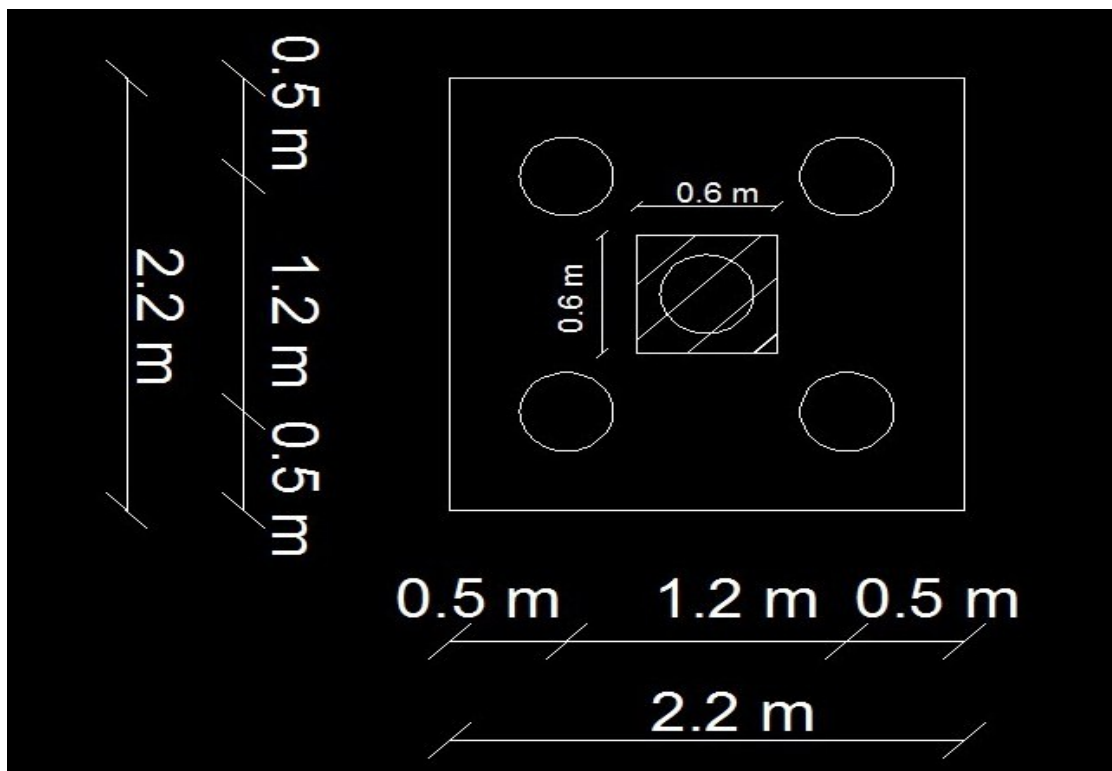
Req : Design Pile Cap.

Solution

$$\text{No.of.pile} = \frac{1.15 * p}{Q_{all}} = \frac{1.15 * 200}{50} = 4.6 \cong 5 \text{ piles}$$

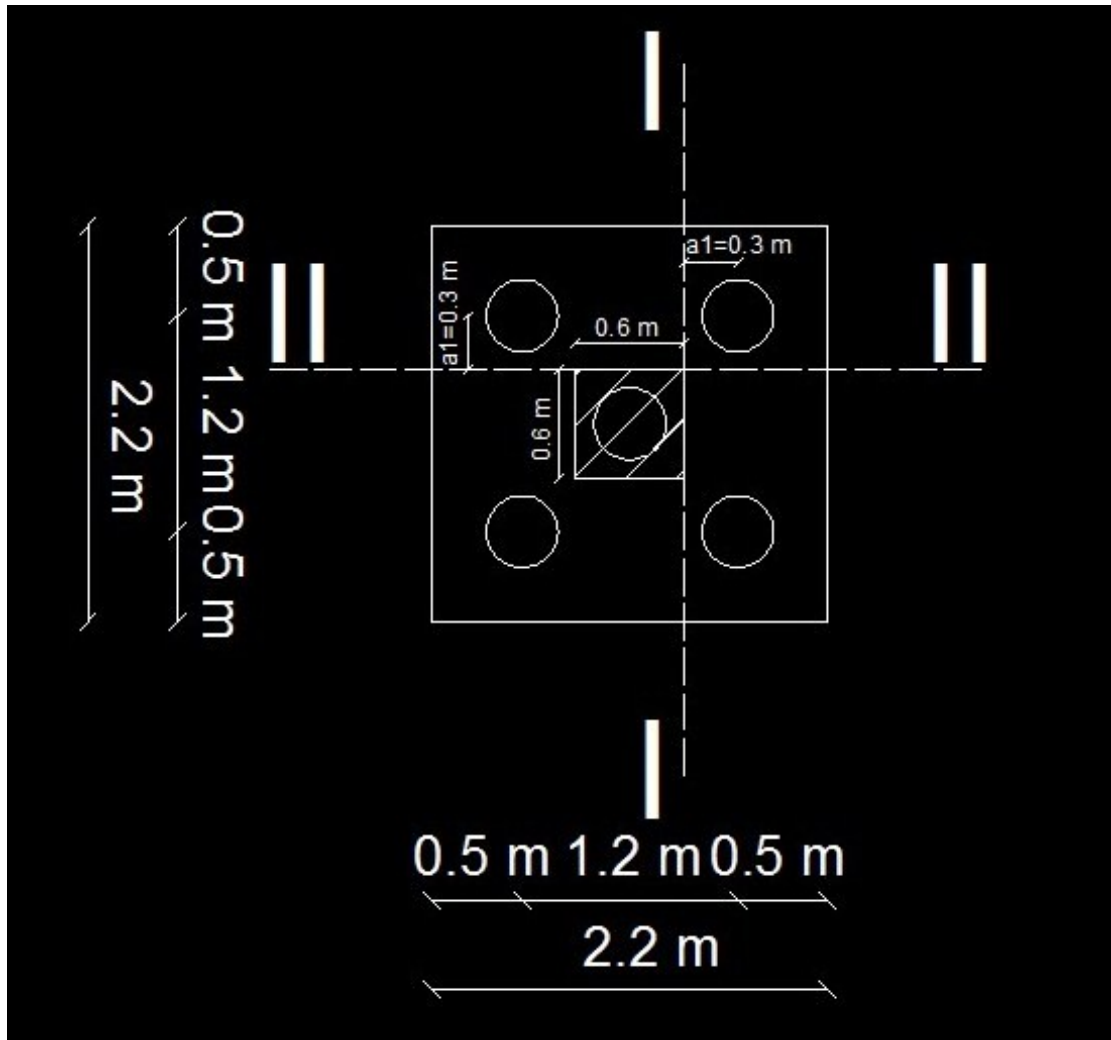
$$S = 3 * v = 3 * 0.4 = 1.2 \text{ m}$$

$$e = 1.25 * v = 1.25 * 0.4 = 0.5 \text{ m}$$



$$P_{\text{pile}} = \frac{1.1 * P}{\text{no. of piles}} = \frac{1.1 * 200}{5} = 44$$

$$P_u = 1.5 * P_{\text{pile}} = 1.5 * 44 = 66 \text{ T}$$



$$M_{ul-I} = M_{ull-II}$$

$$M_u = \text{no. of pile} * P_u * a = 2 * 66 * 0.3 = 39.6 \text{ m.t}$$

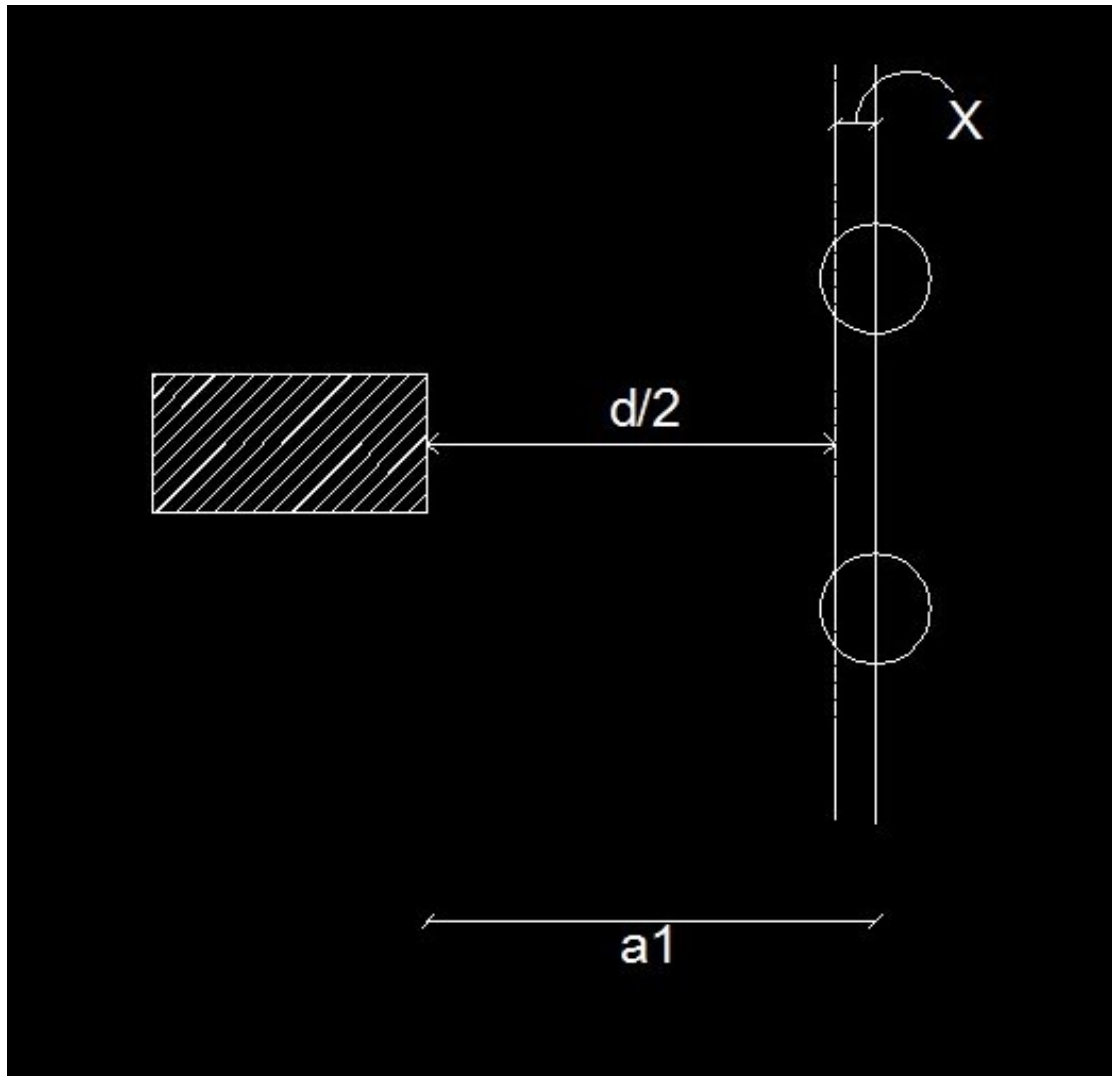
$$d = C_1 \sqrt{\frac{M_u}{F_{cu} * B}} = 5 \sqrt{\frac{39.6 * 10^5}{200 * 220}} = 47.43 \text{ cm} \cong 50 \text{ cm}$$

$$d_{\min} = \{(1.5 * v) + 10\text{cm}\} = \{(1.5 * 40) + 10\} = 70 \text{ cm}$$

take $d = 70 \text{ cm}$

Check Punching:

$$Q_p = \frac{P_u * (X + \frac{v}{2})}{v} = \frac{66 * (0.05 + \frac{0.4}{2})}{0.4} = 41.25 \text{ t}$$



$$A' = (a + d) = (0.6 + 0.7) = 1.3 \text{ m}$$

$$B' = (b + d) = (0.6 + 0.7) = 1.3 \text{ m}$$

$$q_p = \frac{Q_p}{2 * (A' + B') * d} = \frac{41.25 * 10^3}{2 * (130 + 130) * 70} = 1.13 \text{ kg/cm}^2$$

$$q_{pcu} = \sqrt{\frac{F_{cu}}{\gamma_c}} = \sqrt{\frac{200}{1.5}} = 11.55 \text{ kg/cm}^2$$

$$q_{pcu} > q_p$$

11.55 > 1.13 ok safe

$$t = d + \text{cover} = 70 + 10 = 80 \text{ cm}$$

Check Shear:

$$Q_{sh} = Q_p * \text{No. of piles} = 41.25 * 2 = 82.5$$

$$q_{sh} = \frac{Q_{sh}}{B * d} = \frac{82.5 * 10^3}{220 * 70} = 5.36 \text{ kg/cm}^2$$

$$q_{cu} = 0.4 * \sqrt{F_{cu}} = 0.4 * \sqrt{200} = 5.66 \text{ kg/cm}^2$$

$$q_{sh} < q_{cu}$$

5.36 < 5.66 ok safe

$$t = d + \text{cover} = 70 + 10 = 80 \text{ cm}$$

Reinforcement of the Cap Pile:

$$A_s = \frac{\text{Mult}}{J * d * F_y} = \frac{39.6 * 10^5}{0.826 * 70 * 3600} = 19.02 \text{ cm}^2$$

$$A_{s \text{ min}} = \frac{0.15}{100} * B * d = \frac{0.15}{100} * 220 * 70 = 23.1 \text{ cm}^2$$

$$A_s < A_{s \text{ min}}$$

$$\text{take } A_s = A_{s \text{ min}} = 23.1 \text{ cm}^2$$

Use 10 y 18

يتم رسم التسليح كما في الشرح.

If columns subjected to P & M

"Permanent ":

Steps of Design:

$$1) \text{ No.of.pile} = \frac{1.15 * p}{Q_{all}} + (1 \rightarrow 2)$$

approximated to the nearest bigger no \rightarrow
min 2 piles

2) Draw pile cap and get Dimention:

Thickness of PC = 10 cm

$$S_{min} = 3 * v \rightarrow \text{for friction piles}$$

$$S_{min} = 2.5 * v \rightarrow \text{for bearing piles}$$

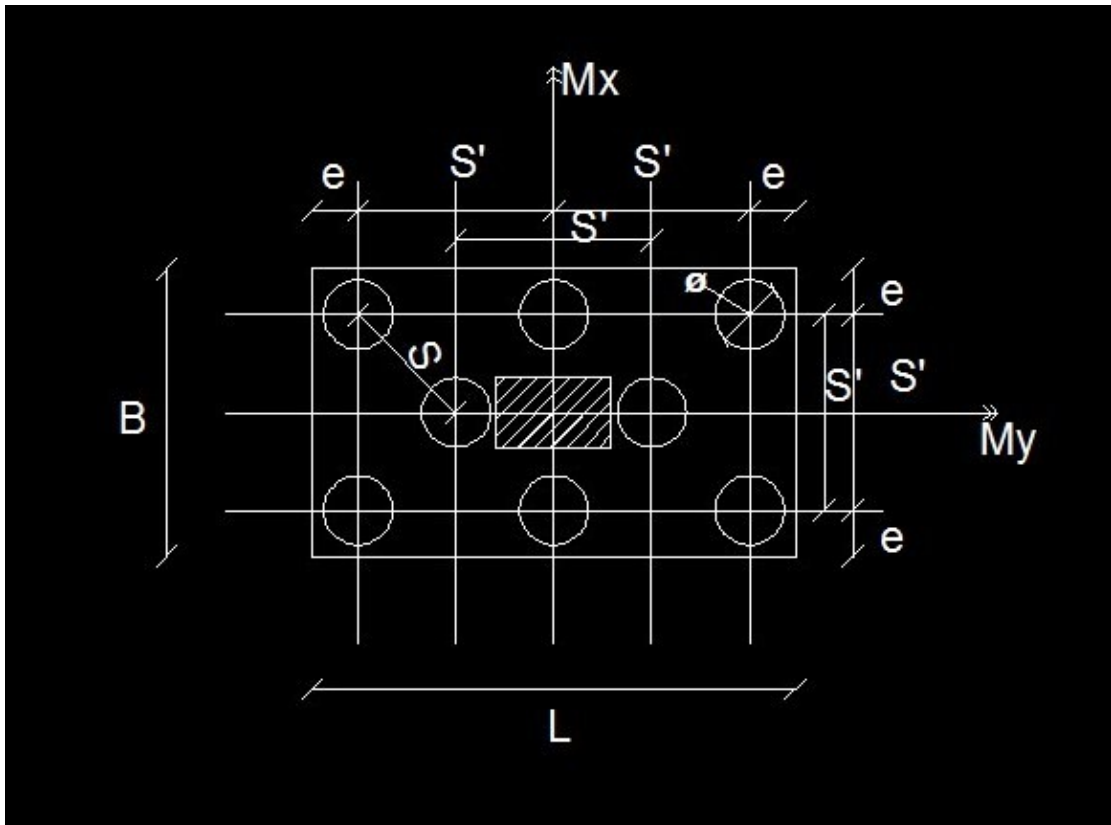
$$S_{max} = 6 * v$$

$$e = (1 \rightarrow 1.5) * v$$

$$S' = \sqrt{(S)^2 + (S)^2}$$

حيث أن:

$v \rightarrow$ pile diameter



Case of M_y :

$$P_i = P_{\max, \min} = \frac{1.15 \cdot P}{\text{no. of pile}} \pm \frac{M_y}{\sum X^2} * X \pm \frac{M_x}{\sum Y^2} * Y$$

$$P_{\max} < \frac{P_{\text{all}}}{\text{pile}}$$

$P_{\min} > \text{zero} \rightarrow \text{if } P_{\min} \text{ (-ve)} < T_{\text{all}} \text{ (friction)}$

If unsafe:

Increase no. of pile

OR

Increase S

OR

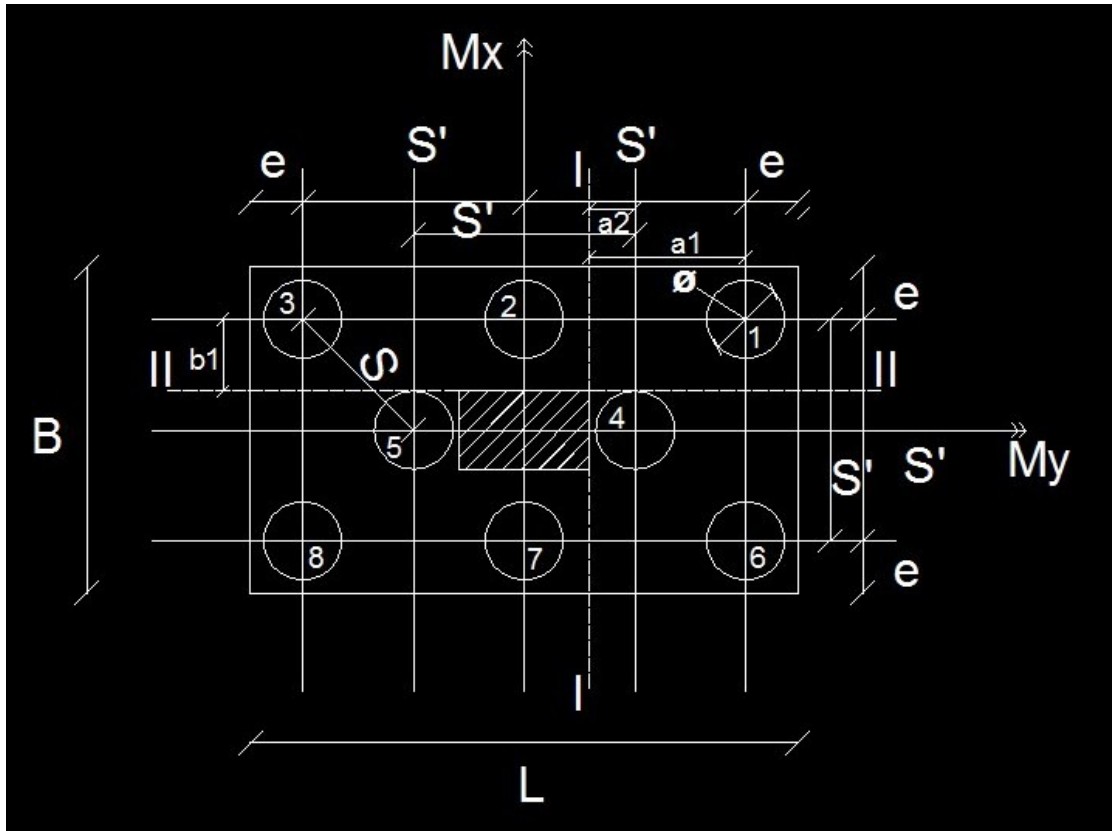
Increase length of piles

يتم عمل جدول كلاتي:

No. of pile	Y	Y ²	X	X ²	Pi
1	Y1	(Y1) ²	X1	(X1) ²	Form eq
2	Y2	(Y2) ²	X2	(X2) ²	Form eq
3	Y3	(Y3) ²	X3	(X3) ²	Form eq
4	Y4	(Y4) ²	X4	(X4) ²	Form eq
5	Y5	(Y5) ²	X5	(X5) ²	Form eq
...
...
		$\sum Y^2$			$\sum X^2$

Design for moment:

The critical section for moment is taken at the column face.



$$M_I = (P_1 + P_6) * a_1 + (p_4) * a_2$$

$P_1, P_6, P_4 \rightarrow$

عدد الخوازيق المقابل لل I

$$M_{II} = (P_1 + P_2 + P_3) * b_1$$

$P_1 + P_2 + P_3 \rightarrow$

عدد الخوازيق المقابل لل II

$$d_I = C_1 \sqrt{\frac{MuI}{F_{cu} * B}}$$

$$d_{II} = C_1 \sqrt{\frac{MuII}{F_{cu} * L}}$$

حيث أن:

$$C_1 = 5$$

Take the bigger of d_I , d_{II}

$$d_{\min} = \{(1.5 * v) + 10 \text{cm}\}$$

حيث أن:

$v \rightarrow$ pile diameter

d_I , d_{II} , $d_{\min} \rightarrow$ depth of pile cap

$$t = d + \text{cover}$$

$$\text{cover} = (10 \text{ to } 15 \text{ cm})$$

Check Punching:

$$Q_p = p_u - p_{upile}$$

$$A' = (a + d) = \dots \text{ m}$$

$$B' = (b + d) = \dots \text{ m}$$

حيث أن:

$a \rightarrow$ عرض العمود , $b \rightarrow$ طول العمود

$d \rightarrow$ depth of pile cap

$p_{upile} \rightarrow$ *parts of the piles inside the column, critical section at $d/2$ from the column as in shallow footing*

$$\chi_c = 1.5$$

$$q_p = \frac{Q_p}{2 * (A' + B') * d} = \dots \text{ kg/cm}^2$$

$$q_{pcu} = \sqrt{\frac{F_{cu}}{\chi_c}} = \dots \text{ kg/cm}^2$$

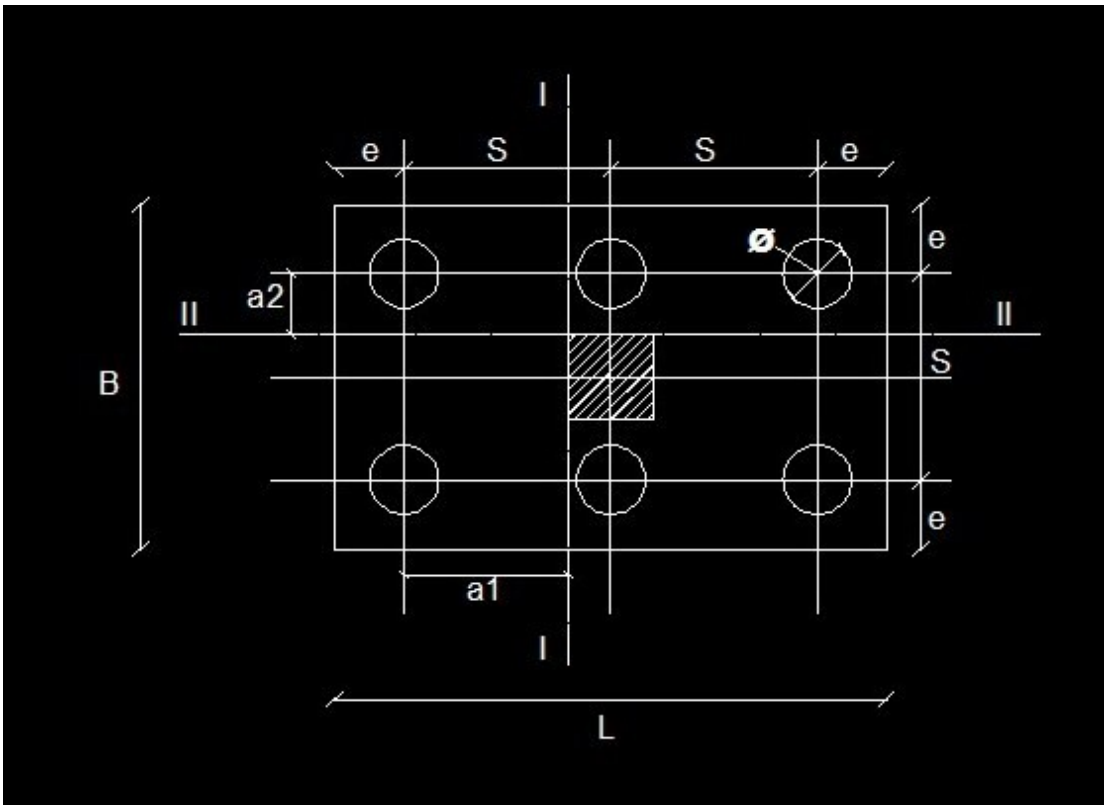
If $q_{pcu} > q_p$ ok safe

If $q_{pcu} < q_p$ un safe \rightarrow increase depth

$$t = d + \text{cover}$$

$$\text{cover} = (10 \text{ to } 15 \text{ cm})$$

Check Shear:



Q_{sh1} = sum no. of piles

No. of piles \rightarrow

مجموع حمل الخوازيق المقابل لل ا

$$q_{sh1} = \frac{Q_{sh1}}{B * d}$$

$$q_{cu} = 0.4 * \sqrt{F_{cu}}$$

if $q_{sh} < q_{cu}$ ok safe

if $q_{sh} > q_{cu}$ not safe increase depth

$$d = Q_{sh1} / (q_{cu} * B)$$

$$t = d + \text{cover}$$

$$\text{cover} = (10 \text{ to } 15 \text{ cm})$$

Q_{sh2} = sum no. of piles

No. of piles \rightarrow

مجموع حمل الخوازيق المقابل لل ||

$$q_{sh2} = \frac{Q_{sh1}}{L * d}$$

$$q_{cu} = 0.4 * \sqrt{F_{cu}}$$

if $q_{sh} < q_{cu}$ ok safe

if $q_{sh} > q_{cu}$ not safe increase depth

$$d = Q_{sh1} / (q_{cu} * L)$$

$$t = d + \text{cover}$$

$$\text{cover} = (10 \text{ to } 15 \text{ cm})$$

Reinforcement of the Cap Pile:

$$A_{s1} = M_{ultI} / J * d_I * f_y / B \text{ -----(1)}$$

$$A_{s2} = M_{ultII} / J * d_{II} * f_y / L \text{ -----(1)}$$

$$A_{s \text{ min}} = (0.15 / 100) * B * d \text{ -----(2)}$$

نأخذ القيمة الأكبر في القيم 1,2

If $A_s \geq A_{s \text{ min}} \rightarrow \text{ok}$

If $A_s < A_{s \text{ min}} \rightarrow \text{take } A_s = A_{s \text{ min}}$

Example: 7

Given : Pile Diameter = 80 cm , $Q_{all} = 192 \text{ T}$, $Q_{ult} = 200 \text{ T}$

$F_{cu} = 350 \text{ Kg/cm}^2$, $F_y = 3600 \text{ Kg/cm}^2$, $M_x = 290.22 \text{ m.t}$

$M_y = 55.71 \text{ m.t}$, Column Caring = 1020 T

Column Dimension = 250x120 cm

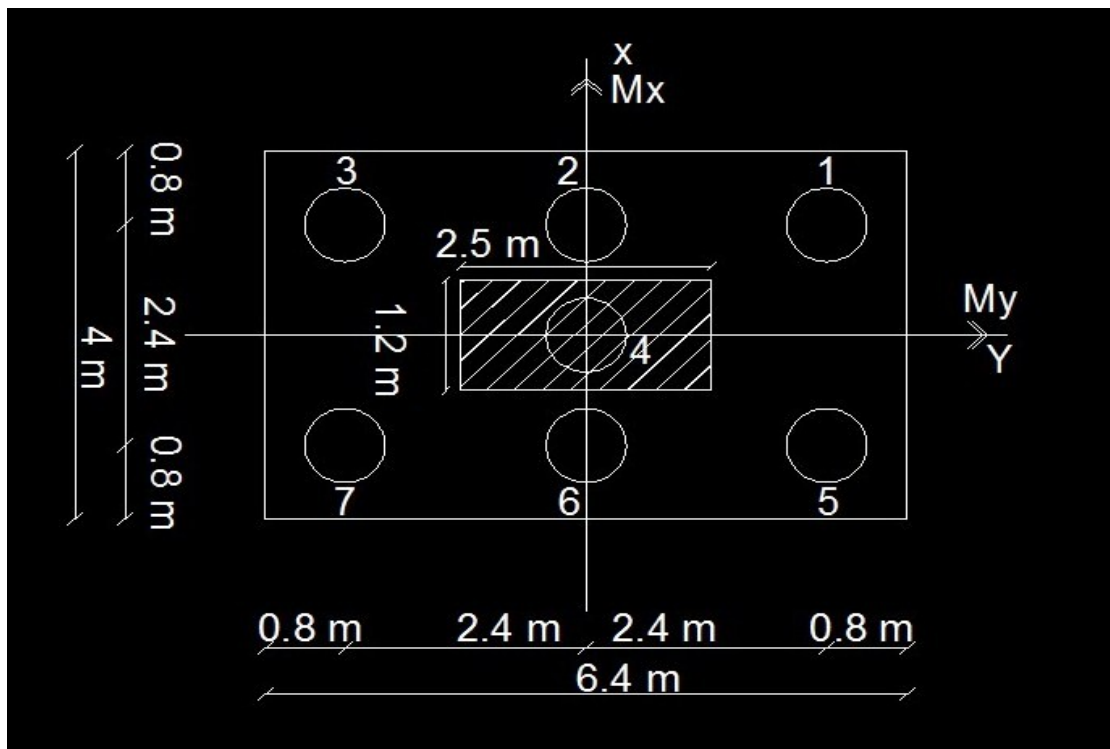
Req : Design Pile Cap.

Solution

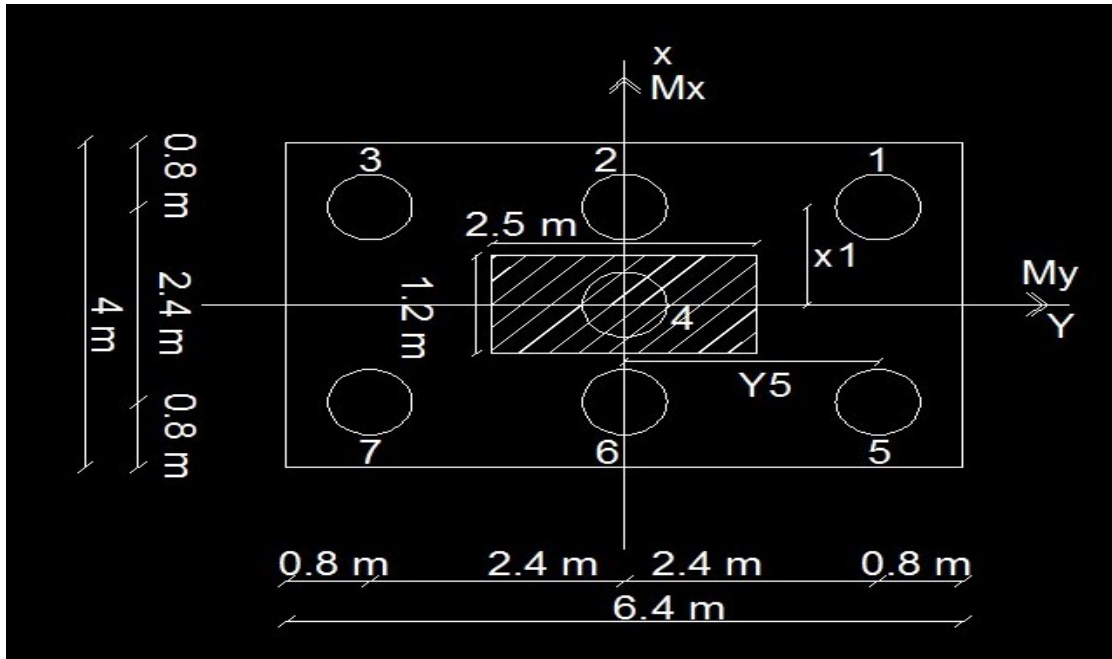
$$\text{No.of.pile} = \frac{1.1 * p}{Q_{all}} = \frac{1.15 * 1020}{192} = 6.11 \cong 7 \text{ piles}$$

$$S = 3 * v = 3 * 0.8 = 2.4 \text{ m}$$

$$e = 1 * v = 1 * 0.8 = 0.8 \text{ m}$$



يتم عمل جدول:



No. of pile	Y	Y ²	X	X ²	P _i
1	2.4	5.76	1.2	1.44	-205.55
2	0	0	1.2	1.44	-159.83
3	2.4	5.76	1.2	1.44	-190.07
4	0	0	0	0	-167.57
5	2.4	5.76	1.2	1.44	-190.07
6	0	0	1.2	1.44	-159.83
7	2.4	5.76	1.2	1.44	-129.59
		\sum 23.04		\sum 8.64	

$$P_i = \frac{1.15 * P}{\text{no. of pile}} \pm \frac{M_x}{\sum Y^2} * y \pm \frac{M_y}{\sum X^2} * x$$

$$\frac{1.15*P}{\text{no.of pile}} = \frac{1.15*1020}{7} = 167.57$$

$$\frac{M_y}{\sum X^2} = \frac{55.71}{8.64} = 6.45$$

$$\frac{M_x}{\sum Y^2} = \frac{290.22}{23.04} = 12.6$$

$$P_{i(1)} = -167.57 - (12.6*2.4) - (6.45*1.2) = -205.55$$

$$P_{i(2)} = -167.57 - 0 + (6.45*1.2) = -159.83$$

$$P_{i(3)} = -167.57 + (12.6*2.4) + (6.45*1.2) = -190.07$$

$$P_{i(4)} = -167.57 - 0 - 0 = -167.57$$

$$P_{i(5)} = -167.57 - (12.6*2.4) + (6.45*1.2) = -190.07$$

$$P_{i(6)} = -167.57 - 0 + (6.45*1.2) = -159.83$$

$$P_{i(7)} = -167.57 + (12.6*2.4) + (6.45*1.2) = -129.59$$

$$P_{i(1)} > Q_{ult}$$

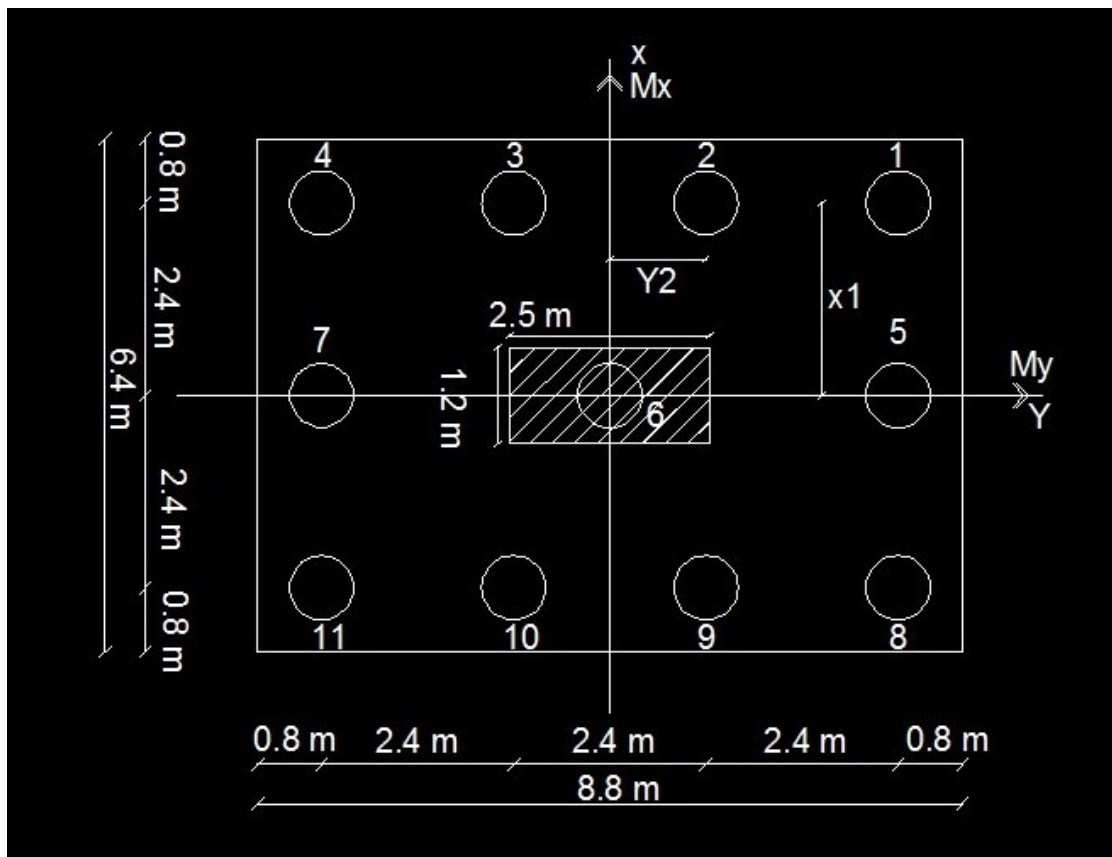
205.55 > 200 unsafe

Increase no. of pile

Taken 8 piles

يتم زيادة عدد الخوازيق بزيادة 1 وكل مرة نشوف الشرط انا
قمت بزيادة عدد الخوازيق والشرط لم يتحقق الا لم تم أخذ
11 خوازيق.

Taken no. of pile = 11 piles



يتم عمل جدول:

No. of pile	Y	Y ²	X	X ²	P _i
1	3.6	12.96	2.4	5.76	-122.04
2	1.2	1.44	2.4	5.76	-113.71
3	1.2	1.44	2.4	5.76	-105.38
4	3.6	12.96	2.4	5.76	-97.05
5	3.6	12.96	0	0	-119.13
6	0	0	0	0	-106.64
7	3.6	12.96	0	0	-94.15
8	3.6	12.96	2.4	5.76	-116.23
9	1.2	1.44	2.4	5.76	-107.9
10	1.2	1.44	2.4	5.76	-99.58
11	3.6	12.96	2.4	5.76	-91.25
		\sum 83.52		\sum 46.08	

$$P_i = \frac{1.15 \cdot P}{\text{no. of pile}} \pm \frac{M_x}{\sum Y^2} * y \pm \frac{M_y}{\sum X^2} * x$$

$$\frac{1.15 \cdot P}{\text{no. of pile}} = \frac{1.15 \cdot 1020}{11} = 106.64$$

$$\frac{M_y}{\sum X^2} = \frac{55.71}{46.08} = 1.21$$

$$\frac{M_x}{\sum Y^2} = \frac{290.22}{83.52} = 3.47$$

$$P_{i(1)} = -106.64 - (3.47 \cdot 3.6) - (1.21 \cdot 2.4) = -122.04$$

$$P_{i(2)} = -106.64 - (3.47 * 1.2) - (1.21 * 2.4) = -113.71$$

$$P_{i(3)} = -106.64 + (3.47 * 1.2) - (1.21 * 2.4) = -105.38$$

$$P_{i(4)} = -106.64 + (3.47 * 3.6) - (1.21 * 2.4) = -97.05$$

$$P_{i(5)} = -106.64 - (3.47 * 3.6) - 0 = -119.13$$

$$P_{i(6)} = -106.64 - 0 - 0 = -106.64$$

$$P_{i(7)} = -106.64 + (3.47 * 3.6) - 0 = -94.15$$

$$P_{i(8)} = -106.64 - (3.47 * 3.6) + (1.21 * 2.4) = -116.23$$

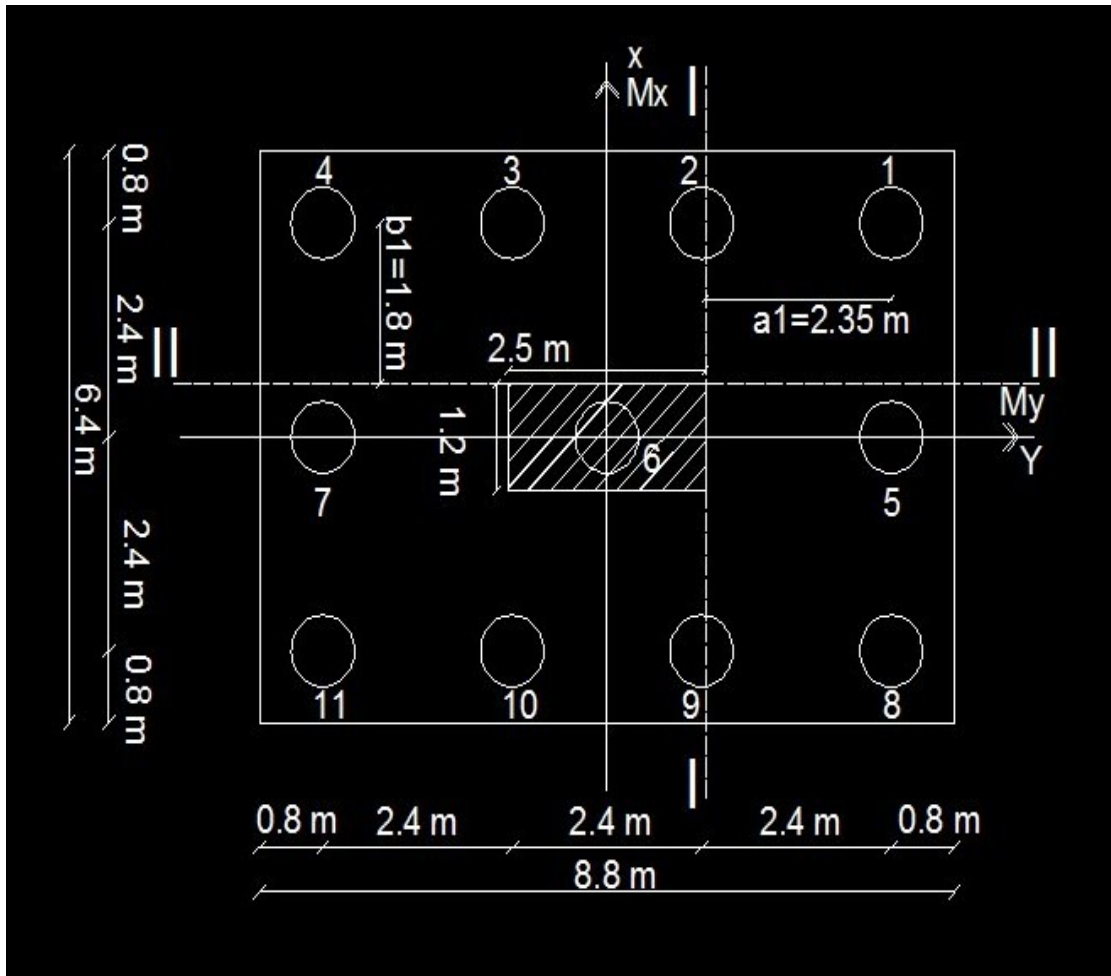
$$P_{i(9)} = -106.64 - (3.47 * 1.2) + (1.21 * 2.4) = -107.9$$

$$P_{i(10)} = -106.64 + (3.47 * 1.2) + (1.21 * 2.4) = -99.58$$

$$P_{i(11)} = -106.64 + (3.47 * 3.6) + (1.21 * 2.4) = -91.25$$

$$P_{i(1)} < Q_{ult}$$

$$122.04 < 200 \quad \text{safe}$$



$$M_I = (P_{i(1)} + P_{i(5)} + P_{i(8)}) * a_1$$

$$= (122.04 + 119.13 + 116.23) * 2.35 = 839.89 \text{ m.t}$$

$$M_{II} = (P_{i(1)} + P_{i(2)} + P_{i(3)} + P_{i(4)}) * b_1$$

$$= (122.04 + 113.71 + 105.38 + 97.05) * 1.8$$

$$= 788.72 \text{ m.t}$$

$$d_I = C_1 \sqrt{\frac{M_{uI}}{F_{cu} * B}}$$
$$= 5 \sqrt{\frac{839.89 * 10^5}{350 * 640}} = 96.82 \text{ cm} \cong 100 \text{ cm}$$

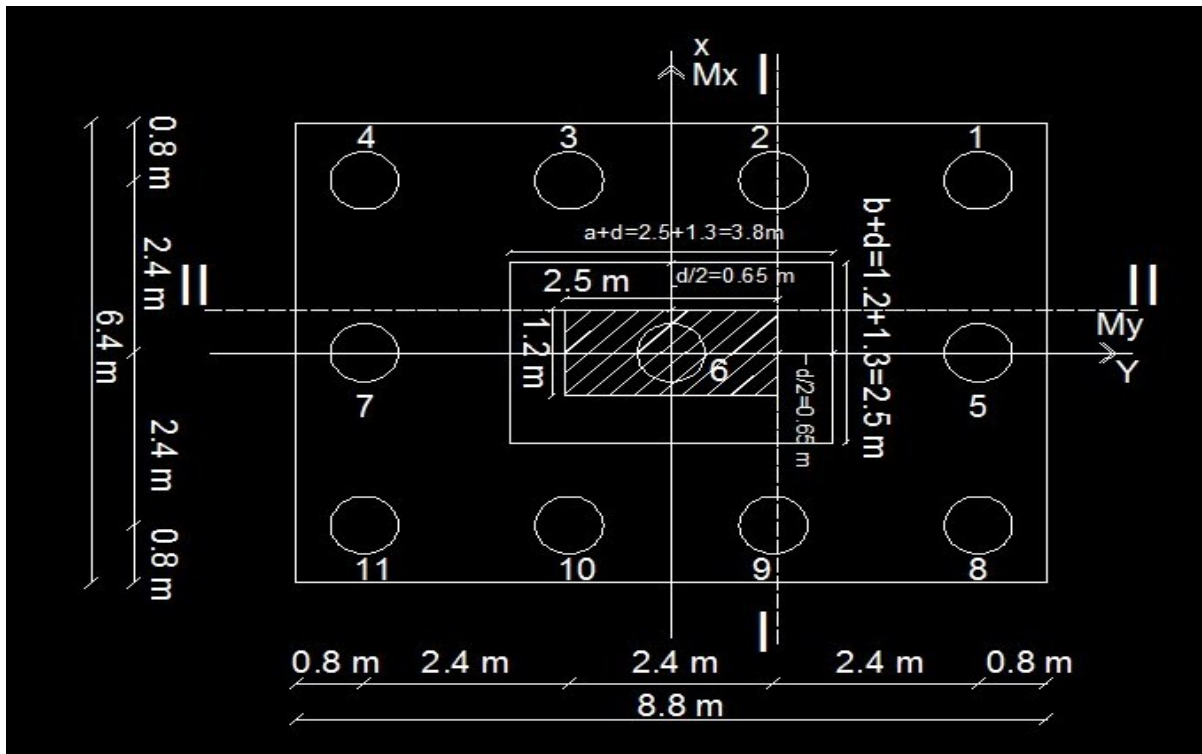
$$d_{II} = C_1 \sqrt{\frac{M_{uII}}{F_{cu} * L}}$$
$$= 5 \sqrt{\frac{788.72 * 10^5}{350 * 880}} = 80 \text{ cm} \cong 85 \text{ cm}$$

$$d_{\min} = \{(1.5 * v) + 10 \text{ cm}\}$$
$$= \{(1.5 * 80) + 10\} = 130 \text{ cm}$$

Take $d = 130 \text{ cm}$

$$t = d + \text{cover} = 130 + 10 = 140 \text{ cm}$$

Check Punching:



$$Q_p = p_{col} - p_{i(6)} = 1020 - 106.64 = 913.36 \text{ T}$$

$$A' = (a + d) = (2.5 + 1.3) = 3.8 \text{ m}$$

$$B' = (b + d) = (1.2 + 1.3) = 2.5 \text{ m}$$

$$q_p = \frac{Q_p}{2 * (A' + B') * d} = \frac{913.36 * 10^3}{2 * (380 + 250) * 130} = 5.58 \text{ kg/cm}^2$$

$$q_{pcu} = \sqrt{\frac{F_{cu}}{\gamma_c}} = \sqrt{\frac{350}{1.5}} = 15.28 \text{ kg/cm}^2$$

$$q_{pcu} > q_p$$

$$15.28 > 5.58 \quad \text{ok safe}$$

$$t = d + \text{cover} = 130 + 10 = 140 \text{ cm}$$

Check Shear:

$$Q_{sh1} = (P_{i(1)} + P_{i(5)} + P_{i(8)})$$

$$= (122.04 + 119.13 + 116.23) = 357.4 \text{ T}$$

$$q_{sh1} = \frac{Q_{sh1}}{B*d} = \frac{357.4 * 10^3}{640 * 130} = 4.3 \text{ kg/cm}^2$$

$$q_{cu} = 0.4 * \sqrt{F_{cu}} = 0.4 * \sqrt{350} = 7.48$$

$$\text{kg/cm}^2 \quad q_{sh1} < q_{cu}$$

$$4.3 < 7.48 \quad \text{ok safe}$$

$$t = d + \text{cover} = 130 + 10 = 140 \text{ cm}$$

$$Q_{sh2} = (P_{i(1)} + P_{i(2)} + P_{i(3)} + P_{i(4)})$$

$$= (122.04 + 113.71 + 105.38 + 97.05)$$

$$= 438.18 \text{ T}$$

$$q_{sh2} = \frac{Q_{sh2}}{L*d} = \frac{438.18 * 10^3}{880 * 130} = 3.83 \text{ kg/cm}^2$$

$$q_{cu} = 0.4 * \sqrt{F_{cu}} = 0.4 * \sqrt{350} = 7.48$$

$$\text{kg/cm}^2$$

$$q_{sh2} < q_{cu}$$

$$3.83 < 7.48 \quad \text{ok safe}$$

$$t = d + \text{cover} = 130 + 10 = 140 \text{ cm}$$

Reinforcement of the Cap Pile:

$$A_{sl} = \frac{\text{Mult I}}{J*d*F_y} = \frac{839.89*10^5}{0.826*130*3600}$$
$$= 217.27 \text{ cm}^2 / B = 217.27 / 6.4 = 34 \text{ cm}^2$$

Use 9 y 22

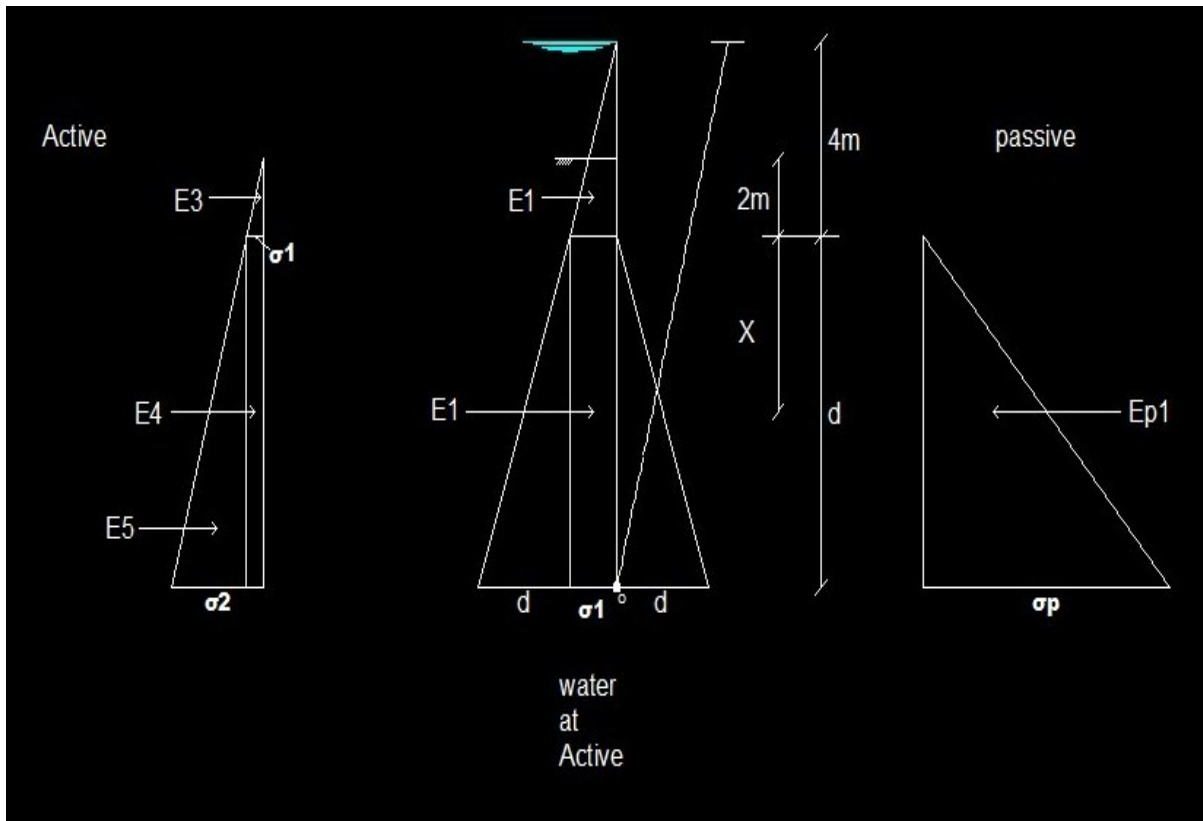
$$A_{sII} = \frac{\text{Mult II}}{J*d*F_y} = \frac{788.72*10^5}{0.826*130*3600}$$
$$= 204.03 \text{ cm}^2 / L = 204.03 / 8.8 = 23.19 \text{ cm}^2$$

Use 7 y 22

$$A_{s \text{ min}} = \frac{0.15}{100} * B * d = \frac{0.15}{100} * 100 * 130 = 19.5 \text{ cm}^2$$

يتم رسم التسليح كما في الشرح.

6) Design of steel sheet piles:

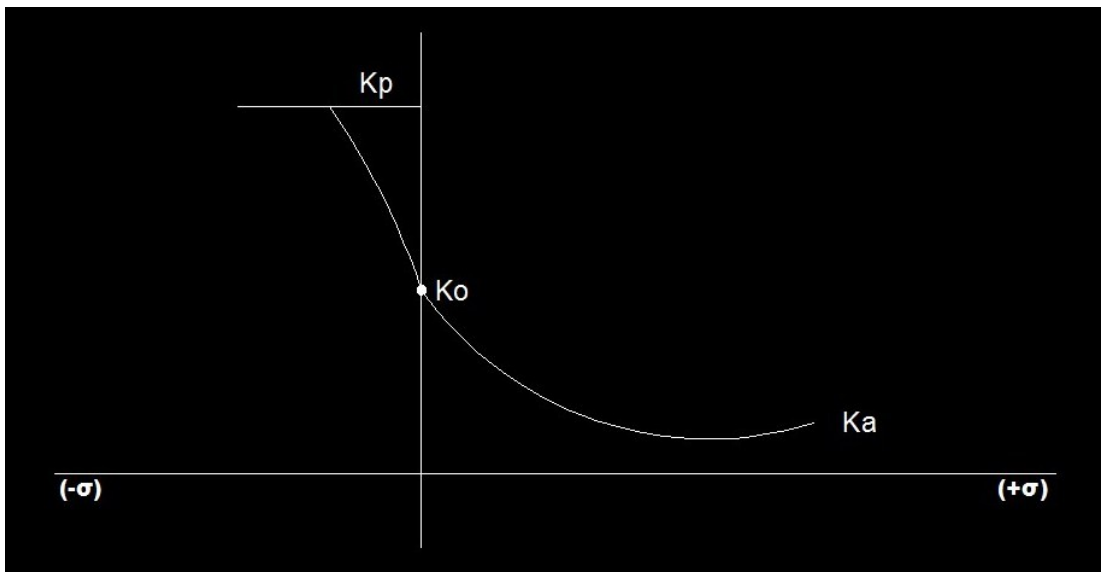


$$\text{Water press} = \gamma_w * h_w$$

$$\sigma_1 = 1 * 4 = 4 \text{ t/m}^2$$

$$\sigma_2 = (1 * d) + 4 = (4 + d) \text{ t/m}^2$$

Take $\nu = 30$



$$K_a = \frac{1 - \sin \nu}{1 + \sin \nu} = \frac{1 - \sin 30}{1 + \sin 30} = 0.333$$

$$K_a = \frac{1 + \sin \nu}{1 - \sin \nu} = \frac{1 + \sin 30}{1 - \sin 30} = 3$$

$$K_o = 1 - \sin \nu = 1 - \sin 30 = 0.5$$

$$\sigma_{@ (1)} = \gamma * H * K_a = 0.8 * 2 * 0.333 = 0.533 \text{ t/m}^2$$

$$\begin{aligned} \sigma_{@ (2)} &= \sigma_{@ (1)} + \gamma * d * K_a \\ &= 0.533 + (0.8 * d * 0.333) \\ &= 0.533 + 0.266d \end{aligned}$$

$$\sigma_p = \gamma * d * K_a = 0.8 * d * 3 = 2.4d$$

Force	Distance From Point O	Moment
$E_{@1}=0.5*4*4=8$	$d+\frac{4}{3}$	$8d+10.666$
$E_{@2}=4d$	$0.5d$	$2d^2$
$E_{@3}=0.5*2*0.533=0.533$	$\frac{2}{3}+d$	$0.35+0.533d$
$E_{@4}=0.533d$	$0.5d$	$0.267d^2$
$E_{@5}=0.5d*0.266d=0.133d$	$\frac{1}{3}d$	$0.0444d^3$
$E_{p1}=0.5*2.4d*d=-1.2d^2$	$\frac{1}{3}d$	$-0.4d^3$

Σ Moment

$$-0.355d^3+2.267d^2+8.533d+11.016 = 0$$

نقسم المعادلة علي -0.355

$$d^3 - 6.3859 d^2 - 24.03d - 31.031 = 0$$

$$d = 9.7 \text{ m}$$

$$(9.7)^3 - 6.3859 *(9.7)^2 - 24.03*9.7 - 31.031$$

$$= 47.7$$

$$L_1 = F.o.s * d = 1.2*9.7 = 11.64$$

$$L = 11.64 + 4 = 15.64 \cong 16 \text{ m}$$

Max moment at point of zero shear:

$$8+(4X)+0.533+0.533X+0.133X^2 - 1.2X^2 = 0$$

$$1.0667X^2 - 4.533X - 8.533 = 0$$

نقسم المعادلة علي 1.0667

$$X^2 - 4.25X - 8 = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$b = -4.25, a = 1, c = 8$$

$$x = \frac{4.25 + \sqrt{(4.25)^2 - (4 \cdot 1 \cdot 8)}}{(2 \cdot 1)} = 5.66 \text{ m}$$

$$M_{\max} = -0.355 \cdot (5.66)^3 + 2.267 \cdot (5.66)^2 + 8.533 \cdot 5.66 + 11.016 = 67.47 \cong 69 \text{ m.t/m'}$$

$$F = \frac{M}{Z_x}$$

$$F = 2.1 \text{ at steel 52}$$

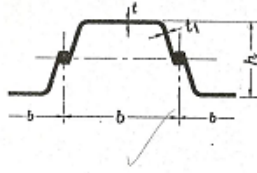
$$2.1 = \frac{69 \cdot 100}{Z_x}$$

$$Z_x = 3385.71 \text{ cm}^3/\text{m'}$$

Take sec VI from table

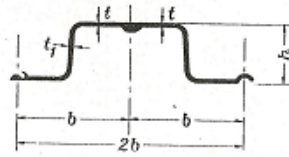
I.10. Properties of Steel Sheet Piles

a) LARCEN - TYPE



Profile	Dimensions mm				Weight		for 1m wall		
	b	h	t	t ₁	<i>g</i> Unit kg/m	<i>G</i> Wall kg/m ²	<i>W_x</i> cm ²	<i>A</i> cm ²	<i>U</i> cm
I	400	220	7.5	6.3	35.6	89	600	113	260
II	400	270	9.5	7.5	48.8	122	1100	156	301
III	400	290	13	9.5	62.0	155	1600	198	369
IV	400	360	14.8	10.0	74.0	185	2200	236	330
V	420	360	20.5	12.0	100.0	238	3000	305	330
VI	420	440	22	14.0	121.8	290	4200	370	368
VII	460	460	26	14.0	142.6	310	5000	394	370

b) HOESCH - TYPE



I	425	160	7	7	37.8	89	600	113	252
II	425	160	8	8	42.5	100	700	127	254
III	425	170	10.5	10.5	51.9	122	850	155	246
IV	425	200	9.50	8.5	51.9	122	1100	155	278
V	400	230	12	9.5	62	155	1600	197	291
VI	400	267	14	10.5	74	185	2200	236	306
VII	425	290	18	12	101.2	238	3000	303	327

profile section	Dimensions (mm)				Weigh	
	b	h	t	t ₁	g(kg/m)unit	G(kg/m ³ wall
VI	420	440	22	14	121.8	290